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# FiberSCIP – A shared memory parallelization of SCIP

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## Abstract

Recently, parallel computing environments have become significantly popular. In order to obtain the benefit of using parallel computing environments, we have to deploy our programs for these effectively. This paper focuses on a parallelization of SCIP (Solving Constraint Integer Programs), which is a MIP solver and constraint integer programming framework available in source code. There is a parallel extension of SCIP named ParaSCIP, which parallelizes SCIP on massively parallel distributed memory computing environments. This paper describes FiberSCIP, which is yet another parallel extension of SCIP to utilize multi-threaded parallel computation on shared memory computing environments, and has the following contributions: First, the basic concept of having two parallel extensions and the relationship between them and the parallelization framework provided by UG (Ubiquity Generator) is presented, including an implementation of deterministic parallelization. Second, the difficulties to achieve a good performance that utilizes all resources on an actual computing environment and the difficulties of performance evaluation of the parallel solvers are discussed. Third, a way to evaluate the performance of new algorithms and parameter settings of the parallel extensions is presented. Finally, current performance of FiberSCIP for solving mixed-integer linear programs (MIPs) and mixed-integer non-linear programs (MINLPs) in parallel is demonstrated.

## 1 Introduction

The paradigm of constraint integer programming (CIP) (formal definition of CIP will be presented in Section 2) developed by Achterberg (2007) combines modeling and solving techniques from the fields of constraint programming (CP), mixed-integer programming (MIP), and satisfiability testing (SAT). The paradigm allows us to address a wide range of optimization problems. SCIP is an implementation of the idea of CIP as a branch-cut-and-price framework and is now continuously extended by a group of researchers centered at Zuse Institute Berlin (ZIB), Technical University Darmstadt, and Friedrich-Alexander-University Erlangen-Nürnberg. SCIP 2.1.0 consists of more than 400,000 non-empty lines of C code and

can handle not only MIP, but also pseudo-Boolean optimization problems (Berthold et al., 2009), mixed-integer quadratically constraint programming problems (MIQCP) (Berthold et al., 2011, 2012), mixed-integer nonlinear programming problems (MINLP) (Vigerske, 2013), etc.

SCIP solves CIPs by a branch-and-bound algorithm. Therefore, SCIP is supposed to be a perfect candidate for parallelization. However, it involves a mathematically supercharged tree search algorithm, employing sophisticated algorithms to keep the enumeration effort small as follows: At each subproblem, domain propagation is performed to exclude further values from the variables domains and a relaxation may be solved to obtain a local dual bound. The relaxation may be strengthened by adding further valid constraints (e.g., linear inequalities), which cut off the optimal solution of the relaxation. In case a subproblem is found to be infeasible, conflict analysis is performed to learn additional valid constraints (conflict clauses). Primal heuristics are used as supplementary methods to improve the primal bound, which is used to prune the branch-and-bound tree.

Since parallel computing environments have become significantly popular nowadays, commercial MIP solvers such as CPLEX, Gurobi, and Xpress work in parallel on multi-core desktop computers. The development of **FiberSCIP**, a parallel version of SCIP on desktop computers, started in 2010. Unfortunately, parallelization was not in the initial design scope of SCIP, though SCIP was designed to be used as a thread-safe library. In order to parallelize the tree search of SCIP internally, one would have to redesign SCIP very carefully in order to keep its plugin-based design structure. On top of that, all developers of SCIP would have to take this parallelism into account. Therefore, we decided to parallelize the tree search for a single problem from “outside”, that is, such that each thread uses its own SCIP instance to work on its subproblem. This paper introduces this solver for use on a shared memory multi-core computer in detail. Preliminary computational results already appeared in Koch et al. (2011) (where it was called `ug [SCIP/spx]`) and on Hans Mittelmann’s benchmark page (Mittelmann, 2011).

There already exist a number of parallel state space search or tree search software frameworks (Goux et al., 2001; Ralphs et al., 2004; Eckstein et al., 2009; van Nieuwpoort et al., 2010; Sun et al., 2011; Bendjoudi et al., 2012)<sup>1</sup>. Especially recent ones are very scalable from a parallel tree search point of view. However, the examples used to show their scalability can often be considered as “easy” for state-of-the-art algorithms, thus not allowing for conclusions about their performance when combined with sophisticated solver implementations. For example, Sun et al. (2011) presented results for scaling up to 4096 processors on the basis of a Traveling Salesman Problem instance with only 25 cities. Further, it can be hard to integrate state-of-the-art solving algorithms into a scalable parallel tree search framework, because the algorithms already exploit very sophisticated tree search methods with shared knowledge and are therefore hard to adjust to an external tree search framework in general.

From a problem solving point of view, parallel implementations of SAT solvers, see

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<sup>1</sup>We cited here only some of those which are still accessible. Many other frameworks have disappeared because the platform or used libraries are not available anymore.

Martins et al. (2012) for a good survey, have been solving harder and larger instances than what was possible by state-of-the-art sequential solvers. Regarding MIP solving, Xu et al. (2009) summarized many software packages for solving MIP in parallel. These solvers are categorized in two types, those which are basically build from scratch (Eckstein, 1994; Linderoth, 1998; Bixby et al., 1999; Chen and Ferris, 2000; Chen et al., 2001; Eckstein et al., 2001; Ralphs et al., 2003, 2011) and the others which embed an already existing powerful sequential/multi-threaded MIP solver (Mitra et al., 1997; Shinano et al., 2003; Nwana et al., 2004; Shinano and Fujie, 2007; Shinano et al., 2008; Bussieck et al., 2009; Shinano et al., 2012). Only a very few members of the latter category obtained competitive problem solving results when compared to state-of-the-art sequential programs at their time. One exceptional case is Bixby et al. (1999), which solved two open instances to exploit parallelism and a new branching variable selection rule. To the best of our knowledge, only GAMS/CPLEX/Condor (Bussieck et al., 2009) and ParaSCIP (Shinano et al., 2012) solved successfully several open instances from the popular MIPLIB2003 and MIPLIB2010 instance libraries (Achterberg et al., 2006; Koch et al., 2011) by using massively parallelized MIP solvers.

Our approach to build **FiberSCIP** is to parallelize tree search from “outside” of **SCIP** by dynamically splitting up the search tree and maintaining each subtree in a separate **SCIP** instance. **SCIP**’s sophisticated tree search is performed in each **SCIP** solver, thereby directly benefiting from the state-of-the-art solving techniques of **SCIP**. Only the distribution of open subproblems to **SCIP** solvers is controlled from “outside”, thereby trying to balance the workload effectively. An obvious disadvantage is that parallelization from “outside” leads to an inevitable overhead. **ParaSCIP**, which parallelizes **SCIP** for massively parallel distributed memory computing environment also from “outside”, has been run by using up to 7,000 cores on the supercomputer HLRN II<sup>2</sup> (Shinano et al., 2012; Koch et al., 2012). Since **ParaSCIP** targets on solving very hard instances, where the overhead could be neglected, **FiberSCIP** is intended to run on a normal desktop computer with multi-core processor(s). Therefore, implementing an “outside” parallelization with low overhead on desktop computers is challenging, but also brings several advantages. That is, **FiberSCIP** virtually gives a development environment for **ParaSCIP**, because the both solvers are implemented in the same software framework, named *Ubiquity Generator (UG) framework*<sup>3</sup>. Thus, algorithmic improvements done for **FiberSCIP** can be used directly in **ParaSCIP** and **FiberSCIP** can be used to gain some insight into the performance of **ParaSCIP**. Further, since parallelization is done from “outside”, effects of different parallelization strategies can be investigated more clearly and **SCIP** solver developers can concentrate on improving algorithmic or mathematical technique within **SCIP** without caring about parallelization aspects.

Even if the parallelization feature is completely separated, the evaluation of the performance of parallel MIP or MINLP solvers on actual computers is difficult. This paper will illustrate these difficulties and investigate their source. The following sections are

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<sup>2</sup><https://www.hlrn.de/>

<sup>3</sup><http://ug.zib.de/>

organized as follows. First, we formally define the problem classes CIP, MIP, and MINLP, and introduce SCIP briefly. Next, we explain main concepts of the UG framework, its instantiation in form of FiberSCIP, and the implementation of deterministic parallelism. After that, extensive computational experiments investigate various aspects of the performance of FiberSCIP. We finish with some concluding remarks.

## 2 SCIP

SCIP is the implementation of the idea of CIP. CIP is formally defined as follows:

**Definition 1** (constraint integer program). A *constraint integer program* (CIP) is a tuple  $(\mathfrak{C}, I, c)$  that encodes the task of solving

$$\min\{\langle c, x \rangle : \mathfrak{C}(x), x \in \mathbb{R}^n, x_I \in \mathbb{Z}^{|I|}\},$$

where  $c \in \mathbb{R}^n$  is the objective function vector,  $\mathfrak{C} = \{\mathcal{C}_1, \dots, \mathcal{C}_m\}$  specifies the constraints  $\mathcal{C}_j : \mathbb{R}^n \rightarrow \{0, 1\}$ ,  $j \in [m]$ , and  $I \subseteq [n]$  specifies the set of variables that have to take integral values. Further, a CIP has to fulfill the condition

$$\forall \hat{x}_I \in \mathbb{Z}^{|I|} \exists (A', b') \in \mathbb{R}^{k \times n} \times \mathbb{R}^k : \{x \in \mathbb{R}^n : \mathfrak{C}(x), x_I = \hat{x}_I\} = \{x \in \mathbb{R}^n : A'x \leq b'\}, \quad (1)$$

where  $C := [n] \setminus I$  and  $k \in \mathbb{N}$ .

Condition (1) states that the problem becomes a linear program when all integer variables are fixed. Thus, if the discrete variables are bounded, a CIP can be solved, in principle, by enumerating all values of the integral variables and solving the corresponding LPs.

A CIP where all constraints are linear is a mixed-integer linear program (MIP):

**Definition 2** (mixed-integer linear program). A *mixed-integer linear program* (MIP) is given by a tuple  $(A, b, c, I)$  with matrix  $A \in \mathbb{R}^{m \times n}$ , vectors  $b \in \mathbb{R}^m$  and  $c \in \mathbb{R}^n$ , and a subset  $I \subseteq [n]$ . The task is to solve

$$\min\{\langle c, x \rangle : Ax \leq b, x_I \in \mathbb{Z}^{|I|}\}. \quad (2)$$

Extending the definition of MIP towards nonlinear objective and constraint functions leads to the class of mixed-integer nonlinear programs (MINLPs):

**Definition 3** (mixed-integer nonlinear program). A *mixed-integer nonlinear program* (MINLP) is given by a tuple  $(c, g, I)$  with vector  $c \in \mathbb{R}^n$ , a function  $g : \mathbb{R}^n \rightarrow \mathbb{R}^m$ , and a subset  $I \subseteq [n]$ . The task is to solve

$$\min\{\langle c, x \rangle : g(x) \leq 0, x_I \in \mathbb{Z}^{|I|}\}.$$

Unlike MIP, MINLP is in general not a special case of CIP, since the nonlinear constraint  $g(x) \leq 0$  may forbid a linear representation of the MINLP after fixing the integer variables, i.e., (1) would be violated (unless  $I = [n]$ ). However, the main purpose of condition (1) is to ensure that the problem that remains after fixing all integer variables in the CIP can be solved efficiently. For practical applications, a spatial branch-and-bound algorithm that can solve the remaining nonlinear program within a finite number of steps up to a given precision is sufficient.

SCIP solves MIPs and MINLPs by a branch-and-bound algorithm that utilizes an LP relaxation for bounding. For a MIP, the LP relaxation is readily given by dropping the integrality restrictions from (2). For a MINLP, the LP relaxation is constructed by computing for each function  $g_j(x)$ ,  $\forall j \in \{1, \dots, m\}$ , linear functions that underestimate  $g_j(x)$  for all  $x$  within the current variable bounds, see also Vigerske (2013) for details. The “convexification gap” between the underestimator of  $g_j(x)$  and  $g_j(x)$  itself depends on the width of the domain of the variables involved in  $g_j(x)$ . Thus, to close this gap, branching on any variable that is involved in  $g_j(x)$  may be applied.

As the variety of different problem types indicates, SCIP a very flexible framework. This is a result of the chosen design. SCIP follows a plugin design which allows for easy customization. This is very handy for the “outside” parallelization, which is introduced in this paper. As a consequence of the design, SCIP is a constraint based system. Each type of constraint is handled by a so-called constraint handler. For MIP instances this can be a disadvantage, since no central matrix exist as it is common for pure MIP solvers. On the other hand, this allows for easy extension to other problem classes. Since FiberSCIP parallelizes the tree search from the “outside”, any problem class which is solvable with SCIP can be handled in parallel without additional work as long as branching is performed on variables only.

### 3 ParaSCIP and FiberSCIP

ParaSCIP and FiberSCIP have been developed by using a single software framework: *Ubiquity Generator(UG) framework*. UG is written in C++. Fundamental mechanisms required to parallelize tree search based MIP/MINLP solvers are provided by UG. Thus, the basic concept of UG is to abstract from an actual MIP/MINLP solver and communication library and to provide a framework that can be used, in principle, to parallelize any powerful state-of-the-art MIP/MINLP solver on any computational environment (shared or distributed memory, multithreading or massively parallel). For a particular MIP/MINLP solver, only the interface to UG in form of specializations of base classes, as provided by UG, needs to be implemented. Similarly, for a particular communication library (e.g., MPI), a specialization of an abstract UG class is necessary.

### 3.1 Basic concept of having two parallel extensions

Generally, parallel tree search based solvers have three running phases, see also Ralphs (2006) and Xu et al. (2009): the *ramp-up phase* is the time period from the beginning until sufficiently many branch-and-bound nodes are available to keep all processing units busy the first time, the *primary phase* is the period between the first and last time all processing units were busy, and the *ramp-down phase* is the time period from the last time all processing units were busy until problem solving finished<sup>4</sup>. UG provides several ramp-up mechanisms to shorten the ramp-up phase, a dynamic load balancing mechanism for all three phases, and a check-pointing and restarting mechanism (see Shinano et al. (2012)) as generic functionality.

The message passing functions used in UG are limited to the least necessary and are wrapped within a base class. Therefore, adding support for an additional parallelization library should be easy. The most used libraries for implementing distributed parallel programs are MPI (Message Passing Interface) implementations. The virtual functions in the base class provided by UG can be mapped straightforward onto corresponding MPI functions. Pthreads is a popular library that is used to make multi-threaded programs and the UG specialization for Pthreads uses a simple message queue implementation. From the UG framework point of view, a particular instantiated parallel solver is referred as:

`ug` [a specific solver name, a specific communication library name].

Using this notation, ParaSCIP is `ug` [SCIP, MPI] and FiberSCIP is `ug` [SCIP, Pthreads]. As ParaSCIP already existed, the realization of FiberSCIP only required to add code to interface with Pthreads as communication library. Note that UG framework is not restricted to SCIP, which can be replaced by any other thread-safe solver.

One of the motivations to have both FiberSCIP and ParaSCIP is to have a systematic development environment for a large scale parallel branch-and-bound based solver based on SCIP. While FiberSCIP has completely the same generic parallelization mechanism as ParaSCIP, FiberSCIP (as a single process program) is much easier to debug than the MPI based ParaSCIP. For example, moving the communication point, see Section 3.4, was only possible due to the availability of FiberSCIP, since it leads to large debugging efforts. Further, also non-deterministic behavior leads to difficulties for debugging, as it may prohibit consistent reproducibility of a faulty program flow. Therefore, a deterministic parallel execution capability was introduced to UG when implementing FiberSCIP.



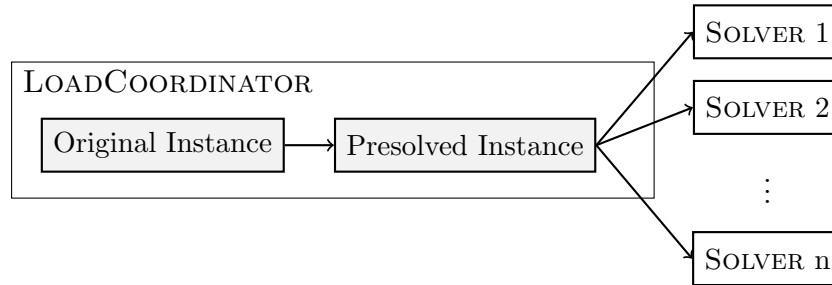


Figure 1: Initialization step

### 3.2 Parallelization mechanism provided by UG

UG provides a common parallelization mechanism that works in both ParaSCIP and FiberSCIP. The latter has two types of threads. One is the `LOADCOORDINATOR` which makes all decisions about the dynamic load balancing, the other is the `SOLVER` which solves subproblems. In the beginning, the `LOADCOORDINATOR` reads the instance data for a MIP/MINLP model which we refer to as the *original instance*. This instance is presolved directly inside the `LOADCOORDINATOR`. Different techniques try to fix or tighten variables, tighten constraints and detect and remove redundancies, for details see Achterberg (2007). The resulting, typically smaller, instance will be called the *presolved instance*. Note that the presolved instance is always converted to a minimization problem. The presolved instance is extracted from the `SCIP` environment, is broadcasted to all available `SOLVER` threads, and is embedded into the (local) `SCIP` environment of each `SOLVER`. This is the only time when the complete instance is transferred. Later, only the differences between a subproblem and the presolved problem will be communicated. Figure 1 illustrates this initialization procedure. At the end of this initialization, all `SOLVERS` are instantiated with the presolved instance.

After the initialization step, the `LOADCOORDINATOR` creates the root node of the branch-and-bound tree. Each node transferred through the system, we call such a node `PARANODE`, acts as the root of a subtree. The information that has to be sent consists only of bound changes of variables between the presolved instance and the subproblem which gets transferred. For the initial root node there is no difference between the presolved instance and the subproblem, thus it contains only administrative information such as a `PARANODE` identifier.

All nodes which are transferred to `SOLVERS` are kept in the `LOADCOORDINATOR` with their solver statuses until the corresponding solving process terminates. The `SOLVER` which

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<sup>4</sup>Note that this definition of ramp-down phase is different from the definition in Ralphs (2006), in which the ramp-down phase is loosely defined to start when the number of available tasks (subproblems) first falls below the number of available processors. In our system, we sometimes observed this situation during the period we consider the “primary phase”. However, when our load balancing mechanism detected this situation, the mechanism also recovered well from this imbalance of workloads among `SOLVERS`, so that enough tasks (subproblems) were generated to keep all `SOLVERS` busy again. Therefore, we use the different definition of the ramp-down phase.

receives a new branch-and-bound node instantiates the corresponding subproblem using the presolved instance (which was distributed in the initialization step) and the received bound changes. After that, the SOLVER starts working on the subproblem.

UG has two kinds of ramp-up mechanisms.

**Normal ramp-up** Active SOLVERS, which are the ones that already received a branch-and-bound node, are solving this subproblem by alternately solving nodes and transferring half of the child nodes back to the LOADCOORDINATOR. The LOADCOORDINATOR has a *node pool* to keep unassigned nodes, from which it assigns nodes to idle SOLVERS as long as an idle SOLVER exists. Even if none exists, the LOADCOORDINATOR still keeps collecting nodes from SOLVERS until it has  $p$  “good” (promising to have a large subtree underneath) unassigned nodes in its node pool. Here,  $p$  is a run-time parameter of UG, which in case of FiberSCIP is set to half of the number of SOLVER threads as default. When the LOADCOORDINATORs node pool accumulated  $p$  “good” nodes, it sends a message to quit sending nodes to all SOLVERS.

**Racing ramp-up** In this mechanism, the LOADCOORDINATOR sends the root branch-and-bound node to all SOLVERS and all SOLVERS start solving the root node of the presolved instance immediately. In order to generate different search trees, each SOLVER uses a different variation of parameter settings, branching variable selections, and permutations of variables and constraints. As shown in Koch et al. (2011), the latter can have a considerable impact on the performance of a solver. Due to these variations, we can expect that many SOLVERS independently generate different search trees. However, an incumbent solution found by one of the SOLVERS is broadcasted to all other SOLVERS and is used to prune parts of the SOLVERS search trees. Under certain criteria, involving the duality gap and the number of open nodes of each SOLVER, a particular SOLVER is chosen as “winner” of the *racing stage*. All open nodes of the winner SOLVER are then collected by the LOADCOORDINATOR and a termination message is sent to all other SOLVERS. Next, the collected nodes are redistributed to all idle SOLVERS. If the winner SOLVER did not provide enough nodes, UG changes its strategy to normal ramp-up. If a SOLVER solves the complete problem during racing stage, the LOADCOORDINATOR terminates all SOLVERS and the solving process is finished.

Racing ramp-up has been designed to run on large scale distributed memory computing environments. In such an environment, normal ramp-up can take much time, i.e., many SOLVERS stay idle until the ramp-up finishes. We note, that racing ramp-up has already been considered in Mitra et al. (1997) and Nwana et al. (2004). In order to use it with state-of-the-art MIP solvers on large scale distributed computing environments, our extended implementation can switch to the second stage seamlessly without waiting for all SOLVERS to terminate the first stage and can switch to normal ramp-up adaptively. Although the racing stage in racing ramp-up, which can be considered as a “learning” or “tuning” process, is a

sequential process, all SOLVERS become active immediately after the LOADCOORDINATOR finished presolving. There are many ways when and how to choose the winner and how to distribute the branch-and-bound nodes of the winner. The racing ramp-up configuration of FiberSCIP will be explained in detail in the beginning of Section 4.4.

Load balancing for MIP solving highly depends on the *primal* and *dual bounds* (*upper* and *lower bounds* on the optimal value, since the presolved instance is always a minimization problem), which are updated during the solving process. The primal bound is given by the value of the best solution that has been found so far during the solving process. If one of the SOLVERS finds an improved solution, this solution is sent to the LOADCOORDINATOR, which distributes the updated primal bound or the new solution to all other SOLVERS, which will then immediately apply bounding, hence, prune all nodes in its search tree that cannot contain any better solution anymore, which is proven by the node dual bound.

Periodically, each SOLVER notifies the LOADCOORDINATOR about the number of unexplored nodes in its SCIP environment and the dual bound of its subtree; we call this information the *solver status*. The dual bound is a proven lower bound on the objective function value of the best solution in that subtree. It is derived from the linear programming relaxations at the individual nodes. At the same time, the SOLVER is notified about the lowest dual bound value of all nodes in the node pool of the LOADCOORDINATOR, which we will refer to as BESTDUALBOUND. Note that this does not include nodes that are currently processed by any SOLVER.

If a SOLVER is idle and the LOADCOORDINATOR has unprocessed nodes available in the node pool, the LOADCOORDINATOR sends one of these nodes to the idle SOLVER. To handle situations in which several solvers become idle at the same time, the LOADCOORDINATOR should always have a sufficient amount of unprocessed nodes left in its node pool. This ensures that the SOLVERS are kept busy throughout the computation, thus minimizing idle time. In order to keep at least  $p$  “good” nodes in the LOADCOORDINATOR, we introduce the *collecting mode*, similar to the one introduced in Shinano et al. (2008). We call a node *good*, if the dual bound value of its subtree (NODEDUALBOUND) is close to the dual bound value of the complete search tree (GLOBALDUALBOUND).

If the LOADCOORDINATOR is not in collecting mode and it detects that less than  $p$  good nodes with

$$\frac{\text{NODEDUALBOUND} - \text{GLOBALDUALBOUND}}{\max\{|\text{GLOBALDUALBOUND}|, 1.0\}} < \text{THRESHOLD} \quad (3)$$

are available in the node pool, the LOADCOORDINATOR switches to collecting mode and requests selected SOLVERS that have nodes which satisfy (3) to switch also into collecting mode. The selection is done in ascending order of the minimum lower bound of open nodes in the SOLVERS. The number of selected SOLVERS increases dynamically depending on the time that the node pool in the LOADCOORDINATOR has been empty. If the LOADCOORDINATOR is in collecting mode and the number of nodes in its pool that satisfy (3) is larger than  $m_p \cdot p$ , it requests all collecting mode SOLVERS to stop the collecting mode. Note that  $m_p$  is a runtime parameter and is set to 1.5 as a default value.

If a SOLVER receives the message to switch into collecting mode, it changes the search strategy to either “best estimate value order” or “best bound order” (see Achterberg (2007)) depending on the specification of UG run-time parameters. It will then alternately solve nodes and transfer them to the LOADCOORDINATOR. This is done until the SOLVER receives the message to stop the collecting mode. If a node of the branch-and-bound tree is selected to be sent to the LOADCOORDINATOR, the corresponding SOLVER collects the bound changes of that node w.r.t. the presolved instance, transfers the differing bounds to the LOADCOORDINATOR, and prunes the node from the subproblem’s branch-and-bound tree.

The most crucial issue for the load balancing mechanism is to avoid solving useless subproblems. Consider the situation that a SOLVER is solving a subproblem N for which the dual bound is already quite large. An improvement in the primal bound will then cause all nodes of this subproblem to be pruned. The SOLVER can detect this situation locally using the best dual bound value of all nodes in the node pool of the LOADCOORDINATOR (BESTDUALBOUND). In this situation, the SOLVER requests another node from the LOADCOORDINATOR while still continuing to solve the current node. After the LOADCOORDINATOR sent a new node to the SOLVER and restored the solving node N in its node pool, the SOLVER stops the solution process and restarts with the new node. The solution of node N is “delayed”. Note that in case that there is no node available in the LOADCOORDINATOR, the SOLVER keeps continuing to solve node N. Further, note that the SOLVER takes a coordinating role here. Reasons for this exceptional behavior is that, first, the SOLVER can detect such a situation earlier than the LOADCOORDINATOR, which has only delayed information, and, second, that it simplifies the process in cases where many SOLVERS get into a similar situation.

The termination phase starts when the LOADCOORDINATOR detects that the node pool is empty and all SOLVERS are idle. In this phase, the LOADCOORDINATOR collects statistical information from all SOLVERS and outputs the optimal solution and the statistics.

### 3.3 Difference between ParaSCIP and FiberSCIP

As already mentioned, the fundamental difference between ParaSCIP and FiberSCIP is the communication library. However, also the initialization of the SOLVERS with the presolved instance is different. Since FiberSCIP runs on a shared memory machine, a pointer to the SCIP environment can be moved between threads easily and the presolved instance is created by using the problem copying functionality of SCIP. Therefore, extensions of SCIP by user-defined constraint handlers can be used straightforwardly in FiberSCIP. ParaSCIP can also handle the large classes of problems that are implemented in SCIP. However, since the SOLVERS do not share the same memory, they have to be initialized either by transferring a serialized form of the presolved instance from the LOADCOORDINATOR or by reading the original problem from file and running presolve on the SOLVER side. Future versions of ParaSCIP will offer further possibilities.

### 3.4 The point of communication in ug [SCIP, \*]

We define the *communication point* as a function called in a SOLVER, in which a series of communications between the LOADCOORDINATOR and the SOLVER are done by message passing including a sending message operation from the SOLVER side. Since several communication points have a risk to introduce an opportunity for dead-locks, both ParaSCIP and FiberSCIP are restricted to use only one communication point, even though the UG framework does not have this restriction.

Originally, the communication point was limited to the time when a branch-and-bound node was selected for processing. That means, at that point in time, the decision has to be made whether this node is solved or passed to the LOADCOORDINATOR. Note that this is the only time during branch-and-bound node processing where the LOADCOORDINATOR can communicate with a SOLVER by sending a message, e.g. to interrupt the current solving process. However, it also means that no communication between the LOADCOORDINATOR and a SOLVER can happen during the processing of a branch-and-bound node, so that vivid response to a request message from the LOADCOORDINATOR may not be possible. This delay can sometimes lead to useless computations. For example, when the LOADCOORDINATOR has decided a winner SOLVER during racing ramp-up, it sends a request message to interrupt the computation in all SOLVERS other than the winner. As the SOLVERS delay reception of these messages, they first finish processing of their current branch-and-bound node before discarding their current subproblems.

To allow for more frequent communication, we added additional communication points. These are after every variable bound change, every solve of the LP relaxation, every modification of the LP, or finding of a new incumbent. This leads to very different communication patterns between the LOADCOORDINATOR and SOLVERS compared to previous implementation. Now, expensive node solving may be interrupted earlier due to pruning.

### 3.5 Implementation of deterministic parallelism

When a user of UG has a brilliant idea for improving performance, e.g., by transferring more information inside a PARANODE, FiberSCIP is a suitable development environment due to its easier debugging possibilities. However, non-deterministic behavior can still make testing and debugging difficult and inefficient. Even though technology like deterministic multiprocessor replay, which can be used to debug non-deterministic programs, is getting more practical (Montesinos et al., 2009), it fundamentally still needs too much resources to apply it to general MIP/MINLP solvers. Therefore, adding the possibility to execute FiberSCIP deterministically is an essential feature for debugging.

Another motivation for implementing a deterministic parallelism in UG is the hope that computational experiments in deterministic mode can be used to predict performance improvements in non-deterministic execution mode. Note, that in the development of SCIP, even small improvements in geometric mean running time for a set of benchmark instances are, in general, crucial to accept a new feature. If repeated runs of FiberSCIP with

the same parameter settings and the same computing environment but non-deterministic behavior produce computational results with more than, say, 10% variation in geometric mean, we have to evaluate the effectiveness of the new feature by averaging the value of several repeated runs. If a deterministic execution could be used to predict the average running time of several non-deterministic runs, the amount of necessary computational experiments could be reduced. However, we note that also with deterministic behavior, several repeated runs of a solver, each using a different random seed or permutation of variables and constraints, on a set of instances may be necessary to get a clear picture of the performance improvement that can be expected by a new feature (Koch et al., 2011).

Deterministic parallelism is also one of the most important features of commercial optimization solvers, because a user of a solver expects that repeated executions on the same computer generate the same results. Therefore, commercial optimization solvers such as CPLEX, GUROBI, and XPRESS have a deterministic option, which is also enabled by default. For all of these solvers, deterministic parallelism is implemented based on their shared memory computing environments. However, since UG is intended to run also on distributed memory computing environments, a new mechanism to implement deterministic parallelism had to be introduced. As UG has an inherent non-deterministic behavior, its deterministic option realizes a *weak* deterministic parallelism (Olszewski et al., 2009), that is, the program is still executed in a non-deterministic way, but it ensures that repeated runs with the same parameter settings and on the same computing environment generate always the same search tree and give the same optimal solution.

In UG, all communications are done between the LOADCOORDINATOR and the SOLVERS. Therefore, all messages are serialized in the LOADCOORDINATOR. A basic idea to implement deterministic parallelism is to ensure that messages between LOADCOORDINATOR and SOLVERS are in the same order in repeated runs. One tool needed to realize this deterministic behavior is a *deterministic timer*, which is called deterministic clock in Olszewski et al. (2009), and which is a counter to indicate progress of computation in a SOLVER. Ideally, intervals of the counter are distributed almost uniformly with respect to wall-clock time. However, since it is difficult to have such an ideal deterministic timer with SCIP, a counter for the number of communication point calls is used as deterministic time. Although the intervals of the calls are not uniform, it is called frequently. Another tool is a *token* that is circulated among SOLVERS via the LOADCOORDINATOR in a predefined order. SOLVERS can execute until reaching specific points of time in deterministic time. If the SOLVER reached such a point, it has to wait until it receives the token. Once it got the token, it can do a series of message passes and then hands over the token to the next SOLVER via the LOADCOORDINATOR. If an idle SOLVER receives the token, it passes it on immediately.

This token circulation mechanism is similar to the one of Liu et al. (2011). We note the following points: First, the token is not sent to the next SOLVER directly, but it is sent as an ordinary message via the LOADCOORDINATOR, thus it does not require a shared memory architecture. Second, the general parts of token passing and deterministic timer are implemented in the UG framework, while the actual deterministic timing mechanism is specialized for each solver.

## 4 Computational results

FiberSCIP is intended to run on a shared memory computing environment with small scale parallelization and only a few hours of computing time. Therefore, all computational experiments conducted in this paper have a two hours time limit. The objective of the computational experiments is not only to analyze the performance of FiberSCIP, but also to point out difficulties of performance evaluation.

At first, we analyze the fundamental overhead of FiberSCIP compared to SCIP and give baseline sequential computational results for comparison. Second, in order to clarify the effects of using several SOLVER threads, we present computational results when omitting parallel tree search. Finally, we evaluate our parallel tree search computational results for solving MIPs and MINLPs with four and eight SOLVER threads. For MIP, we also present results when using deterministic parallelism.

For all our experiments we present the following numbers:

- The “geometric mean (solved:  $n$ )” is computed w.r.t. the  $n$  instances that are solved in all runs within one experiment. It is given for the number of search nodes and for the running time.
- The “geometric mean (all)” of time is computed w.r.t. all instances, where aborts and timeouts are accounted with the time limit of 7200 seconds. Note, that we omit this measure for the number of search nodes, since it is not clear how aborted instances should be accounted.
- The “solved/timeout/abort” rows shows the number of solved instances, the number of instances that hit the time limit, and the number of aborted instances.
- The “speedup (solved:  $n$ )” is computed w.r.t. the  $n$  instances which are solved in all runs within one experiment.

The detailed computational results are given in the Appendix.

### 4.1 Setup for computational experiments in MIP solving

Computational experiments were conducted on 40 PowerEdge™ 2950 computers, each equipped with two Quad-Core Xeon E5420 CPUs at 2.5 GHz and 16 GB RAM.

The 87 instances of the benchmark set of MIPLIB2010 (Koch et al., 2011) are used for the computational experiments. Table 6 in Appendix shows for each instance the total number of variables, the number of constraints, and the number of variables of certain type in the original and presolved problem. For the latter, the table also shows the product of the number of variables and number of constraints, which will serve as a rough and simple estimate for the certain memory usage.

We used SCIP version 2.1.1 in default settings, except that we set the time limit in the Chvátal-Gomory separator to infinity to prohibit a non-deterministic behavior of this SCIP

Table 1: Comparing the sequential executions of SCIP and FiberSCIP. Instancewise results are shown in Table 8.

Summary	SCIP		FiberSCIP			
			Presolve Once		Presolve Twice	
	Nodes	Time	Nodes	Time	Nodes	Time
geom. mean (solved: 56)	8711	623.5	8718	623.7	9204	669.5
geom. mean (all)	–	1466.2	–	1467.9	–	1554.7
solved/timeout/abort	58/22/7		59/20/8		58/21/8	
speedup (solved: 56)	reference		1.000		0.931	

version<sup>5</sup>. In order to standardize memory usage of each SOLVER thread, we assume 2GB of RAM for each SOLVER thread and therefor set the SCIP option `limits/memory` to 1600 (the memory usage of the LP solver cannot be measured). As a consequence, SCIP switches the search strategy to depth first search when the memory usage of SCIP (excluding the LP solver) reaches 80% of 1.6GB.

## 4.2 Fundamental overhead of FiberSCIP

Even if FiberSCIP runs with only one SOLVER thread, the original instance is presolved twice in default settings, once in the LOADCOORDINATOR and once in the SOLVER. In order to clarify the communication overhead between the LOADCOORDINATOR and the SOLVER, we also conducted computational experiments where presolving in the LOADCOORDINATOR was prohibited.

Table 1 summarizes the computational results of sequential runs executed by SCIP, FiberSCIP without presolving in the LOADCOORDINATOR, and FiberSCIP with double presolving (in the LOADCOORDINATOR and in the SOLVER). Figure 2 visualizes the speedup of the one thread FiberSCIP runs w.r.t. SCIP for all solved instances (56 in total). We see, that FiberSCIP with one presolve usually takes the same computing time as SCIP. The number of nodes processed by SCIP and that of FiberSCIP with one presolve is expected to be completely the same. However, Table 8 shows differences for only three instances (`timtab1`, `triptim1` and `zib54-UUE`). As FiberSCIP installs additional plugins into SCIP (e.g., event handler), its memory usage is slightly different, which seems to cause this difference. That is, due to different amounts of allocated memory, computations that get close to the specified memory limit may change the node selection strategy to depth first search at different points of the search. FiberSCIP (with single presolving) took basically the same computing time in geometric mean, which indicates that there is almost no communication overhead between the SOLVER and the LOADCOORDINATOR. Note that FiberSCIP solves one more instance (`zib54-UUE`), shortly before hitting the time limit (Table 8). Analyzing this issue more carefully reveals that FiberSCIP changes to depth first search earlier due to reaching

<sup>5</sup>SCIP 3.0 has this option set to infinity by default.



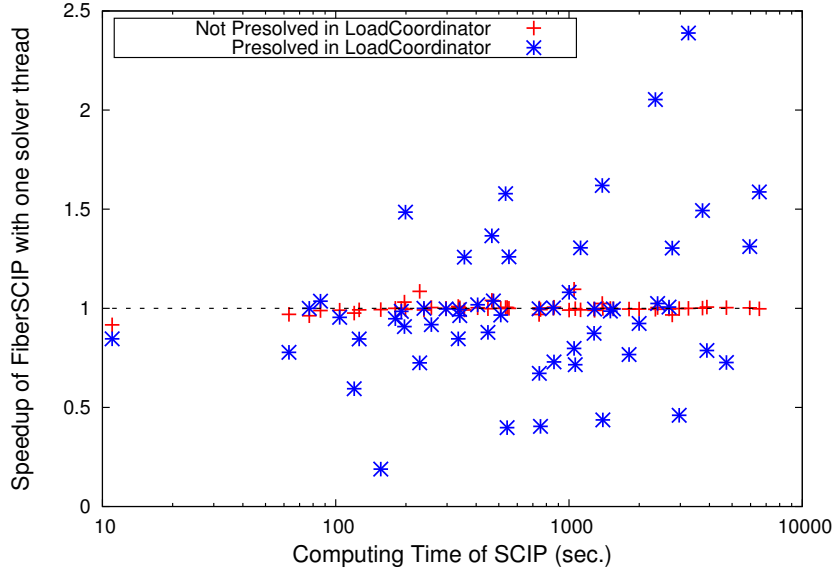


Figure 2: Computing time of FiberSCIP relative to SCIP.

the memory limit (see Section 4.1), which is resulting in a better performance here.

Figure 2 also shows that FiberSCIP with double presolving works different to SCIP, one can observe both speedups and slowdowns depending on the instance. These differences result from the additional presolving in the LOADCOORDINATOR and therefore the SOLVER gets a changed instance. This leads to a 7% increase in the geometric mean of the computing time when using FiberSCIP with double presolve compared to SCIP using one thread. But to avoid repeating the same preprocessing steps multiple times when using multiple SOLVER threads and also to keep the memory consumption as small as possible, double presolving was decided to be the default setting in FiberSCIP. Using it with one SOLVER thread will serve us as the baseline for comparisons with the runs that use multiple SOLVER threads.

### 4.3 Omitting parallel tree search

We conducted two computational experiments running FiberSCIP in racing stage throughout the whole computation, meaning that the ramp-up phase is never left and thus the parallel tree search is omitted. First, we were disabling communication of the incumbents, whereas it was enabled in the second experiment. The SCIP parameter settings for each racing SOLVER is a combination of the emphasis settings “off”, “fast”, “default”, and “aggressive” for the different groups of components like primal heuristics, presolvers, and separators. Exactly one SOLVER ran with SCIP’s default settings.

#### 4.3.1 Racing without communication of incumbents

In this subsection, we are evaluating the possible speedups when omitting communication of incumbents. Independent sequential SOLVER threads ran in parallel with different parameter

Table 2: Comparing the sequential execution of FiberSCIP with one SOLVER thread to two, four, six, and eight SOLVER threads in racing stage throughout computation without communication of incumbents. Detailed results are shown in Table 9 in Appendix.

Summary	One thread		Two threads		Four threads		Six threads		Eight threads	
	Nodes	Time	Nodes	Time	Nodes	Time	Nodes	Time	Nodes	Time
geom. mean (solved: 51)	9817	573.9	8148	529.7	6935	507.5	6386	569.4	5905	672.0
geom. mean (all)	-	1554.6	-	1460.1	-	1434.4	-	1564.4	-	1723.6
solved/timeout/abort	58/21/8		60/20/7		60/21/6		59/23/5		56/27/4	
speedups (solved: 51)		reference	1.084		1.131		1.008		0.854	

settings. Theoretically, an increase in the number of threads should result in a better overall performance w.r.t. the running time and the number of solved instances. The choice of the winner is basically deterministic, though several highly competitive SOLVERS could introduce non-determinism.

Table 2 summarizes the results for racing without communication of incumbents when using one (which gives the baseline), two, four, six, and eight threads. From an algorithmic point of view, a higher number of independent SOLVER threads should lead to a monotonous decrease in minimal computing time and an increase in solved instances, but the results for using six threads show nearly the same overall performance in speed, i.e., a factor of only 1.008, and the number of solved instances compared to one thread. For eight threads we even encounter less solved instances and a slowdown by a factor of 0.854. Even though the SOLVER threads do not interact logically with each other, their actual parallel execution in a single machine increases the number of context switches by the operating system and can lead to more frequent major or minor page faults, cache misses, and collisions in memory access. We note that hard disk access for swapping (major page faults) has not been observed. In the following, we aim to clarify these effects further.

In order to investigate the change in performance of the winner solver, we selected the results of the 12 instances where the number of nodes processed is the same in all runs with one, two, four, six, and eight threads (marked by ‘(i)’ in Table 9). We assumed that an increase in memory access latency due to using more threads on the same machine is mostly responsible for the slow down effect. The latency is related to the fundamental memory usage of the solver. As an indicator of the memory usage, we use the product of number of variables and number of constraints of the presolved instance, see Table 6, because it is easy to obtain from SCIP and does not change during the solving process (as the actual memory usage does). Figure 3 shows the number of minor page faults for each number of SOLVER threads, left, and the number of context switches for each number of SOLVER threads, right, in relation to the memory usage indicator for the 12 instances. While these numbers do not seem to be related to the memory usage indicator, they usually increase with the number of threads. Note that for better visibility we connected data points belonging to the same number of threads.

The left picture in Figure 4 illustrates the speedups for the 12 selected instances. Except for instance `ex9` at the far left side of the graph, only slowdowns can be observed when

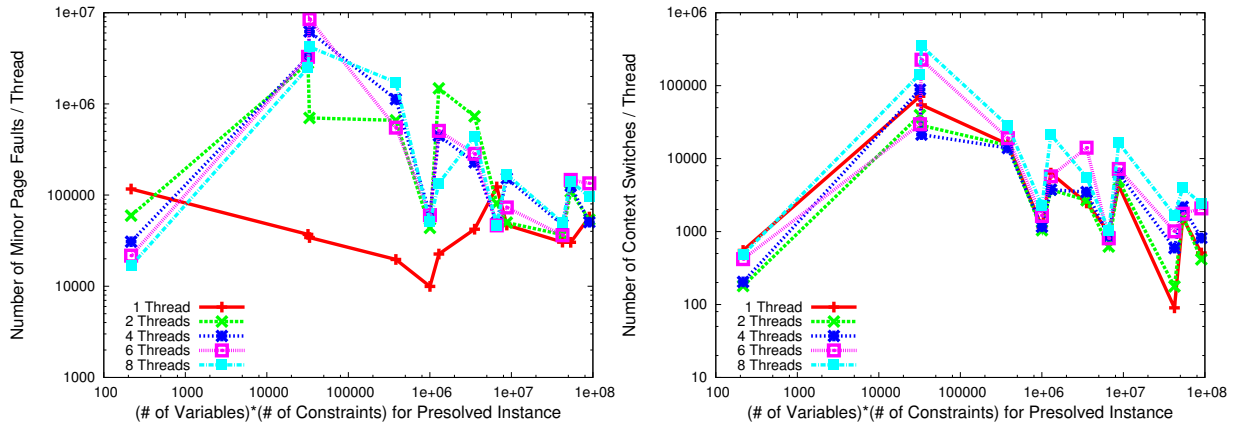


Figure 3: Minor Page faults (left) and Context switches (right) of FiberSCIP runs.

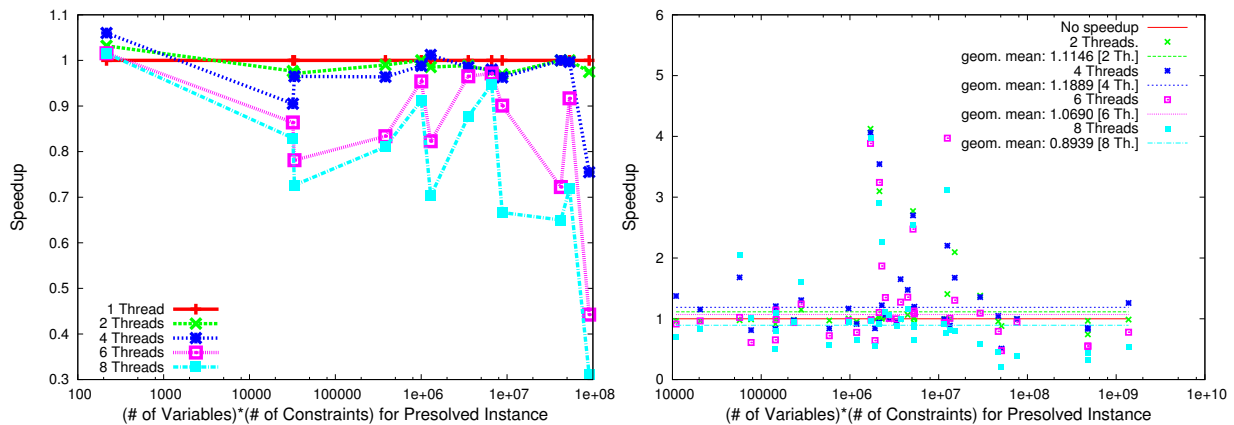


Figure 4: Computing time ratio of FiberSCIP for different numbers of SOLVER threads w.r.t. one thread for, first, the twelve instances in which the winner solver did not change (left) and, second, the 39 instances in which the winner solver changed (right).

adding more SOLVER threads. The reason is the increase in the number of minor page faults and context switches.

The right picture in Figure 4 illustrates the speedups for the other 39 instances that were solved in all runs. For these 39 instances, the winner SOLVER changed when more SOLVER threads were added. If the performance of each SOLVER thread would remain the same when changing the amount of solver threads, a speedup should be observed for each instance. For each run, also the geometric mean of the speedups is shown in the figure. We see that in the case of four SOLVER threads, the best speedup can be observed, while more than four SOLVER threads lead to a slow down.

Table 3: Comparing FiberSCIP in racing stage with and without communication of incumbents. Detailed results are shown in Tables 10, 11, 12, and 13 in Appendix.

(a) Four SOLVER Threads

Summary	Without comm.		Average			Summary	One thread		Average	
	Nodes	Time	Nodes	Time			Nodes	Time	Nodes	Time
geom. mean (solved: 57)	7110	620.7	6725.4	591.69		geom. mean (solved: 56)	9173	670.3	6116.8	582.89
geom. mean (all)	-	1434.4	-	1379.54		geom. mean (all)	-	1554.6	-	1379.54
solved/timeout/abort speedups (solved: 57)	60/21/6 reference		62.2/19.4/5.4 1.049			solved/timeout/abort speedups (solved: 56)	58/21/8 reference		62.2/19.4/5.4 1.150	

(b) Eight SOLVER Threads

Summary	Without comm.		Average			Summary	One thread		Average	
	Nodes	Time	Nodes	Time			Nodes	Time	Nodes	Time
geom. mean (solved: 52)	5128	706.1	4470.2	605.81		geom. mean (solved: 49)	9226	555.2	4781.2	552.68
geom. mean (all)	-	1723.6	-	1551.98		geom. mean (all)	-	1554.6	-	1551.98
solved/timeout/abort speedup (solved: 52)	56/27/4 reference		57.2/25.4/4.4 1.166			solved/timeout/abort speedups (solved: 49)	58/21/8 reference		57.2/25.4/4.4 1.005	

### 4.3.2 Racing with communication of incumbents

In contrast to the last subsection, we now enabled the communication of incumbents between SOLVER threads and LOADCOORDINATOR. We expect an overall performance improvement in running time. As execution is now non-deterministic, five repeated runs were conducted for each number of threads.

The left-hand side of Table 3 shows the results of only racing with communication of incumbents for four and eight SOLVER threads, respectively. In both tables, the results of only racing without communication of incumbents for the same number of SOLVER threads are set as a baseline to clarify the effect of communication. The runs with four SOLVER threads always solved more instances and lead to an improvement of the geometric mean over all solved instances. The runs with eight SOLVER threads did not always solve more instances, but the geometric mean running time decreased always. The speedups w.r.t. solved instances are always larger when compared to the results with four SOLVER threads. However, the mean speedups are calculated w.r.t. 57 instances in case of four SOLVER threads and only 52 instances in case of eight SOLVER threads. As long as an instance is solved in the time limit, more SOLVER threads reduce the solving time, since communication of a newly found incumbent in one SOLVER may allow to prune branch-and-bound nodes in the search trees of other SOLVERS.

The right-hand side of Table 3 summarizes the same results for four and eight SOLVER threads, respectively, except that the baseline result is replaced by the result for one SOLVER thread (FiberSCIP with double presolving, see Table 1). Communicating of incumbents lead in both cases to a decrease of the geometric mean running time and for four SOLVER threads also to an increase in solved instances. As expected, the performance increases when comparing the results against the runs without communication. For eight threads, we can even overcome the slowdown due to context switches and page faults.

Tables 14 and 15 in Appendix show the variations in the number of enumerated nodes and computing times of repeated runs for each instance that was solved. The numbers show a high variation for repeated runs with communication of incumbents. The maximal deviations for nodes is nearly 190%, while it is around 93% for time. This indicates, that doing several repeated runs of a non-deterministic algorithm is crucial in order to measure its performance.

### 4.3.3 Overall results on racing

Our results illustrate some of the difficulties in doing a parallel implementation which uses all computing resources efficiently. Tables 2 and 3 show that for four SOLVER threads, the number of solved instances increases by 4.2 and the speedup is 1.150 on average when communicating the incumbents, while they were only 2 and 1.131, respectively, when disabling the communication. For eight SOLVER threads, the number of solved instances decreases by 0.8 and the speedup is 1.005 in average when communication is enabled, while they were 2 and 0.854, respectively, when using no communication. As expected, only if the gain of parallelization exceeds the decline in a SOLVER’s performance due to the addition of more threads, parallelization can be beneficial.

## 4.4 Parallel tree search for MIP solving

We conducted computational experiments using normal and racing ramp-ups for four and eight SOLVER threads. Therefore, for the same number of SOLVER threads, two types of settings were tested. Since FiberSCIP has a non-deterministic behavior, for each setting five repeated runs were conducted. For comparison purpose, additional deterministic runs were performed using four and eight SOLVER threads (only one run for each setting).

Racing ramp-up is a distinguished feature of UG. Many variations are possible by configuring how the parameter sets are chosen in each SOLVER and how the racing stage is terminated. The configuration of FiberSCIP as used in this paper is as follows. The SCIP parameter settings for each racing SOLVER are the same as in Section 4.3. Termination of the racing stage is decided based on the performance of all SOLVERS. When the LOADCOORDINATOR recognizes that

1. at least for half of the SOLVERS it received the first SOLVER status message<sup>6</sup>,
2. a feasible solution has been found,
3. the candidate has more than 300 open nodes, and
4. the elapsed computation time has exceeded 36 seconds (0.5% of our 2 hours time-limit),

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<sup>6</sup>It is not unusual that a SOLVER sends a first status message late when some of the emphasis settings has been set to “aggressive”.

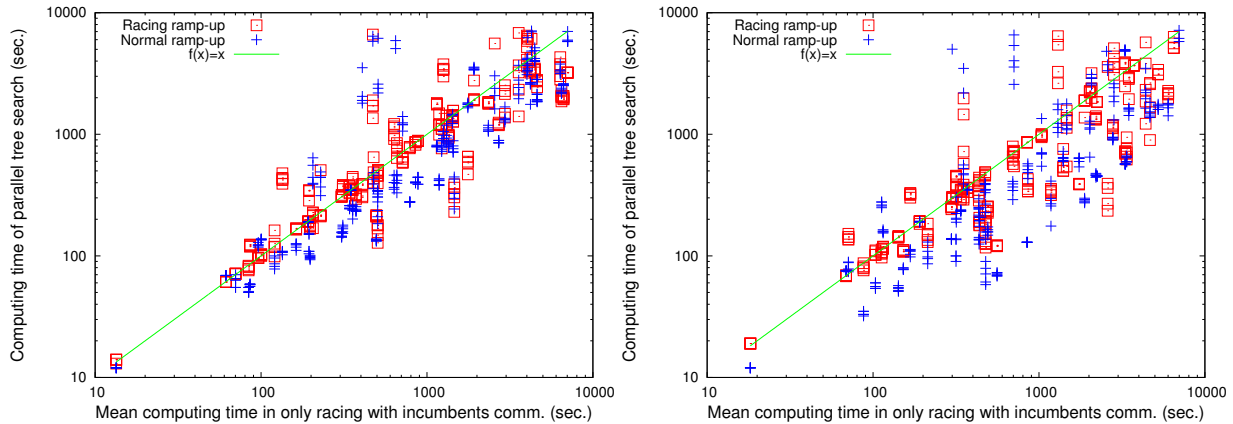


Figure 5: Relationship between only racing with communication of incumbents and racing followed by parallel tree search for four SOLVER threads (left) and eight SOLVER threads (right).

a SOLVER with best dual bound value is chosen as candidate for the winner SOLVER. Conditions 1 and 4 are essential, but if Condition 2 is not satisfied, the racing stage is continued until a solution is found, the problem is proven to be infeasibility, or the time limit is reached. If only Condition 3 is not satisfied, the racing stage is terminated when the elapsed time of computation exceeds 1800 seconds (25% of our 2 hours time-limit). The parameters of this termination criteria can be specified via UG options.

Tables 16–21 in the Appendix show all computational results for MIP solving for all settings. For non-deterministic runs, we conducted five repeated runs and observed higher variation than in the racing with communication of incumbents experiments from Section 4.3, even when all SOLVER settings were the same.

Figure 5 shows the computing times for all parameter settings with respect to the mean computing time when doing only racing with communication of incumbents. The computing time for racing only is considered as an execution without parallel tree search, because the winner’s search tree is generated by a single SOLVER thread. Figure 5 shows that the effectiveness of racing to choose a good parameter setting is not strong enough to overcome the advantages of a parallel tree search in our current implementation. Further, it shows that parallel tree search should be used after the winner SOLVER has been chosen, since the combination of racing and parallel tree search leads to better performance in many cases, especially when computing time increases. This trend is even better visible when the number of threads increases. Note that the plot also includes results for settings that are considered disadvantageous for FiberSCIP.

Table 4 summarizes the speedups and improvements in number of solved instances for each setting, including those for racing only from Section 4.3. The speedups for  $n$  SOLVER threads are calculated w.r.t. the sequential run with double presolve as baseline as follows:

$$\text{Speedup}(n) = \frac{\text{Geometric mean of computing times of FiberSCIP with } n \text{ SOLVER threads}}{\text{Geometric mean of computing times of FiberSCIP with 1 SOLVER thread}}$$

Table 4: Speedups - Nondeterministic and deterministic runs. 87 instances in total, 58 solved by a sequential FiberSCIP run (double presolve). Detailed results are shown in Tables 16–21 in Appendix.

Settings	Non-deterministic						Deterministic		
	# solved				Speedup		# solved	Speedup	
	Share	Min	Max	Average	Share	Average	Single	Share	Value
Four th. only racing with comm.	60	61	63	62.2	56	1.150	48	46	0.52
Four th. racing ramp-up	62	64	66	64.4	53	1.261	50	46	0.47
Four th. normal ramp-up	59	64	65	64.6	52	1.668	49	47	0.64
Eight th. only racing with comm.	53	56	59	57.8	49	1.005	47	45	0.35
Eight th. racing ramp-up	60	64	67	65.4	51	1.402	52	47	0.37
Eight th. normal ramp-up	58	62	64	63.0	50	1.898	48	47	0.61

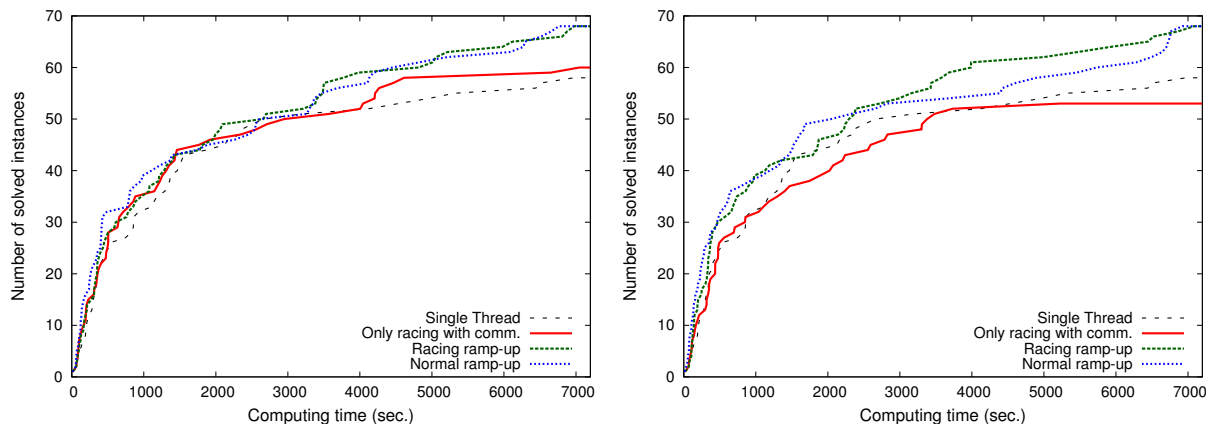


Figure 6: Profiles of number of solved instances w.r.t. solving time for four SOLVER threads (left) and eight SOLVER threads (right).

Since the number of solved instances changes among several runs with the same setting, we print the number of instances only solved by all multi-threaded runs and the number of instances solved by all multi-threaded runs together with the sequential run in the “Share” columns. The speedups are calculated w.r.t. the instances solved by the sequential and the multi-threaded runs. For each run, we show the minimum, maximum, and average number of instances solved by a multi-thread run. Since most of these numbers are higher than the number of instances solved by the sequential run (58 many), most of the multi-threaded runs solved more instances than the sequential run. Especially for the racing ramp-up settings, the number of instances solved by all multi-threaded runs of one setting are usually higher than the number of instances solved by the sequential run. However, for almost all settings, some instances that could be solved by the sequential run were not solved by at least one of the multi-threaded runs.

Whether normal or racing ramp-up is preferable is not clear. The normal ramp-up

shows overall best average speedups but racing ramp-up dominates in the number of solved instances especially when eight SOLVER threads are used. Also the increase in the average number of additionally solved instances when increasing the number of SOLVER threads is larger for racing ramp-up (6.4 for four threads to 7.4 for eight threads) than for normal ramp-up (6.6 for four threads to 5.0 for eight threads). A reason might be, that with only a few SOLVER threads, the effects of tuning w.r.t. a different parameter setting for each thread might not be as strong as when having more threads available. In order to clarify the performance differences, we generated profiles of the number of solved instances w.r.t. computing time, see Figure 6, where in case of five repeated runs average values were used. If an instance could not be solved, but a timeout or abort occurred, the solving time was accounted with 7200s. These cases are responsible for “jumps” in the graphs near the time limit, e.g., for the runs with eight SOLVER thread and normal ramp-up. They indicate that the corresponding configuration makes the solver unstable. For the runs with four SOLVER threads, racing ramp-up and normal ramp-up seem competitive. In contrast, for eight SOLVER threads, racing ramp-up even dominates normal ramp-up. These trends supplement the conclusions we have drawn from Table 4 and are the reason why racing ramp-up is the default setting of FiberSCIP.

We also performed deterministic runs to investigate if we can estimate the average results for non-deterministic runs for a specific setting. Such a possibility would be very useful, e.g., to conduct parameter tunings. Table 4 shows that, obviously, all deterministic runs have worse performance than that of a sequential run, especially when the number of threads increases. This is clearly because SOLVERS have to wait for the token and this waiting time increases when more SOLVER threads are added. Figures 7 and 8 show the relations between the deterministic and non-deterministic runs w.r.t. average number of enumerated nodes and average computing time for all instances solved by the deterministic runs. For the number of nodes, a good correlation can be observed, indicating the possibility to estimate the number of enumerated nodes in non-deterministic runs by those from deterministic ones. For the solving time, Figure 8 show no clear pattern for the changes in running times, that is, the accuracy is currently not sufficient to estimate the computing times of non-deterministic runs from that of deterministic runs. Figure 9 shows the correlation of relative computing time when doing racing ramp-up w.r.t. that of normal ramp-up between deterministic and non-deterministic runs. For non-deterministic runs, the average computing time of five repeated runs is used. If there were a good correlation, it would indicate that the relative racing ramp-up computing time w.r.t. that of normal ramp-up in non-deterministic runs is preserved when switching to deterministic runs. However, no correlations between them could be identified when looking at both pictures in Figure 9. Thus, deterministic runs cannot be used to evaluate a parameter setting for non-deterministic runs.

## 4.5 Computational results for MINLP solving

As the experiments for parallel MINLP solving required several fixes in SCIP and were done much later than the ones for MIP solving, we used SCIP 3.0 for the results on MINLP. Further, since we could not install SCIP with all required plugins for MINLP solving (in



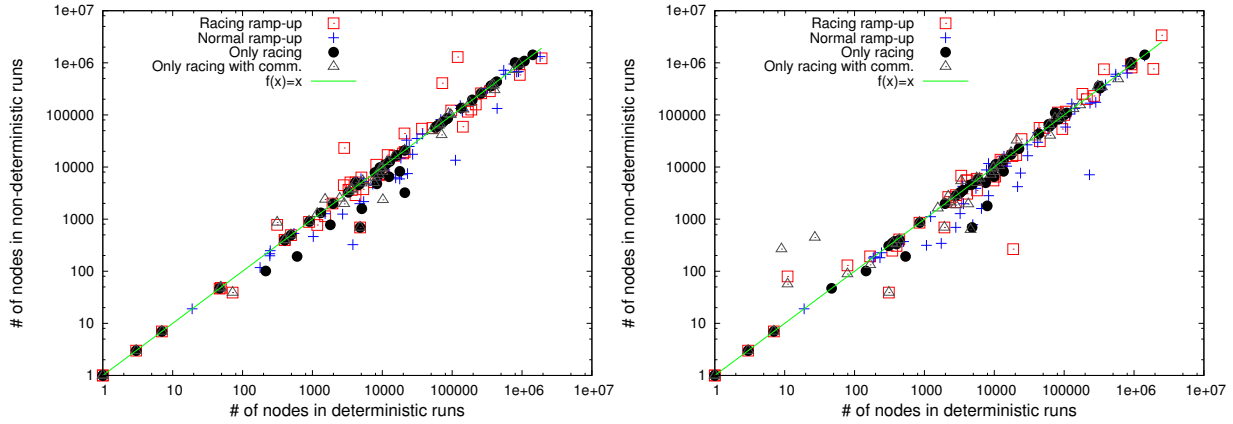


Figure 7: Relationship of average number of nodes between deterministic and non-deterministic runs for four SOLVER threads (left) and eight SOLVER threads (right).

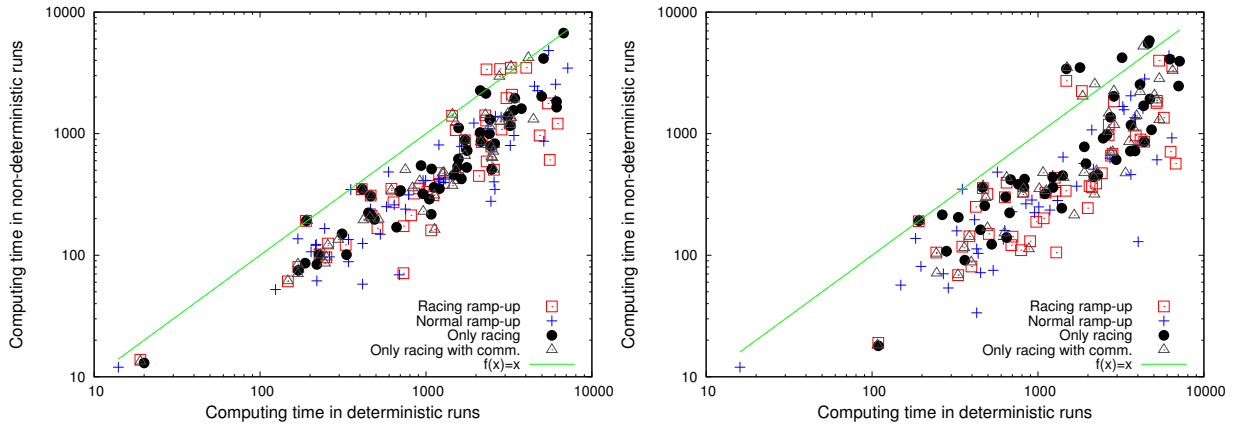


Figure 8: Relationship of average computing time between deterministic and non-deterministic runs for four SOLVER threads (left) and eight SOLVER threads (right).

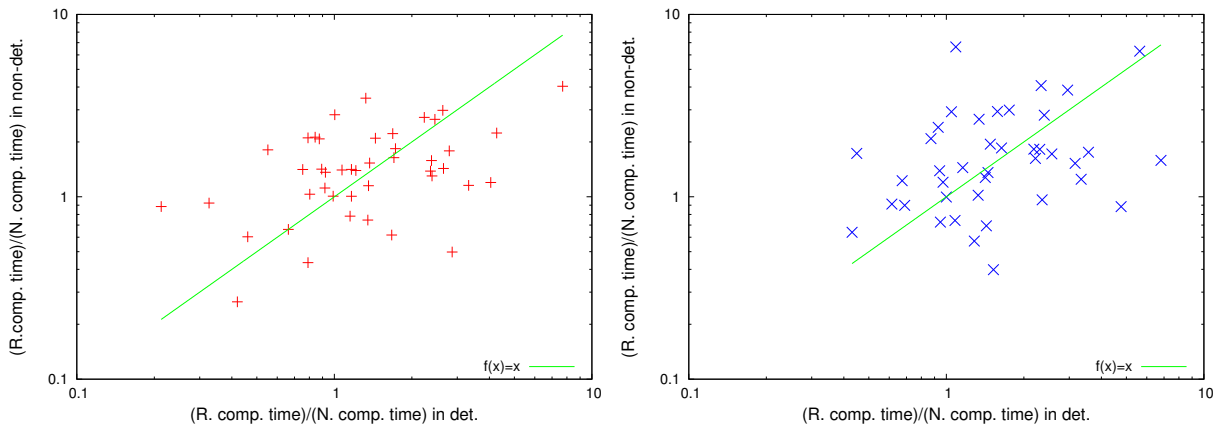


Figure 9: Relationship of relative computing time of racing ramp-up w.r.t. that of normal ramp-up between deterministic and non-deterministic runs for four SOLVER threads (left) and eight SOLVER threads (right).

Table 5: Speedups - Nondeterministic runs (MINLP). 86 instances in total, 27 solved by a sequential **FiberSCIP** run (double presolve). Detailed results are shown in Tables 22 and 23 in Appendix.

Settings	# solved				Speedup	
	Share	Min	Max	Average	Share	Average
Four th. racing ramp-up (default)	28	28	29	28.4	26	1.780
Eight th. racing ramp-up (default)	26	27	30	29.0	23	2.779

particular IPOPT) on the cluster where we conducted our MIP computations, we used a different computing environment with 8 cores divided into two Quad-Core Intel Xeon 5460 CPUs at 3.16 GHz and 48 GB RAM. We performed our test on the MINLPLib (Bussieck et al., 2003) instance library. Even though this collection is not as well-balanced as the benchmark set of MIPLIB2010, it is commonly used for testing and comparing MINLP solvers. From MINLPLib (as of 02/17/2013), we took all instances except for those 12 instances that use the functions `sin`, `cos`, or `erf`, which cannot be handled by SCIP so far. Since the MINLPLib includes many trivial instances, we first run all remaining 252 instances with **SCIP** in sequential mode and then removed those that were solved within 60 seconds (135 instances), as we are interested here in measuring possible gains from running **FiberSCIP** on instances that are not already solved easily in sequential mode. Further, we removed instances where **SCIP** in sequential mode aborted (6 instances), reported a wrong optimal solution (9 instances), or could not compute a finite dual bound (16 instances). Table 7 in the Appendix shows for the remaining set of 86 instances the number of variables, number of constraints, and number of variables of certain types for the original and presolved problems. For the latter, we also distinguish between linear and nonlinear constraints.

We ran **SCIP** in sequential mode and **FiberSCIP** using racing ramp-up with four and eight **SOLVER** threads. The computing times are detailed in Tables 22 and 23 and summarized in Table 5. Out of the 86 selected instances from MINLPLib, **SCIP** solved 27 instances in sequential mode and hit the time limit on the remaining ones. With **FiberSCIP**, instance `netmod_d011` was not solved anymore, but up to two additional instances could be solved when using 4 threads and up to three additional instances could be solved when using 8 threads. Unfortunately, we also noted aborts or wrong solutions on up to 10 (4 threads) or 12 (8 threads) instances. In some cases, aborts were due to running out of memory. Note, that when **SCIP** solves a MINLP, it generates many cutting planes during the branch-and-bound search. Storing these cuts not only for one but for 4 or 8 threads can cost a lot of memory.

Regarding speedup on the number of instances that were solved by **SCIP** and both runs of **FiberSCIP**, we observe average factors of 1.78 when using 4 threads and 2.779 when using 8 threads, which are larger speedups than observed for MIP. However, one should not assume that these numbers can be carried over to MINLP in general, since this set of solved instances is heavily dominated by the `fo*`, `no*`, and `o*` instances, which all have there origin in the same application.

## 5 Concluding remarks

This paper introduced **FiberSCIP**, a parallel extension of **SCIP**, realized via the **UG** framework. **FiberSCIP** has been designed to preserve as much of the flexibility of the **SCIP** framework as possible, that is, extensions to **SCIP**, e.g., in order to solve further classes of optimization problems, are readily available for parallelization in **FiberSCIP**. By linking the same code to **ParaSCIP**, these additional classes can also be handled on large scale distributed memory computing environments.

We have shown quite good performance improvements when using **FiberSCIP**, especially when considering that parallelization is realized from “outside” of **SCIP**, i.e., a developer or user of **SCIP** does have to take care of this parallelization. As for any non-deterministic parallel solver, difficulties emerge regarding evaluation of solver performance and parameter tuning. This paper discussed in detail the performance and behavior of **FiberSCIP** on challenging MIP and MINLP problems and described a possibility to evaluate parallelization.

There are still many open questions about how to parallelize state-of-the-art solving techniques in a most efficient form. Already racing ramp-up offers a variety of choices, like which parameter settings to use in each **SOLVER** thread, when to terminate the racing stage, and how to choose a winner **SOLVER**. How to measure the performance of each configuration of parameter settings for **SCIP** and **UG** in non-deterministic runs is another open question. To evaluate the performance of **FiberSCIP**, we conducted several (non-deterministic) runs for each setting, which required a lot of computing resources. Therefore, an open point for future development is the improvement of the deterministic mode in **FiberSCIP**, so that it can be used to estimate the average behavior of non-deterministic runs.

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## References

- Achterberg, Tobias. 2007. Constraint integer programming. Ph.D. thesis, Technische Universität Berlin. urn:nbn:de:0297-zib-11129.
- Achterberg, Tobias, Thorsten Koch, Alexander Martin. 2006. MIPLIB 2003. *Operations Research Letters* **34** 1–12. doi:10.1016/j.orl.2005.07.009.
- Bendjoudi, Ahcene, Nouredine Melab, El-Ghazali Talbi. 2012. An adaptive hierarchical masterworker (AHMW) framework for grids – application to B&B algorithms. *Journal of Parallel and Distributed Computing* **72** 120 – 131. doi:10.1016/j.jpdc.2011.10.002.

- Berthold, Timo, Ambros M. Gleixner, Stefan Heinz, Stefan Vigerske. 2012. Analyzing the computational impact of MIQCP solver components. *Numerical Algebra, Control and Optimization* **2** 739–748. doi:10.3934/naco.2012.2.739.
- Berthold, Timo, Stefan Heinz, Marc E. Pfetsch. 2009. Nonlinear pseudo-boolean optimization: relaxation or propagation? Oliver Kullmann, ed., *Theory and Applications of Satisfiability Testing – SAT 2009*. No. 5584 in Lecture Notes in Computer Science, Springer, 441–446. doi:10.1007/978-3-642-02777-2\_40.
- Berthold, Timo, Stefan Heinz, Stefan Vigerske. 2011. Extending a CIP framework to solve MIQCPs. Jon Lee, Sven Leyffer, eds., *Mixed Integer Nonlinear Programming, The IMA Volumes in Mathematics and its Applications*, vol. 154. Springer, 427–444. doi:10.1007/978-1-4614-1927-3\_15.
- Bixby, Robert E., William Cook, Alan Cox, Eva K. Lee. 1999. Computational experience with parallel mixed integer programming in a distributed environment. *Annals of Operations Research* 19–43doi:10.1023/A:1018960631213.
- Bussieck, Michael R., Arne S. Drud, Alex Meeraus. 2003. MINLPLib - a collection of test models for mixed-integer nonlinear programming. *INFORMS Journal on Computing* **15** 114–119. doi:10.1287/ijoc.15.1.114.15159. <http://www.gamsworld.org/minlp/minlplib.htm>.
- Bussieck, Michael R., Michael C. Ferris, Alexander Meeraus. 2009. Grid-enabled optimization with GAMS. *INFORMS Journal on Computing* **21** 349–362. doi:10.1287/ijoc.1090.0340.
- Chen, Qun, Michael C. Ferris. 2000. FATCOP: A fault tolerant Condor-PVM mixed integer programming solver. *SIAM Journal on Optimization* **11** 1019–1036. doi:10.1137/S1052623499353911.
- Chen, Qun, Michael C. Ferris, Jeff Linderoth. 2001. FATCOP 2.0: Advanced features in an opportunistic mixed integer programming solver. *Annals of Operations Research* **103** 17–32. doi:10.1023/A:1012982400848.
- Eckstein, Jonathan. 1994. Parallel branch-and-bound algorithms for general mixed integer programming on the CM-5. *SIAM Journal on Optimization* **4** 794–814. doi:10.1137/0804046.
- Eckstein, Jonathan, William E. Hart, Cynthia A. Phillips. 2001. PICO: An object-oriented framework for parallel branch-and-bound. *Inherently Parallel Algorithms in Feasibility and Optimization and Their Applications*. Elsevier Scientific Series on Studies in Computational Mathematics, 219–265. doi:10.1016/S1570-579X(01)80014-8.
- Eckstein, Jonathan, Cynthia A. Phillips, William E. Hart. 2009. PEBBL 1.0 user guide. RUTCOR Research Report RRR 19-2006, Rutgers Center for Operations Research, Rutgers University. URL [http://rutcor.rutgers.edu/pub/rrr/reports2006/19\\_2006.ps](http://rutcor.rutgers.edu/pub/rrr/reports2006/19_2006.ps).

- Goux, Jean-Pierre, Sanjeev Kulkarni, Michael Yoder, Jeff Linderoth. 2001. Master–worker: An enabling framework for applications on the computational grid. *Cluster Computing* **4** 63–70. doi:10.1023/A:1011416310759.
- Koch, Thorsten, Tobias Achterberg, Erling Andersen, Oliver Bastert, Timo Berthold, Robert E. Bixby, Emilie Danna, Gerald Gamrath, Ambros M. Gleixner, Stefan Heinz, Andrea Lodi, Hans Mittelmann, Ted K. Ralphs, Domenico Salvagnin, Daniel E. Steffy, Kati Wolter. 2011. MIPLIB 2010 – Mixed Integer Programming Library version 5. *Mathematical Programming Computation* **3** 103–163. doi:10.1007/s12532-011-0025-9.
- Koch, Thorsten, Ted K. Ralphs, Yuji Shinano. 2012. Could we use a million cores to solve an integer program? *Mathematical Methods of Operations Research* **76** 67–93. doi:10.1007/s00186-012-0390-9.
- Linderoth, Jeff. 1998. Topics in parallel integer optimization. Ph.D. thesis, School of Industrial and Systems Engineering, Georgia Institute of Technology, Atlanta, GA.
- Liu, Tongping, Charlie Curtsinger, Emery D. Berger. 2011. Dthreads: efficient deterministic multithreading. *Proceedings of the Twenty-Third ACM Symposium on Operating Systems Principles*. SOSP '11, ACM, New York, NY, USA, 327–336. doi:10.1145/2043556.2043587.
- Martins, Ruben, Vasco Manquinho, Inês Lynce. 2012. An overview of parallel SAT solving. *Constraints* **17** 304–347. doi:10.1007/s10601-012-9121-3.
- Mitra, Gautam, Ilan Hai, Mozafar T. Hajian. 1997. A distributed processing algorithm for solving integer programs using a cluster of workstations. *Parallel Computing* **23** 733–753. doi:10.1016/S0167-8191(97)00016-1.
- Mittelmann, Hans. 2011. Mixed integer linear programming benchmark (serial codes). <http://plato.asu.edu/ftp/milpf.html>.
- Montesinos, Pablo, Matthew Hicks, Samuel T. King, Josep Torrellas. 2009. Capo: A software-hardware interface for practical deterministic multiprocessor replay. *ACM SIGPLAN Notices* **44** 73–84. doi:10.1145/1508244.1508254.
- Nwana, Vincent, Ken Darby-Dowman, Gautam Mitra. 2004. A twostage parallel branch and bound algorithm for mixed integer programs. *IMA Journal of Management Mathematics* **15** 227–242. doi:10.1093/imaman/15.3.227.
- Olszewski, Marek, Jason Ansel, Saman Amarasinghe. 2009. Kendo: efficient deterministic multithreading in software. *ACM SIGPLAN Notices* **44** 97–108. doi:10.1145/1508284.1508256.
- Ralphs, Ted K. 2006. Parallel branch and cut. E. Talbi, ed., *Parallel Combinatorial Optimization*. Wiley, New York, 53–101.

- Ralphs, Ted K., Menal Güzelsoy, Ashutosh Mahajan. 2011. SYMPHONY 5.4 user's manual. Tech. rep., COR@L Laboratory, Lehigh University. URL <http://www.coin-or.org/SYMPHONY/doc/SYMPHONY-5.4.0-Manual.pdf>.
- Ralphs, Ted K., Laszlo Ladányi, Matthew J. Saltzman. 2003. Parallel branch, cut, and price for large-scale discrete optimization. *Mathematical Programming Series B* **98** 253–280. doi:10.1007/s10107-003-0404-8.
- Ralphs, Ted K., Laszlo Ladányi, Matthew J. Saltzman. 2004. A library hierarchy for implementing scalable parallel search algorithms. *The Journal of Supercomputing* **28** 215–234. doi:10.1023/B:SUPE.0000020179.55383.ad.
- Shinano, Yuji, Tobias Achterberg, Timo Berthold, Stefan Heinz, Thorsten Koch. 2012. ParaSCIP – a parallel extension of SCIP. Christian Bischof, Heinz-Gerd Hegering, Wolfgang E. Nagel, Gabriel Wittum, eds., *Competence in High Performance Computing 2010*. Springer, 135–148. doi:10.1007/978-3-642-24025-6\_12.
- Shinano, Yuji, Tobias Achterberg, Tetsuya Fujie. 2008. A dynamic load balancing mechanism for new ParaLEX. *Proceedings of ICPADS 2008*. 455–462. doi:10.1109/ICPADS.2008.75.
- Shinano, Yuji, Tetsuya Fujie. 2007. Paralex: A parallel extension for the CPLEX mixed integer optimizer. Franck Cappello, Thomas Herault, Jack Dongarra, eds., *Recent Advances in Parallel Virtual Machine and Message Passing Interface, Lecture Notes in Computer Science*, vol. 4757. Springer Berlin Heidelberg, 97–106. doi:10.1007/978-3-540-75416-9\_19.
- Shinano, Yuji, Tetsuya Fujie, Yuusuke Kounoike. 2003. Effectiveness of parallelizing the ILOG-CPLEX mixed integer optimizer in the PUBB2 framework. Harald Kosch, Lszl Bszrmnyi, Hermann Hellwagner, eds., *Euro-Par 2003 Parallel Processing, Lecture Notes in Computer Science*, vol. 2790. Springer Berlin Heidelberg, 451–460. doi:10.1007/978-3-540-45209-6\_67.
- Sun, Yanhua, Gengbin Zheng, Pritish Jetley, Laxmikant V. Kalé. 2011. ParSSSE: An adaptive parallel state space search engine. *Parallel Processing Letters* **21** 319–338. doi:10.1142/S0129626411000242.
- van Nieuwpoort, Rob V., Gosia Wrzesińska, Cerial J.H. Jacobs, Henri E. Bal. 2010. Satin: A high-level and efficient grid programming model. *ACM Transactions on Programming Languages and Systems* **32** 1–39. doi:10.1145/1709093.1709096.
- Vigerske, Stefan. 2013. Decomposition of multistage stochastic programs and a constraint integer programming approach to mixed-integer nonlinear programming. Ph.D. thesis, Humboldt-Universität zu Berlin. urn:nbn:de:kobv:11-100208240.
- Xu, Yan, Ted K. Ralphs, Laszlo Ladányi, Matthew J. Saltzman. 2009. Computational experience with a software framework for parallel integer programming. *INFORMS Journal on Computing* **21** 383–397. doi:10.1287/ijoc.1090.0347.

## Appendix A Benchmark set

The 87 instances of the benchmark set of MIPLIB2010 (Koch et al., 2011) were used for the computational experiments in MIP solving. For MINLP, we used instances from the MINLPLib (Bussieck et al., 2003) instance library, see also Section 4.5. Tables 6 and 7 show the following properties of the MIP and MINLP instances, respectively:

<b>Vars.</b>	The number of variables.
<b>Cons.</b>	The number of constraints.
<b>NZs</b>	The number of non-zero elements in constraint matrix.
<b>Bin</b>	The number of binary variables.
<b>Int</b>	The number of integer variables.
<b>Cont</b>	The number of continuous variables.
<b>Impl</b>	The number of implied integer variables.
<b>LinCons</b>	The number of linear constraints.
<b>NLCons</b>	The number of non-linear constraints.

Table 6: Benchmark set for MIP (MIPLIB2010 benchmark set)

Name	Original instance						Presolved instance						Vars. × Cons.
	Vars.	Cons.	NZs	Bin	Int	Cont	Vars.	Cons.	Bin	Int	Impl	Cont	
30n20b8	18380	576	109706	11036	7344	0	8028	403	7971	2	55	0	3235284
acc-tight5	1339	3052	16134	1339	0	0	998	2291	998	0	0	0	2286418
aflow40b	2728	1442	6783	1364	0	1364	1878	1144	940	0	0	938	2148432
air04	8904	823	72965	8904	0	0	7412	605	7412	0	0	0	4484260
app1-2	26871	53467	199175	13300	0	13571	26265	52555	13000	0	0	13265	1380357075
ash608gpia-3col	3651	24748	74244	3651	0	0	3651	24748	3651	0	0	0	90354948
bab5	21600	4964	155520	21600	0	0	21366	4819	21366	0	0	0	102962754
beasleyC3	2500	1750	5000	1250	0	1250	1704	1153	852	0	0	852	1964712
biella1	7328	1203	71489	6110	0	1218	7311	1202	6110	0	1197	4	8787822
bienst2	505	576	2184	35	0	470	449	520	35	0	0	414	233480
binkar10.1	2298	1026	4496	170	0	2128	1443	825	170	0	0	1273	1190475
bley_x11	5831	175620	869391	5831	0	0	829	7988	829	0	0	0	6622052
bnatt350	3150	4923	19061	3150	0	0	1757	6587	1757	0	0	0	11573359
core2536-691	15293	2539	177739	15284	0	9	15269	1920	15269	0	0	0	29316480
cov1075	120	637	14280	120	0	0	120	637	120	0	0	0	76440
csched010	1758	351	6376	1457	0	301	1654	295	1457	0	1	196	487930
danoint	521	664	3232	56	0	465	513	656	56	0	0	457	336528
dfn-gwin-UUM	938	158	2632	90	0	848	936	156	0	90	0	846	146016
eil33-2	4516	32	44243	4516	0	0	4516	32	4516	0	0	0	144512
eilB101	2818	100	24120	2818	0	0	2818	100	2818	0	0	0	281800
enlight13	338	169	962	169	169	0	338	169	173	165	0	0	57122
enlight14	392	196	1120	196	196	0	392	196	200	192	0	0	76832
ex9	10404	40962	517112	10404	0	0	12	18	12	0	0	0	216
glass4	322	396	1815	302	0	20	317	392	298	0	0	19	124264
gmu-35-40	1205	424	4843	1200	0	5	560	325	555	0	0	5	182000
iis-100-0-cov	100	3831	22986	100	0	0	100	3831	100	0	0	0	383100
iis-bupa-cov	345	4803	38392	345	0	0	341	4803	341	0	0	0	1637823
iis-pima-cov	768	7201	71941	768	0	0	736	7201	736	0	0	0	5299936
lectsched-4-obj	7901	14163	82428	7665	236	0	2606	4801	2500	106	0	0	12511406
m100n500k4r1	500	100	2000	500	0	0	500	100	500	0	0	0	50000
macrophage	2260	3164	9492	2260	0	0	2260	3164	2260	0	0	0	7150640
map18	164547	328818	549920	146	0	164401	15398	31183	118	0	0	15280	480155834
map20	164547	328818	549920	146	0	164401	15398	31183	118	0	0	15280	480155834
mcsched	1747	2107	8088	1731	14	2	1495	1853	1495	0	0	0	2770235
mik-250-1-100-1	251	151	5351	100	150	1	201	159	107	93	1	0	31959
mine-166-5	830	8429	19412	830	0	0	746	7135	746	0	0	0	5322710
mine-90-10	900	6270	15407	900	0	0	800	4656	800	0	0	0	3724800
msc98-1p	21143	15850	92918	20237	53	853	12737	14986	11927	0	0	810	190876682
mspp16	29280	561657	27678735	29280	0	0	12737	14986	11927	0	0	810	190876682
mzzv11	10240	9499	134603	9989	251	0	6892	6816	6657	184	51	0	46975872
n3div36	22120	4484	340740	22120	0	0	19764	4454	19764	0	0	0	88028856
n3seq24	119856	6044	3232340	119856	0	0	119856	5950	119856	0	0	0	713143200
n4-3	3596	1236	14036	174	3422	0	3360	996	0	174	0	3186	3346560
neos-1109824	1520	28979	89528	1520	0	0	1520	9979	1520	0	0	0	15168080
neos-1337307	2840	5687	30799	2840	0	0	2840	5687	2840	0	0	0	16151080
neos-1396125	1161	1494	5511	129	0	1032	1158	1491	129	0	3	1026	1726578
neos13	1827	20852	253842	1815	0	12	1827	17320	1815	0	0	12	31643640
neos-1601936	4446	3131	72500	3906	0	540	3920	3105	3570	0	350	0	12171600
neos18	3312	11402	24614	3312	0	0	761	3300	761	0	0	0	2511300
neos-476283	11915	10015	3945693	5588	0	6327	11825	9583	5544	0	0	6281	113318975
neos-686190	3660	3664	18085	3600	60	0	3660	3658	3600	60	0	0	13388280
neos-849702	1737	1041	19308	1737	0	0	1713	996	1713	0	0	0	1706148
neos-916792	1474	1909	134442	717	0	757	1361	1408	708	0	0	653	1916288
neos-934278	23123	11495	125577	19955	0	3168	8121	8123	7354	0	767	0	65966883
net12	14115	14021	80384	1603	0	12512	12546	12787	1120	0	0	11426	160425702
netdiversion	129180	119589	615282	129180	0	0	128968	99483	128968	0	0	0	12830123544
newdano	505	576	2184	56	0	449	449	520	56	0	0	393	233480
noswot	128	182	735	75	25	28	120	171	75	20	0	25	20520
ns1208400	2883	4289	81746	2880	0	3	2596	1981	2596	0	0	0	5142676
ns1688347	2685	4191	66908	2685	0	0	1360	2599	1360	0	0	0	3534640
ns1758913	17956	624166	1283444	17822	0	134	17624	588479	17622	0	0	2	10371353896
ns1766074	100	182	666	90	10	10	100	110	90	0	0	10	11000
ns1830653	1629	2932	100933	1458	0	171	648	1489	514	0	134	0	964872
opm2-z7-s2	2023	31798	79762	2023	0	0	1900	26839	1900	0	0	0	50994100
pg5_34	2600	225	7700	100	0	2500	2600	225	100	0	0	2500	585000
pigeon-10	490	931	8150	400	0	90	400	525	370	0	0	30	210000
pw-myciel4	1059	8164	17779	1058	1	0	1036	4180	1035	1	0	0	4330480
qu	840	1192	3432	48	0	792	840	1192	48	0	0	792	1001280
rail507	63019	509	468878	63009	0	10	62997	473	62997	0	0	0	29797581
ran16x16	512	288	1024	256	0	256	512	288	256	0	0	256	147456
reblock67	670	2523	7495	670	0	0	606	2130	606	0	0	0	1290780
rmatr100-p10	7359	7260	21877	100	0	7259	7359	7260	100	0	0	7259	53426340
rmatr100-p5	8784	8685	26152	100	0	8684	8784	8685	100	0	0	8684	76289040
rmine6	1096	7078	18084	1096	0	0	1084	7066	1084	0	0	0	7659544
rocl-4-11	9234	21738	243106	9086	0	148	1403	3734	1321	0	0	82	5238802
rococoC10-001000	3117	1293	11751	2993	124	0	2442	576	2442	0	0	0	1406592
roll3000	1166	2295	29386	246	492	428	862	1439	624	114	11	113	1240418
satellites1-25	9013	5996	59023	8509	0	504	7081	4203	7049	0	0	32	29761443
sp98ic	10894	825	316317	10894	0	0	10894	797	10894	0	0	0	8682518
sp98ir	1680	1531	71704	871	809	0	1557	1372	869	688	0	0	2136204
tanglegram1	34759	68342	205026	34759	0	0	34759	68342	34759	0	0	0	2375499578
tanglegram2	4714	9880	26940	4714	0	0	4714	8980	4714	0	0	0	42331720
timtab1	397	171	829	64	107	226	201	166	54	92	0	55	33366
triptim1	30055	15706	515436	20451	9597	7	21938	15679	12446	9492	0	0	343965902
unitcal.7	25755	48939	127595	2856	0	22899	20292	38651	2503	0	0	17789	784306092
vpphard	51471	47280	372305	51471	0	0	28966	24896	28966	0	0	0	721137536
zib54-UUE	5150	1809	15288	81	0	5069	5069	1761	80	0	0	4989	8926509



Table 7: Benchmark set for MINLP (MINLPLib selected instances)

Name	Original instance					Presolved instance						
	Vars.	Cons.	Bin	Int	Cont	Vars.	LinCons	NLCons	Bin	Int	Impl	Cont
4stufen	150	98	48	0	102	125	21	55	48	0	4	73
beuster	158	114	52	0	106	164	108	62	51	0	7	106
cecil_13	840	898	180	0	660	659	736	174	96	0	0	563
chp_partload	2248	2516	45	0	2203	1244	469	995	42	0	0	1202
csched2a	233	138	140	0	93	291	109	87	140	0	0	151
csched2	401	138	308	0	93	457	109	85	308	0	0	149
eg_all_s	8	28	0	7	1	46546	0	46566	2	5	0	46539
eg_disc2_s	8	28	0	3	5	46558	0	46578	0	3	0	46555
eg_disc_s	8	28	0	4	4	46552	0	46572	0	4	0	46548
eg_int_s	8	28	0	3	5	46546	0	46566	2	1	0	46543
enpro48pb	154	215	92	0	62	154	213	2	92	0	0	62
ex1233	53	65	12	0	41	83	46	41	10	0	0	73
fac2	67	34	12	0	55	67	27	4	12	0	0	55
feedtray	98	92	7	0	91	251	19	224	7	0	0	244
fo7	114	211	42	0	72	82	137	14	42	0	0	40
fo8_ar2_1	144	347	0	56	88	101	204	16	1	54	0	46
fo8_ar25_1	144	347	0	56	88	101	204	16	1	54	0	46
fo8_ar3_1	144	347	0	56	88	101	204	16	1	54	0	46
fo8_ar4_1	144	347	0	56	88	101	204	16	1	54	0	46
fo8_ar5_1	144	347	0	56	88	101	204	16	1	54	0	46
fo8	146	273	56	0	90	102	173	16	56	0	0	46
fo9_ar2_1	180	435	0	72	108	123	248	18	1	70	0	52
fo9_ar25_1	180	435	0	72	108	123	248	18	1	70	0	52
fo9_ar3_1	180	435	0	72	108	123	248	18	1	70	0	52
fo9_ar4_1	180	435	0	72	108	123	248	18	1	70	0	52
fo9_ar5_1	180	435	0	72	108	123	248	18	1	70	0	52
fo9	182	343	72	0	110	124	213	18	72	0	0	52
fuzzy	897	1057	120	0	777	819	694	55	110	0	10	699
ghg_1veh	30	38	12	0	18	77	49	55	4	0	0	73
ghg_3veh	96	119	36	0	60	359	357	218	35	0	8	316
hda	723	719	13	0	710	464	230	233	7	0	0	457
lop97ic	1754	92	831	831	92	5220	11509	0	708	704	3808	0
lop97icx	987	88	68	831	88	486	1135	0	68	67	351	0
mbtd	210	70	200	0	10	81310	360	81000	81200	0	0	110
netmod_doll	1999	3138	462	0	1537	1993	3131	1	462	0	1530	1
no7_ar3_1	112	269	0	42	70	87	182	14	1	40	0	46
no7_ar4_1	112	269	0	42	70	87	182	14	1	40	0	46
no7_ar5_1	112	269	0	42	70	87	182	14	1	40	0	46
nous1	51	44	2	0	49	47	11	29	2	0	0	45
nuclear10a	13010	3339	10920	0	2090	23826	32761	3026	10920	0	0	12906
nuclear10b	23826	24971	10920	0	12906	23826	21945	3026	10920	0	0	12906
nuclear14a	992	633	600	0	392	1568	1801	560	600	0	0	968
nuclear14b	1568	1785	600	0	968	1568	1225	560	600	0	0	968
nuclear25a	1058	659	650	0	408	1683	1951	583	650	0	0	1033
nuclear25b	1683	1909	650	0	1033	1683	1326	583	650	0	0	1033
nuclear49a	3341	1431	2450	0	891	5742	7351	1283	2450	0	0	3292
nuclear49b	5742	6233	2450	0	3292	5742	4950	1283	2450	0	0	3292
nvs09	11	1	0	10	1	40	0	30	0	10	9	21
o7_2	114	211	42	0	72	90	153	14	42	0	0	48
o7_ar2_1	112	269	0	42	70	89	188	14	1	40	0	48
o7_ar25_1	112	269	0	42	70	89	188	14	1	40	0	48
o7_ar3_1	112	269	0	42	70	89	188	14	1	40	0	48
o7_ar4_1	112	269	0	42	70	89	188	14	1	40	0	48
o7_ar5_1	112	269	0	42	70	89	188	14	1	40	0	48
o7	114	211	42	0	72	90	153	14	42	0	0	48
o8_ar4_1	144	347	0	56	88	117	252	16	1	54	0	62
o9_ar4_1	180	435	0	72	108	137	290	18	1	70	0	66
oil2	937	927	2	0	935	1065	119	952	2	0	0	1063
oil	1535	1546	19	0	1516	1409	410	1143	19	0	0	1390
pb302035	601	51	600	0	1	1180	1790	0	600	0	580	0
pb302055	601	51	600	0	1	1152	1751	0	585	0	567	0
pb302075	601	51	600	0	1	1074	1640	0	544	0	530	0
pb302095	601	51	600	0	1	931	1436	0	469	0	462	0
pb351535	526	51	525	0	1	1035	1580	0	525	0	510	0
pb351555	526	51	525	0	1	1035	1580	0	525	0	510	0
pb351575	526	51	525	0	1	1035	1580	0	525	0	510	0
pb351595	526	51	525	0	1	1013	1547	0	514	0	499	0
product2	2842	3125	128	0	2714	480	338	128	128	0	0	352
qap	226	31	225	0	1	436	663	0	225	0	211	0
qapw	451	256	225	0	226	675	930	0	225	0	450	0
saa_2	4407	6205	400	0	4007	24115	2170	23743	366	0	0	23749
space25a	383	201	240	0	143	308	101	25	240	0	24	44
space960	5537	6497	0	960	4577	2657	2657	960	0	960	0	1697
stockcycle	481	98	432	0	49	481	97	1	432	0	48	1
super1	1308	1659	44	0	1264	928	592	667	31	0	3	894
super2	1308	1659	44	0	1264	929	592	667	31	0	3	895
super3	1308	1659	44	0	1264	943	603	672	37	0	3	903
super3t	1056	1343	44	0	1012	675	486	449	37	0	3	635
synheat	58	65	12	0	46	75	46	33	10	0	0	65
tln12	168	72	12	156	0	180	85	11	24	144	12	0
tln5	35	30	5	30	0	35	20	5	5	30	0	0
tln6	48	36	6	42	0	48	24	6	6	42	0	0
tls4	105	64	85	4	16	124	100	13	85	0	39	0
waste	2484	1991	400	0	2084	1238	516	2140	400	0	0	838
waterx	70	54	14	0	56	96	36	44	14	0	0	82
waterz	195	137	126	0	69	207	120	29	126	0	0	81

## Appendix B All computational results

All tables except for Tables 14 and 15 evaluate the number of nodes and the running times for different settings over a whole testset. The ‘Nodes’ column shows the number of processed nodes, the ‘Time’ column shows computing time in seconds. In the ‘Time’ column, a number is preceded by ‘>’ if the execution hit the time limit of 2 hours and it is preceded by ‘!’ if execution has aborted. A ‘–’ in the number of nodes and computing time columns indicates that the result was lost for some reason<sup>7</sup>. This case is considered like an ‘abort’. In the bottom of the table, geometric means of the number of processed nodes and computing times are presented w.r.t. the  $n$  instances that were solved by the various **FiberSCIP** runs and the baseline run. The number  $n$  is shown in “(solved:  $n$ )”. The speedup is calculated by using the results for the  $n$  instances. The tables also show geometric means of solving time w.r.t. all instances in the “geom. mean (all)” row, where aborted instances are accounted with the time limit of 7200s. In the following row, in order to see the stability of parallel runs, geometric means of the number of processed nodes and computing times are presented w.r.t. the  $n'$  instances that were solved by the settings of all **FiberSCIP** runs, disregarding the baseline run. The number of solved instances, timeouts, and aborts are shown below and the speedups calculated by the results of  $n$  instances are presented at the bottom of the table. The average values of the geometric means, the computing time, and the speedups in the number of solved instances between the baseline result and the evaluated setting are added in the left most column of the summary.

Tables 14 and 15 show the variation of five repeated runs of **FiberSCIP** with racing only and communication of the incumbents enabled and the same number of threads on the same computer for all instances that are solved within 7200s.

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<sup>7</sup> The main reason for loosing a result is that solving an LP took too long, the job was killed by the resource management system of the cluster, and the result files were not moved from the local disk of the worker node to the network file system.

Table 8: Sequential executions of SCIP and FiberSCIP

Name	SCIP		FiberSCIP			
	Nodes	Time	Presolve Once		Presolve Twice	
			Nodes	Time	Nodes	Time
30n20b8	4691	> 7201	8753	> 7202	4639	> 7219
acc-tight5	1649	340	1649	339	1808	353
afflow40b	286358	2967	286358	2971	668667	6444
air04	144	126	144	127	215	149
app1-2	76	1997	76	2004	392	2163
ash608gpia-3col	7	77	7	80	7	77
bab5	17595	> 7202	17615	> 7202	12846	> 7201
beasleyC3	1151024	> 7203	1193762	> 7203	992738	> 7203
biella1	3270	1549	3270	1552	3270	1554
biens2	117922	553	117922	553	86468	439
binkar10-1	114820	257	114820	256	135435	280
bley_x11	17	467	17	449	1	342
bnatt350	6685	1121	6685	1130	4134	859
core2536-691	281	1064	281	1066	810	1487
cov1075	965740	> 7201	953142	> 7201	976932	> 7201
csched010	651293	> 7200	646222	> 7201	684362	> 7200
danoint	881262	> 7200	879302	> 7201	870942	> 7201
dfn-gwin-UUM	87889	239	87889	241	87613	239
eil33-2	10571	180	10571	180	10571	190
eilB101	9239	1287	9239	1300	9239	1292
enlight13	1116961	1388	1116961	1355	745476	857
enlight14	172555	229	172555	211	259155	316
ex9	1	191	1	191	1	194
glass4	3780000	! 5244	3735142	! 5150	2990992	! 4138
gmu-35-40	2080000	! 1905	2058222	! 1849	1970052	! 1785
iis-100-0-cov	106874	2685	106874	2694	106874	2669
iis-bupa-cov	111227	> 7200	113790	> 7201	113309	> 7202
iis-pima-cov	13011	1504	13011	1505	12469	1526
lectsched-4-obj	2772	156	2772	157	21026	826
m100n500k4r1	5025592	> 7201	5072925	> 7200	5050160	> 7201
macrophage	528171	> 7200	528062	> 7200	541612	> 7201
map18	293	862	293	857	261	1182
map20	353	1001	353	1010	526	926
mcsched	16113	339	16113	339	16113	341
mik-250-1-100-1	1421995	474	1421995	457	1421995	457
mine-166-5	6949	104	6949	105	6170	109
mine-90-10	92852	543	92852	541	189285	1364
msec98-ip	626	> 7203	624	> 7217	485	> 7212
mssp16	1	! 144	1	! 143	1	! 144
mzzv11	2621	755	2621	760	8361	1868
n3div36	40000	! 3101	37642	! 2857	37993	! 2825
n3seq24	542	> 7228	1	! 71	1	! 72
n4-3	48686	1281	48686	1285	57354	1466
neos-1109824	24162	356	24162	359	20142	283
neos-1337307	238371	> 7200	238721	> 7200	239423	> 7201
neos-1396125	65896	6547	65896	6563	40087	4125
neos13	17151	> 7201	17220	> 7201	17847	> 7201
neos-1601936	19862	> 7200	19874	> 7200	7771	5311
neos18	9133	63	9133	65	6827	81
neos-476283	1	! 483	1	! 163	1	! 273
neos-686190	9894	199	9894	200	4739	134
neos-849702	50303	1396	50303	1396	126716	3193
neos-916792	57471	449	57471	450	66213	511
neos-934278	2526	> 7200	2567	> 7201	2755	> 7206
net12	7260	5950	7260	5938	3678	4536
netdiversion	33	> 7278	33	> 7511	26	> 7295
newdano	3062795	> 7200	3052375	> 7201	2842106	> 7201
noswot	463569	197	463569	191	575618	217
ns1208400	12202	3251	12202	3252	4817	1361
ns1688347	4995	510	4995	510	4538	528
ns1758913	1	! 3043	1	! 2853	1	! 3132
ns1766074	946987	1051	946987	959	945109	1318
ns1830653	42213	746	42213	745	88276	1111
opm2-z7-s2	4401	2345	4401	2357	1978	1142
pg5_34	318742	2396	318742	2387	318742	2339
pigeon-10	3757759	> 7200	3535086	> 7200	2955734	> 7200
pw-myciel4	494676	> 7200	482684	> 7200	488828	> 7201
qiu	11012	86	11012	87	9811	83
rail507	1472	2772	1472	2868	1319	2126
ran16x16	371304	335	371304	332	441109	396
reblock67	140595	535	140595	533	83043	339
rmatr100-p10	901	297	901	297	901	298
rmatr100-p5	397	857	397	857	397	855
rmine6	530871	4728	530871	4712	687364	6508
rocII-4-11	13591	406	13591	405	13194	399
rococoC10-001000	365708	2679	365708	2687	1075742	> 7201
roll3000	977873	> 7200	978756	> 7201	1322672	> 7201
satellites1-25	9374	3902	9374	3879	16711	4956
sp98ic	40000	! 5253	41967	! 5110	40930	! 5053
sp98ir	4807	120	4807	123	8984	202
tanglegram1	27	1808	27	1815	27	2358
tanglegram2	3	11	3	12	3	13
timtab1	1039843	744	1085175	768	1014862	> 746
triptim1	30	4535	12	5122	39	> 7207
unitcal_7	17499	3734	17499	3731	12785	2501
vpphard	2319	> 7203	2318	> 7203	3693	> 7206
zib54-UUE	736111	> 7200	553363	6934	565989	6971
geom. mean (solved; 56)	8711	623.5	8718	623.7	9204	669.5
geom. mean (all)	-	1466.2	-	1467.9	-	1554.7
solved/timeout/abort	58/22/7		59/20/8		58/21/8	

Table 9: Racing only runs without communication of incumbents

Name	One thread		2 threads		4 threads		6 threads		8 threads	
	Nodes	Time	Nodes	Time	Nodes	Time	Nodes	Time	Nodes	Time
30n20b8	4639	> 7219	2539	> 7212	2568	> 7200	2038	> 7207	5277	> 7207
acc-tight5	1808	353	1808	353	777	289	748	189	308	156
aflow40b	668667	6444	238236	2080	194236	1818	192294	1987	178690	2220
air04	215	149	179	140	101	101	101	110	101	129
app1-2	392	2163	392	2192	47	1716	47	2776	47	3991
ash608gpia-3col (i)	7	7	7	79	7	102	7	174	7	248
bab5	12846	> 7201	12206	> 7210	10802	> 7201	9131	> 7201	2211	> 7203
beasleyC3	992738	> 7203	901232	> 7200	808112	> 7200	509292	> 7200	479393	> 7200
biella1 (i)	3270	1554	3270	1603	3270	1614	3270	1725	3270	2332
bienst2	86468	439	86468	447	86468	450	86468	468	84244	460
binkar10.1	135435	280	135435	294	135435	306	67149	361	67149	432
bley_xl1 (i)	1	342	1	350	1	349	1	352	1	361
bnatt350	4134	859	4134	866	5058	864	4134	919	2831	945
core2536-691	810	1487	192	1078	192	1096	192	1361	192	2566
cov1075	976932	> 7201	926202	> 7200	912832	> 7200	873782	> 7200	799632	> 7200
csched010	684362	> 7200	676752	> 7200	654132	> 7200	509701	> 7200	527202	> 7200
danoint	870942	> 7201	833042	> 7200	794262	> 7200	768882	> 7200	764882	> 7200
dfn-gwin-UUM	87613	239	87613	242	63562	198	43321	209	22548	218
eil33-2	10571	190	10571	208	10571	228	11423	291	10571	380
eilB101	9239	1292	10512	1124	9770	989	9770	1039	7381	805
enlight13	745476	857	745476	878	367322	510	109200	839	109200	418
enlight14	259155	316	259155	319	259155	388	259155	518	100054	311
ex9 (i)	1	194	1	188	1	183	1	191	1	191
glass4	2990992	! 4138	3954522	! 6086	1082160	1655	637482	! 1510	1082160	2281
gmu-35-40	1970052	! 1785	1354062	! 2376	2792362	! 3117	1881932	! 3486	1796808	! 3988
iis-100-0-cov (i)	106874	2669	106874	2696	106874	2769	106874	3201	106874	3293
iis-bupa-cov	113309	> 7202	112222	> 7200	107022	> 7200	91622	> 7200	75290	> 7200
iis-pima-cov	12469	1526	12469	1493	6523	1318	6523	1394	6523	2368
lectsched-4-obj	21026	826	4591	587	3213	375	1796	208	1796	265
m100n500k4r1	5050160	> 7201	5006321	> 7200	5027960	> 7200	4662679	> 7200	1	> 7200
macrophage	541612	> 7201	385422	> 7200	305392	> 7200	145872	> 7200	114520	> 7200
map18	261	1182	261	1589	493	1418	493	2129	347	3595
map20	526	926	526	958	399	1085	295	1707	333	2148
mcsched	16113	341	16113	342	16625	343	14860	339	13508	319
mik-250-1-100-1 (i)	1421995	457	1421995	468	1421995	505	1421995	529	1421995	551
mine-166-5	6170	109	6170	117	1583	91	4289	101	3582	126
mine-90-10	189285	1364	189285	1376	74459	826	74459	1071	74459	1374
msc98-ip	485	> 7212	393	> 7230	125	> 7209	102	> 7221	233	> 7208
mspp16	1	! 144	1	! 159	1	! 2541	1	! 2430	1	! 2566
mzzv11	8361	1868	4756	1954	4756	1784	4877	2355	4665	4148
n3div36	37993	! 2825	31316	! 3386	47030	! 4023	62009	> 7201	25456	> 7201
n3seq24	1	! 72	1	! 721	1	> 7225	6	> 7258	4	> 7312
n4-3	57354	1466	57354	1543	57354	1554	43434	1469	43434	1677
neos-1109824	20142	283	8268	135	8268	169	8268	217	8268	355
neos-1337307	239423	> 7201	182852	> 7200	176094	> 7200	165083	> 7200	85322	> 7200
neos-1396125	40087	4125	40087	4131	40087	4164	38909	4204	38909	4258
neos13	17847	> 7201	1	> 7202	1	> 7202	1947	> 7201	912	> 7201
neos-1601936	7771	5311	7771	5323	7771	5468	9458	5655	9458	6936
neos18	6827	81	6827	80	7855	76	5830	60	5830	73
neos-476283	1	! 273	372	1017	13	! 876	372	1667	372	2632
neos-686190	4739	134	4739	134	4739	151	3241	133	3241	164
neos-849702	126716	3193	20907	774	20907	786	17371	822	20907	803
neos-916792	66213	511	66213	518	66213	606	60176	796	66213	933
neos-934278	2755	> 7206	248	> 7218	161	> 7216	139	> 7207	45	> 7229
net12	3678	4536	3513	4152	3513	4162	3513	6633	2932	7201
netdiversion	26	> 7295	24	> 7313	16	> 7316	8	> 7718	1	> 7371
newdano	2842106	> 7201	2720074	> 7200	2874552	7199	2058508	6520	2058508	7024
noswot	575618	217	575618	225	434470	188	393317	225	324848	260
ns1208400	4817	1361	691	491	691	504	691	550	691	534
ns1688347 (i)	4538	528	4538	534	4538	536	4538	547	4538	602
ns1758913	1	! 3132	1	! 3903	1	! 4869	-	-	-	> 7881
ns1766074	945109	1318	907103	1367	934754	959	934754	1441	934754	1871
ns1830653	88276	1111	88276	1107	61053	950	61053	1149	60186	1178
opm2-z7-s2	1978	1142	1978	1297	1978	2238	1822	2405	1978	5401
pg5-34	318742	2339	318742	2407	318742	2782	318742	3239	253046	4173
pigeon-10	2955734	> 7200	2	> 7200	2	> 7200	! 613	1	! 3071	1
pw-myciel4	488828	> 7201	474846	> 7201	115605	4945	296556	4496	296556	4666
qui (i)	9811	83	9811	83	9811	84	9811	87	9811	91
rail507	1319	2126	1319	3837	1319	4127	1319	4578	578	> 7202
ran16x16	441109	396	441109	401	356748	350	356748	401	356748	499
reblock67 (i)	83043	339	83043	344	83043	335	83043	412	83043	482
rmatr100-p10 (i)	901	298	901	298	901	299	901	325	901	415
rmatr100-p5	397	855	397	859	397	858	413	905	397	2171
rmine6	687364	6508	687364	6650	586282	> 7200	400132	> 7200	284372	> 7200
rocII-4-11	13194	399	13194	398	11288	342	11288	354	11288	443
rococoC10-001000	1075742	> 7201	1086082	> 7200	562119	4846	562119	5755	347586	! 4231
roll3000	1322672	> 7201	1310742	> 7200	1283482	> 7200	644372	> 7200	688092	> 7200
satellites1-25	16711	4956	16711	5064	3656	4244	3656	6115	11313	> 7203
sp98ic	40930	! 5053	85902	! 5845	83433	! 6251	87508	> 7201	36653	> 7201
sp98ir	8984	202	7236	199	8685	215	4999	183	4999	223
tanglegram1	27	2358	27	2516	27	3941	27	4546	22	> 7264
tanglegram2 (i)	3	13	3	13	3	13	3	18	3	20
timtab1 (i)	1014862	746	1014862	768	1014862	773	1014862	955	1014862	1027
triptim1	39	> 7207	162	6881	4	> 7346	8	> 7300	9	3183
unitcal_7	12785	2501	12785	2529	12785	3906	10723	> 7202	8171	> 7201
vpphard	3693	> 7206	5	> 7210	2	> 7226	4	> 7202	2	> 7215
zib54-UUE	565989	6971	565989	7090	537672	> 7200	492492	> 7200	383842	> 7200
geom. mean (solved: 51)	9817	573.9	8148	529.7	6935	507.5	6386	569.4	5905	672.0
geom. mean (all)	-	1554.6	-	1460.1	-	1434.4	-	1564.4	-	1723.6
geom. mean (solved: 51)			8148	529.7	6935	507.5	6386	569.4	5905	672.0
solved/timeout/abort speedup (solved: 51)	58/21/8		60/20/7 1.084		60/21/6 1.131		59/23/5 1.008		56/27/4 0.854	

Table 10: Effect of communication of incumbents (Four SOLVER Threads)

Name	Without comm. Nodes	comm. Time	Run - 1 Nodes	Run - 1 Time	Run - 2 Nodes	Run - 2 Time	Run - 3 Nodes	Run - 3 Time	Run - 4 Nodes	Run - 4 Time	Run - 5 Nodes	Run - 5 Time
30n20b8	2568	> 7200	902	> 7218	1022	> 7209	820	> 7204	516	> 7203	1174	> 7202
acc-tight5	777	289	39	62	39	62	39	61	39	61	39	61
aflow40b	194236	1818	181535	1875	181535	1856	181535	1841	175610	1639	198942	1611
air04	101	101	49	97	49	96	49	96	49	96	49	96
app1-2	47	1716	47	1930	47	1893	47	1953	47	1902	47	1923
ash608gpia-3col	7	102	7	101	7	100	7	101	7	99	7	100
bab5	10802	> 7201	16846	> 7201	15454	> 7202	12252	> 7201	15235	> 7201	10966	> 7201
beasleyC3	808112	> 7200	898942	> 7201	956912	> 7200	885932	> 7200	1099922	> 7200	801642	> 7200
biella1	3270	1614	2288	1159	2654	1340	1649	1408	1658	1062	1575	1309
biestn2	86468	450	94998	465	97769	499	104468	506	101544	531	104990	523
binkar10_1	135435	306	165250	395	136563	343	107798	259	121683	292	111086	267
bley_x11	1	349	1	349	1	349	1	351	1	352	1	338
bnatt350	5058	864	5058	864	5058	863	5058	814	5058	864	5058	861
core2536-691	192	1096	901	1335	901	1537	810	1607	901	1340	810	1575
cov1075	912832	> 7200	944582	> 7200	1078532	> 7200	1077042	> 7200	950542	> 7200	1069092	> 7200
csched010	654132	> 7200	563541	> 7200	580012	> 7200	656582	> 7200	642848	> 7200	683582	> 7200
cdnoint	794262	> 7200	704140	6653	704140	6662	704140	6619	704140	6684	704140	6643
dfn-gwin-UUM	63562	198	63710	199	63909	201	63551	201	64307	201	61020	186
eil33-2	10571	228	98779	209	9401	201	8975	197	9759	212	9772	208
eilB101	9770	989	4872	692	4402	562	5689	758	4811	624	5049	659
enlight13	367322	510	367322	395	367322	490	367322	489	367322	496	367322	489
enlight14	259155	388	259155	305	259155	388	259155	556	259155	390	259155	398
ex9	1	183	1	191	1	197	1	192	1	191	1	191
glass4	1082160	1655	939959	1544	702114	1167	1050611	1650	2542544	3495	3421535	4949
gmu-35-40	2792362	! 3117	2405472	! 2458	2333392	! 2144	2375502	! 2429	1738622	! 2235	2518052	! 2415
iis-100-0-cov	106874	2769	98732	2731	94430	2598	104420	2863	91513	2490	104420	2855
iis-bupa-cov	107022	> 7200	106992	> 7200	111527	> 7200	106892	> 7200	106616	> 7200	106382	> 7200
iis-pima-cov	6523	1318	7124	1146	7124	1149	7124	1148	7124	1144	7124	1145
lectsched-4-obj	3213	375	4540	264	337	184	3506	237	2794	215	563	243
m100n500k4r1	5027960	> 7200	4959466	> 7200	4975506	> 7200	4915463	> 7200	4857441	> 7200	5004431	> 7200
macrophage	305392	> 7200	307152	> 7201	345402	> 7200	348672	> 7200	381712	> 7200	433012	> 7200
map18	493	1418	493	1427	493	1403	493	1428	493	1465	493	1410
map20	399	1085	399	1180	399	1097	399	1567	399	1184	399	1101
mcsched	16625	343	13704	309	20407	406	16861	344	15775	336	14646	312
mik-250-1-100-1	1421995	505	1421995	490	1421995	495	1421995	500	1421995	496	1421995	494
mine-166-5	1583	91	5138	85	3576	83	4167	87	1028	84	2888	82
mine-90-10	74459	826	291363	2503	65635	494	199943	1949	96075	873	199321	1483
mnc98-ip	125	> 7201	45	> 7242	138	> 7209	209	> 7201	130	> 7242	138	> 7220
mspp16	4756	! 2549	4048	! 2544	6993	! 2551	4461	! 2536	4806	! 2562	4152	! 2575
mzvw11	4756	1784	4048	1147	6993	1612	4461	1264	4806	1305	4152	1227
n3div36	47030	! 4023	40083	! 4683	56160	! 5047	50186	! 4698	52637	! 4788	35660	! 4707
n3seq24	1	> 7225	152	> 7209	193	> 7210	285	> 7242	156	> 7225	1	> 674
n4-3	57354	1554	49902	1301	51789	1403	46044	1293	48271	1355	50043	1406
neos-1109824	8268	169	8164	171	8164	285	8164	171	8164	171	8164	175
neos-1337307	176094	> 7200	204864	> 7201	208705	> 7200	214352	> 7200	211707	> 7200	211819	> 7200
neos-1396125	40087	4164	39799	4152	42121	4796	41808	4444	44725	4925	43032	4750
neos13	161	> 7202	4882	3741	50	2952	46	3674	6882	4596	425	2895
neos-1601936	7771	5468	12605	> 7200	3967	3662	6206	6749	14135	> 7200	3191	3404
neos18	7855	76	6292	70	6292	70	6292	70	6292	71	6292	70
neos-476283	13	! 876	1	! 439	1	! 2840	12	! 869	31	! 855	70	! 1117
neos-686190	4739	151	3589	118	4306	129	3018	109	3679	123	3970	124
neos-849702	20907	786	20907	788	20907	786	20907	790	20907	788	20907	788
neos-916792	66213	606	66296	584	66044	581	68269	836	64479	594	69786	641
neos-934278	161	> 7206	712	> 7206	291	> 7206	291	> 7206	291	> 7206	291	> 7206
net12	3513	4162	3850	3314	3056	4018	3484	4383	4464	4095	4721	4216
netdiversion	16	> 7316	15	> 7315	14	> 7353	-	-	23	> 7317	16	> 7320
newdano	2874552	7199	2870908	6711	2719657	> 7200	1898642	4595	2394587	7152	2791732	6957
noswot	434470	188	301829	159	301829	158	301829	164	301829	170	301829	163
ns1208400	691	504	691	506	691	507	691	507	691	507	691	510
ns1688347	4538	536	3515	483	3752	476	4538	536	4310	505	2944	383
ns1758913	1	! 4869	1	! 7898	1	! 5011	1	! 4796	1	! 4709	1	! 4709
ns1766074	934754	959	934754	1194	934754	1190	934754	1188	934754	1170	934754	1180
ns1830653	61053	950	38073	677	48232	810	43242	748	39359	655	37962	679
opm2-z7-s2	1978	2238	3233	2833	2321	2693	2156	4070	2485	2744	2285	2416
pg5_34	318742	2782	292798	2336	318401	2726	310197	2319	309644	2589	267308	1752
pigeon-10	2	> 7200	2	> 7200	2	> 7200	2	> 7200	2	> 7200	2	> 7200
pw-myciel4	115605	4945	400202	> 7200	411708	> 7200	255557	> 7200	419942	> 7200	396017	> 7200
qui	9811	84	9543	187	9471	85	9467	86	9483	86	9471	85
rail507	1319	4127	1303	4485	1334	4519	1191	3921	1213	4174	1329	3920
ran16x16	356748	350	365028	380	392537	365	365185	371	377618	385	361003	367
reblock67	83043	335	107761	475	107282	438	91057	555	110107	445	107846	610
rmatr100-p10	901	299	901	299	901	309	901	309	901	306	901	308
rmatr100-p5	397	858	397	881	397	883	397	885	397	882	397	882
rmine6	586282	> 7200	607682	> 7200	563296	5305	561803	6544	578703	6873	607822	7126
rocl-4-11	11288	342	16131	413	14119	388	12484	348	10857	328	9250	306
rocoC10-001000	562119	4846	650113	4766	510849	4016	359182	3362	646531	5183	545121	4990
roll3000	1283482	> 7200	1277802	> 7200	912872	> 7200	1002162	> 7200	1236382	> 7200	1073372	> 7200
satellites1-25	3656	4244	11745	4256	11745	4124	11745	4289	11745	4309	11745	4354
sp98ic	83433	! 6251	109475	> 7201	101909	> 7201	106408	> 7200	115019	> 7200	105718	> 7201
sp98ir	8685	215	5720	142	4831	132	5312	130	5361	128	5902	140
tanglegram1	27	3941	27	4031	27	3914	27	3982	27	3991	27	5135
tanglegram2	3	13	3	14	3	13	3	13	3	13	3	14
timtab1	1014862	773	781984	715	758833	622	744540	609	708098	650	697892	573
triptim1	4	> 7346	3	> 7266	3	> 7233	3	> 7246	4	> 7226	3	> 7261
unitcal.7	12785	3906	15221	4499	15613	4424	12599	3796	12996	3933	16640	3570
vpphard	2	> 7226	2	> 720								

Table 11: Effect of communication of incumbents (Eight SOLVER Threads)

Name	Without comm. Nodes Time	Run - 1 Nodes Time	Run - 2 Nodes Time	Run - 3 Nodes Time	Run - 4 Nodes Time	Run - 5 Nodes Time
30n20b8	5277 > 7207	6696 > 7204	17111 > 7201	7233 > 7204	6775 > 7216	7004 > 7217
acc-tight5	308 156	39 69	39 68	39 75	39 63	39 69
aflow40b	178690 2220	146859 1650	145062 1816	143459 1775	142275 1730	136915 1755
air04	101 129	41 119	44 120	59 119	94 99	44 118
app1-2	47 3991	254 3847	47 3905	47 2439	47 2478	47 3831
ash008gpia-3col	7 248	7 249	7 254	7 475	7 259	7 247
bab5	2211 > 7203	2478 > 7201	3685 > 7202	6790 > 7201	2926 > 7202	1883 > 7202
beasleyC3	479393 > 7200	834752 > 7201	537512 > 7200	556352 > 7200	505657 > 7200	768232 > 7200
biella1	3270 2332	1734 1148	1721 1741	1605 1144	2079 1426	2564 1048
biest2	84244 460	91266 539	84210 454	87102 530	81682 431	81735 504
binkar10_1	67149 432	119952 371	142863 531	141806 489	129169 459	119952 536
bley_x11	1 361	1 361	1 361	1 401	1 364	1 363
bnatt350	2831 945	2831 980	2831 693	2831 1533	2831 999	2831 984
core2536-691	192 2566	101 1318	325 2134	101 1298	87 1340	49 1258
cov1075	799632 > 7200	978382 > 7200	873462 > 7200	935292 > 7200	874972 > 7200	944552 > 7200
csched010	527202 > 7200	470959 > 7200	587666 > 7200	622132 > 7200	530962 > 7200	577262 > 7200
danoint	764862 > 7200	729792 > 7200	670262 > 7200	671842 > 7200	746122 > 7200	779562 > 7200
dfn-gwin-UUM	22548 218	20837 125	19914 107	42928 182	20837 123	58127 224
eil33-2	10571 380	10228 350	10508 366	8207 344	9958 359	8561 335
eilB101	7381 805	7897 881	8227 682	5314 702	5593 565	3626 647
enlight13	109200 418	138288 335	125558 201	188996 409	153848 377	167082 434
enlight14	100054 311	100054 298	100054 300	100054 309	100054 292	99882 ! 304
ex9	1 191	1 193	1 191	1 189	1 190	1 191
glass4	1082160 2281	1323490 5001	507573 932	709838 1807	1748611 4002	450004 1229
gmu-35-40	1796808 ! 3988	1574672 ! 2505	2007802 ! 2687	2073102 ! 2772	1937782 ! 2430	2108322 ! 2776
iis-100-0-cov	106874 3293	99765 3265	104531 3438	97503 3306	93341 3249	93341 3275
iis-bupa-cov	75290 > 7200	70091 > 7200	78072 > 7199	78442 > 7200	101141 > 7200	77770 > 7200
iis-pima-cov	6523 2368	6547 2021	7155 2058	7589 2076	7321 2810	7321 2060
lectsched-4-obj	1796 265	1184 131	672 108	340 109	771 102	162 113
m100n500k4r1	1 > 7200	2 > 7200	1 > 7200	1 > 7200	2828190 > 7200	2 > 7200
macrophage	114520 > 7200	132312 > 7200	134282 > 7200	46432 > 7200	131312 > 7200	143382 > 7200
map18	347 3595	347 3421	339 3516	347 3571	347 3438	347 3455
map20	333 2148	333 2204	333 2262	333 2363	333 2172	333 1117
mcsched	13508 319	15356 348	12850 345	15074 355	12239 302	12840 340
mik-250-1-100-1	1421995 551	1421995 565	1432187 519	1421995 575	1421995 565	1421995 571
mine-166-5	3582 126	1792 97	2399 112	1848 100	1494 96	3028 112
mine-90-10	74459 1374	96792 > 1170	101568 1194	60457 719	98243 749	167794 2074
msec98-ip	233 > 7208	24 > 7222	24 > 7245	23 > 7215	24 > 7224	23 > 7212
mssp16	1 ! 2566	1 ! 2561	1 ! 2413	1 ! 2574	1 ! 2569	1 ! 2570
mzvw11	4665 4148	4374 2523	5502 2496	4131 2616	8043 3118	4931 3392
n3din36	25456 > 7201	22031 > 7201	24854 > 7201	25133 > 7201	17862 > 7201	20802 > 7202
n3seq24	4 > 7312	18 > 7222	5 > 7311	6 > 7246	1 > 7140	17 > 7213
n4-3	43434 1677	37108 1195	37831 1479	36245 1416	36261 1403	39036 1504
neos-1109824	8268 355	8164 355	8164 245	8164 360	8164 251	7810 370
neos-1337307	85322 > 7200	88012 > 7200	106106 > 7200	103066 > 7200	106682 > 7200	104462 > 7200
neos-1396125	38909 4258	35099 2834	28818 2812	31703 2699	34698 2802	33686 2792
neos13	912 > 7201	88 2085	63 1862	559 2093	284 2439	337 1880
neos-1601936	9458 6936	8825 > 7200	4556 5120	3711 3677	2123 3326	4969 5463
neos18	5830 73	6318 77	6318 78	5703 69	5450 54	6318 77
neos-476283	372 2632	495 2473	397 2598	443 2631	445 2493	441 2580
neos-686190	3241 164	2692 138	2704 145	2751 144	2767 140	2705 144
neos-849702	20907 803	20907 863	20907 859	17371 856	17371 803	17371 859
neos-916792	66213 933	67052 931	57690 1618	65356 971	67925 947	63971 1963
neos-934278	45 > 7229	4 > 7214	4 > 7227	4 > 7245	48 > 7229	40 > 7215
net12	2932 > 7201	992 > 7202	2001 6359	2412 6237	2119 6391	2418 6973
netdiversion	1 > 7371	2 > 7609	2 > 7562	1 > 7501	- -	1 ! 348
newdano	2058508 7024	2176391 5912	1976816 5849	2587985 > 7200	1659115 6580	1818678 5683
noswot	324848 260	345185 226	281390 185	362474 238	365152 196	362474 222
ns1208400	691 534	691 722	691 691	691 698	691 720	691 705
ns1688347	4538 602	2192 382	1449 311	1435 237	2185 357	2029 299
ns1758913	2 > 7881	-	-	-	-	-
ns1766074	934754 1871	934754 1833	934754 1884	934754 1916	934754 1896	934754 1893
ns1830653	60186 1178	48303 1034	33323 747	36032 820	37907 799	46111 882
opm2-z7-s2	1978 5401	1627 5261	1714 5706	1365 3799	1768 5599	1602 5762
pg5_34	253046 4173	259057 3129	250574 3126	290705 3606	260489 3148	304596 3885
pigeon-10	1 ! 3071	1 > 7200	1 > 7200	1 > 7200	1 > 7200	1 ! 3681
pw-myciel4	296556 4666	307406 > 7200	308496 > 7200	309270 > 7200	304966 > 7200	308893 > 7200
qui	9811 91	9975 87	9692 87	9917 89	9713 87	9961 88
rail507	878 > 7202	373 > 7202	438 > 7205	662 > 7202	643 > 7204	653 > 7203
ran16x16	356748 499	418668 441	299623 346	302695 400	423285 452	316070 546
reblock67	83043 482	83902 489	83293 476	96807 439	81377 452	84623 529
rmatr100-p10	901 415	881 405	886 521	768 428	881 408	881 416
rmatr100-p5	397 2171	397 2121	403 2377	397 2279	397 2317	397 2098
rmine6	284372 > 7200	274192 > 7200	440912 > 7200	269093 > 7200	282942 > 7200	280202 > 7200
roch-4-11	11288 443	10012 407	11029 418	12366 461	9107 486	10104 397
roccocoC10-001000	347586 ! 4231	364404 3613	351486 3628	480102 ! 4297	596605 5416	633055 6006
roll3000	688092 > 7200	595095 > 7200	587822 > 7200	621274 > 7200	614672 > 7200	663042 > 7200
satellites1-25	11313 > 7203	3479 > 7201	11323 > 7201	3479 > 7202	11745 6990	9260 > 7204
sp98ic	36653 > 7201	38050 > 7201	43735 > 7201	73025 > 7201	45665 > 7201	42167 > 7201
sp98ir	4999 223	4939 164	5555 173	4920 171	4416 161	5105 169
tanglegram1	22 > 7264	22 > 7264	1 ! 324	22 > 7231	22 > 7241	11 > 7381
tanglegram2	3 20	3 19	3 19	3 20	3 14	3 19
timtab1	1014862 1027	464378 460	491225 429	496261 495	498709 457	493857 530
triptim1	9 3183	9 3690	9 3746	9 3678	9 3783	9 3760
unitcal7	8171 > 7201	8657 > 7201	6438 > 7201	6265 > 7201	7447 > 7201	6820 > 7201
vpphard	2 > 7215	2 > 7232	1 > 7213	1 > 7217	2 > 7208	2 > 7208
zib54-UUE	383842 > 7200	408932 > 7200	397992 > 7200	397412 > 7200	412702 > 7200	399582 > 7200
geom. mean (solved: 52): 605.81	5128 706.1	4708 615.4	4440 594.9	4322 610.5	4551 588.8	4330 619.5
geom. mean (all): 1551.98	- 1723.6	- 1557.3	- 1515.9	- 1551.8	- 1512.0	- 1622.8
geom. mean (solved: 53): 617.52		4368 629.7	4097 607.8	4158 624.8	4319 604.8	4126 632.6
solved/timeout/abort	56/27/4	56/28/3	58/25/4	56/27/4	59/23/5	57/24/6
speedup (solved: 52): 1.166		1.15	1.19	1.16	1.20	1.14

Table 12: Only racing with communication of incumbents (Four SOLVER Threads)

Name	One thread Nodes Time	Run - 1 Nodes Time	Run - 2 Nodes Time	Run - 3 Nodes Time	Run - 4 Nodes Time	Run - 5 Nodes Time
30n20b8	4639 > 7219	902 > 7218	1022 > 7209	820 > 7204	516 > 7203	1174 > 7202
acc-tight5	1808 353	39 62	39 62	39 61	39 61	39 61
aflow40b	668667 6444	181535 1875	181535 1856	181535 1841	175610 1639	198942 1611
air04	215 149	49 97	49 96	49 96	49 96	49 96
app1-2	392 2163	47 1930	47 1893	47 1953	47 1902	47 1923
ash608gpia-3col	7 77	7 101	7 100	7 101	7 99	7 100
bab5	12846 > 7201	16846 > 7201	15454 > 7202	12252 > 7201	15235 > 7201	10966 > 7201
beasleyC3	992738 > 7203	898942 > 7201	956912 > 7200	885932 > 7200	1099922 > 7200	801642 > 7200
biella1	3270 1554	2288 1159	2654 1340	1649 1408	1658 1062	1575 1309
biest2	86468 439	94998 465	97769 499	104468 506	101544 531	104990 523
binkar10_1	135435 280	165250 395	136563 343	107798 259	121683 292	111086 267
bley_x11	1 342	1 349	1 349	1 351	1 352	1 338
bnatt350	4134 859	5058 864	5058 863	5058 814	5058 864	5058 861
core2536-691	810 1487	901 1335	901 1537	810 1607	901 1340	810 1575
cov1075	976932 > 7201	944582 > 7200	1078532 > 7200	1077042 > 7200	950542 > 7200	1069092 > 7200
csched1010	684362 > 7200	563541 > 7200	580012 > 7200	656582 > 7200	642848 > 7200	683582 > 7200
danoind	870942 > 7201	704140 6653	704140 6662	704140 6619	704140 6684	704140 6643
dfn-gwin-UUM	87613 239	63710 199	63909 201	63551 201	64307 201	61020 186
eil33-2	10571 190	9879 209	9401 201	8975 197	9759 212	9772 208
eilB101	9239 1292	4872 692	4402 562	5689 758	4811 624	5049 659
enlight13	745476 857	367322 395	367322 490	367322 489	367322 496	367322 489
enlight14	259155 316	259155 305	259155 388	259155 556	259155 390	259155 398
ex9	1 194	1 191	1 197	1 192	1 191	1 191
glass4	2990992 ! 4138	939959 1544	702114 1167	1050611 1650	2542544 3495	3421535 4949
gmu-35-40	1970052 ! 1785	2405472 ! 2458	2333392 ! 2144	2375502 ! 2429	1738622 ! 2235	2518052 ! 2415
iis-100-0-cov	106874 2669	98732 2731	94430 2598	104420 2863	91513 2490	104420 2855
iis-bupa-cov	113309 > 7202	106992 > 7200	111527 > 7200	106892 > 7200	106616 > 7200	106382 > 7200
iis-pima-cov	12469 1526	7124 1146	7124 1149	7124 1148	7124 1144	7124 1145
lectsched-4-obj	21026 826	4540 264	337 184	3506 237	2794 215	563 243
m100n500k4r1	5050160 > 7201	4959466 > 7200	4975506 > 7200	4915463 > 7200	4857441 > 7200	5004431 > 7200
macrophage	541612 > 7201	307152 > 7201	345402 > 7200	348672 > 7200	381712 > 7200	433012 > 7200
map18	261 1182	493 1427	493 1403	493 1428	493 1465	493 1410
map20	526 926	399 1180	399 1097	399 1567	399 1184	399 1101
mcsched	16113 341	13704 309	20407 406	16861 344	15775 336	14646 312
mik-250-1-100-1	1421995 457	1421995 490	1421995 495	1421995 500	1421995 496	1421995 494
mine-166-5	6170 109	5138 85	3576 83	4167 87	1028 84	2888 82
mine-90-10	189285 1364	291363 2503	65635 494	199943 1949	96075 873	199321 1483
msec98-ip	485 > 7212	45 > 7242	138 > 7209	209 > 7201	130 > 7242	138 > 7270
mspp16	8361 ! 144	4048 ! 2544	6993 ! 2551	4461 ! 2536	4806 ! 2562	4152 ! 2525
mzvw11	275 > 7206	4882 > 7201	493 > 7207	493 > 7201	493 > 7206	493 > 7202
n3div36	37993 ! 2825	40083 ! 4683	56160 ! 5047	50186 ! 4698	52637 ! 4788	35660 ! 4707
n3seq24	1 ! 72	152 > 7209	193 > 7210	285 > 7242	156 > 7225	1 ! 674
n4-3	57354 1466	49902 1301	51789 1403	46044 1293	48271 1355	50043 1406
neos-1109824	20142 283	8164 171	8164 285	8164 171	8164 171	8164 175
neos-1337307	239423 > 7201	204864 > 7201	208705 > 7200	214352 > 7200	211707 > 7200	211819 > 7200
neos-1396125	40087 4125	39799 4152	42121 4796	41808 4444	44725 4925	43032 4750
neos13	17847 > 7201	4882 > 7201	50 2952	46 3674	6882 4596	406 > 7205
neos-1601936	7771 5311	12605 > 7200	3967 3662	6206 6749	14135 > 7200	3191 3404
neos18	6827 81	6292 70	6292 70	6292 70	6292 71	6292 70
neos-476283	1 ! 273	1 ! 439	1 ! 2840	12 ! 869	31 ! 855	70 ! 1117
neos-686190	4739 134	3589 118	4306 129	3018 109	3679 123	3970 124
neos-849702	126716 3193	20907 788	20907 786	20907 790	20907 788	20907 788
neos-916792	66213 511	66296 584	66044 581	68269 836	64479 594	69786 641
neos-934278	275 > 7206	275 > 7206	275 > 7206	275 > 7206	275 > 7206	275 > 7206
net12	3678 4536	3850 3314	3056 4018	3484 4383	4464 4095	4721 4216
netdiversion	26 > 7295	15 > 7315	14 > 7353	- -	23 > 7317	16 > 7320
newdano	2842106 > 7201	2870908 6711	2719657 > 7200	1898642 4595	2394587 7152	2791732 6957
noswt	575618 217	301829 159	301829 158	301829 164	301829 170	301829 163
ns1208400	4817 1361	691 506	691 507	691 507	691 507	691 510
ns1688347	4538 528	3515 483	3752 476	4538 536	4310 505	2944 383
ns1758913	1 ! 3132	1 ! 7898	1 ! 5011	1 ! 4796	1 ! 4709	1 ! 4709
ns1766074	945109 1318	934754 1194	934754 1190	934754 1188	934754 1170	934754 1180
ns1830653	88276 1111	38073 677	48232 810	43242 748	39359 655	37962 679
opm2-z7-s2	1978 1142	3233 2833	2321 2693	2156 4070	2485 2744	2285 2416
pg5_34	318742 2339	292798 2336	318401 2726	310197 2319	309644 2589	267308 1752
pigeon-10	2955734 > 7200	2 > 7200	2 > 7200	2 > 7200	2 > 7200	2 > 7200
pw-myciel4	488828 > 7201	400202 > 7200	411708 > 7200	255557 > 7200	419942 > 7200	396017 > 7200
qui	9811 83	9543 87	9471 85	9467 86	9483 86	9471 85
rail507	1319 2126	1303 4485	1334 4519	1191 3921	1213 4174	1329 3920
ran16x16	441109 396	365028 380	392537 365	365185 371	377618 385	361003 367
reblock67	83043 339	107761 475	107282 438	91057 555	110107 445	107846 610
rmatr100-p10	901 298	901 299	901 309	901 307	901 306	901 308
rmatr100-p5	397 855	397 881	397 883	397 885	397 882	397 882
rmine6	687364 6508	607682 > 7200	563296 5305	561803 6544	578703 6873	607822 7126
rocl-4-11	13194 399	16131 413	14119 388	12484 348	10857 328	9250 306
roccocoC10-001000	1075742 > 7201	650113 4766	510849 4016	359182 3362	646531 5183	545121 4990
roll3000	1322672 > 7201	1277802 > 7200	912872 > 7200	1002162 > 7200	1236382 > 7200	1073372 > 7200
satellites1-25	16711 4956	11745 4256	11745 4124	11745 4289	11745 4309	11745 4354
sp98ic	40930 ! 5053	109475 > 7201	101909 > 7201	106408 > 7200	115019 > 7200	105718 > 7201
sp98ir	8984 202	5720 142	4831 132	5312 130	5361 128	5902 140
tanglegram1	27 2358	27 4031	27 3914	27 3982	27 3991	27 5135
tanglegram2	3 13	3 14	3 13	3 13	3 13	3 14
timtab1	1014862 > 746	781984 715	758833 622	744540 609	708098 650	697892 573
triptim1	39 > 7207	3 > 7266	3 > 7233	3 > 7246	4 > 7226	3 > 7261
unitcal.7	12785 2501	15221 4499	15613 4424	12599 3796	12996 3933	16640 3570
vpphard	3693 > 7206	2 > 7207	2 > 7201	2 > 7205	2 > 7203	2 > 7205
zib54-UUE	565989 6971	547411 7111	564644 7073	546678 7018	546544 7015	570034 7021
geom. mean (solved: 56): 582.89	9173 670.3	6438 585.2	6014 579.8	6182 602.0	5987 571.8	5963 575.7
geom. mean (all): 1379.54	- 1554.6	- 1386.5	- 1353.3	- 1398.4	- 1383.9	- 1375.7
geom. mean (solved: 60): 661.36		8132 661.5	7008 648.3	7186 675.7	7770 659.5	7134 661.9
solved/timeout/abort	58/21/8	61/21/5	62/20/5	63/18/6	62/20/5	63/18/6
speedup (solved: 56): 1.150		1.15	1.16	1.11	1.17	1.16

Table 13: Only racing with communication of incumbents (Eight SOLVER Threads)

Name	One thread Nodes Time	Run - 1 Nodes Time	Run - 2 Nodes Time	Run - 3 Nodes Time	Run - 4 Nodes Time	Run - 5 Nodes Time
30n20b8	4639 > 7219	6696 > 7204	17111 > 7201	7233 > 7204	6775 > 7216	7004 > 7217
acc-tight5	1808 353	39 69	39 68	39 75	39 63	39 69
aflow40b	668667 6444	146859 1650	145062 1816	143459 1775	142275 1730	136915 1755
air04	215 149	41 119	44 120	59 119	94 99	44 118
app1-2	392 2163	254 3847	47 3905	47 2439	47 2478	47 3831
ash608gpia-3col	7 77	7 249	7 254	7 475	7 259	7 247
bab5	12846 > 7201	2478 > 7201	3685 > 7202	6790 > 7201	2926 > 7202	1883 > 7202
beasleyC3	992738 > 7203	834752 > 7201	537512 > 7200	556352 > 7200	505657 > 7200	768232 > 7200
biella1	3270 1554	1734 1148	1721 1741	1605 1144	2079 1426	2564 1048
biest2	86468 439	91266 539	84210 454	87102 530	81682 431	81735 504
binkar10_1	135435 280	119952 371	142863 531	141806 489	129169 459	119952 536
bley_x11	1 342	1 361	1 361	1 401	1 364	1 363
bnatt350	4134 859	2831 980	2831 693	2831 1533	2831 999	2831 984
core2536-691	810 1487	101 1318	525 2134	101 1298	87 1340	49 1258
cov1075	976932 > 7201	978382 > 7200	873462 > 7200	935292 > 7200	874972 > 7200	944552 > 7200
csched1010	684362 > 7200	470959 > 7200	587666 > 7200	622132 > 7200	530962 > 7200	577262 > 7200
danoint	870942 > 7201	729792 > 7200	670262 > 7200	671842 > 7200	746122 > 7200	779562 > 7200
dfn-gwin-UUM	87613 239	20837 125	19914 107	42928 182	20837 123	58127 224
eil33-2	10571 190	10228 350	10508 366	8207 344	9958 359	8561 335
eilB101	9239 1292	7897 881	8227 682	5314 702	5593 565	3626 647
enlight13	745476 857	138288 335	125558 201	188996 409	153848 377	167082 434
enlight14	259155 316	100054 298	100054 300	100054 309	100054 292	99882 ! 304
ex9	1 194	1 193	1 191	1 189	1 190	1 191
glass4	2990992 ! 4138	1323490 5001	507573 932	709838 1807	1748611 4002	450004 1229
gmu-35-40	1970052 ! 1785	1574672 ! 2505	2007802 ! 2687	2073102 ! 2772	1937782 ! 2430	2108322 ! 2776
iis-100-0-cov	106874 2669	99765 3265	104531 3438	97503 3306	93341 3249	93341 3275
iis-bupa-cov	113309 > 7202	70091 > 7200	78072 > 7199	78442 > 7200	101141 > 7200	77770 > 7200
iis-pima-cov	12469 1526	6547 2021	7155 2058	7589 2076	7321 2810	7321 2060
lectsched-4-obj	21026 826	1184 131	672 108	340 109	771 102	162 113
m100n500k4r1	5050160 > 7201	2 > 7200	1 > 7200	1 > 7200	2828190 > 7200	2 > 7200
macrophage	541612 > 7201	132312 > 7200	134282 > 7200	46432 > 7200	131312 > 7200	143382 > 7200
map18	261 1182	347 3421	339 3516	347 3571	347 3438	347 3455
map20	265 926	333 2204	333 2262	333 2363	333 2172	333 1117
mcsched	16113 341	15356 348	12850 345	15074 355	12239 302	12840 340
mik-250-1-100-1	1421995 457	1421995 565	1432187 519	1421995 575	1421995 565	1421995 571
mine-166-5	6170 109	1792 97	2399 112	1848 100	1494 96	3028 112
mine-90-10	189285 1364	96792 > 1170	101568 1194	60457 719	98243 749	167794 2074
msec98-ip	485 > 7212	24 > 7222	24 > 7245	23 > 7215	24 > 7224	23 > 7212
mspp16	1 ! 144	1 ! 2561	1 ! 2413	1 ! 2574	1 ! 2569	1 ! 2570
mzvw11	8361 1868	4374 2523	5501 2496	4131 2616	8043 3118	4931 3392
n3div36	37993 ! 2825	22031 > 7201	24854 > 7201	25133 > 7201	17862 > 7201	20802 > 7202
n3seq24	1 ! 72	18 > 7222	5 > 7311	6 > 7246	1 ! 2140	17 > 7213
n4-3	57354 1466	37108 1195	37831 1479	36245 1416	36261 1403	39036 1504
neos-1109824	20142 283	8164 355	8164 245	8164 360	8164 251	7810 370
neos-1337307	239423 > 7201	88012 > 7200	106106 > 7200	103066 > 7200	106682 > 7200	104462 > 7200
neos-1396125	40087 4125	35099 2834	28818 2812	31703 2699	34698 2802	33686 2792
neos13	17847 > 7201	8 2085	63 1862	559 2093	284 2439	337 1880
neos-1601936	7771 5311	8825 > 7200	4556 5120	3711 3677	2123 3326	4969 5463
neos18	6827 81	6318 77	6318 78	5703 69	5450 54	6318 77
neos-476283	1 ! 273	495 2473	397 2598	443 2631	445 2493	441 2580
neos-686190	4739 134	2692 138	2704 145	2751 144	2767 140	2705 144
neos-849702	126716 3193	20907 863	20907 859	17371 856	17371 803	17371 859
neos-916792	66213 511	67052 931	57690 1618	65356 971	67925 947	63971 1063
neos-934278	275 > 7206	4 ! 7214	4 > 7227	4 > 7245	48 > 7202	40 > 7232
net12	3678 4536	992 > 7202	2001 6359	2412 6237	2119 6391	2418 6973
netdiversion	26 > 7295	2 > 7609	2 > 7562	1 > 7501	- -	1 ! 348
newdano	2842106 > 7201	2176391 5912	1976816 5849	2587985 > 7200	1659115 6580	1818678 5683
noswot	575618 217	345185 226	281390 185	362474 238	365152 196	362474 222
ns1208400	4817 1361	691 722	691 691	691 698	691 720	691 705
ns1688347	4538 528	2192 382	1449 311	1435 237	2185 357	2029 299
ns1758913	1 ! 3132	- -	- -	- -	- -	- -
ns1766074	945109 1318	934754 1833	934754 1884	934754 1916	934754 1896	934754 1893
ns1830653	88276 1111	48303 1034	33323 747	36032 820	37907 799	46111 882
opm2-z7-s2	1978 1142	1627 5261	1714 5706	1365 3799	1768 5599	1602 5762
pg5_34	318742 2339	259057 3129	250574 3126	290705 3606	260489 3148	304596 3885
pigeon-10	2955734 > 7200	1 > 7200	1 > 7200	1 > 7200	1 > 7200	1 ! 3681
pw-myciel4	488828 > 7201	307406 > 7200	308496 > 7200	309270 > 7200	304966 > 7200	308893 > 7200
qui	9811 83	9975 87	9692 87	9917 89	9713 87	9961 88
rail507	1319 2126	373 > 7202	438 > 7205	662 > 7202	643 > 7204	653 > 7203
ran16x16	441109 396	418668 441	299623 346	302695 400	423285 452	316070 546
reblock67	83043 339	83902 489	83293 476	96807 439	81377 452	84623 529
rmatr100-p10	901 298	881 405	886 521	768 428	881 408	881 416
rmatr100-p5	397 855	397 2121	403 2377	397 2279	397 2317	397 2098
rmine6	687364 6508	274192 > 7200	440912 > 7200	269093 > 7200	282942 > 7200	280202 > 7200
rocl-4-11	13194 399	10012 407	11029 418	12366 461	9107 486	10104 397
roccoco10-001000	1075742 > 7201	364404 3613	351486 3628	480102 ! 4297	596605 5416	633055 6006
roll3000	1322672 > 7201	595095 > 7200	587822 > 7200	621274 > 7200	614672 > 7200	663042 > 7200
satellites1-25	16711 4956	3479 > 7201	11323 > 7201	3479 > 7202	11745 6990	9260 > 7204
sp98ic	40930 ! 5053	38050 > 7201	43735 > 7201	73025 > 7201	45665 > 7201	42167 > 7201
sp98ir	8984 202	4939 164	5555 173	4920 171	4416 161	5105 169
tanglegram1	27 2358	22 > 7264	1 ! 324	22 > 7231	22 > 7241	11 > 7381
tanglegram2	3 13	3 19	3 19	3 20	3 14	3 19
timtab1	1014862 > 746	464378 460	491225 429	496261 495	498709 457	493857 530
triptim1	39 > 7207	9 3690	9 3746	9 3678	9 3783	9 3760
unitcal.7	12785 2501	8657 > 7201	6438 > 7201	6265 > 7201	7447 > 7201	6820 > 7201
vpphard	3693 > 7206	2 > 7232	1 > 7213	1 > 7217	2 > 7208	2 > 7208
zib54-UUE	565989 6971	408932 > 7200	397992 > 7200	397412 > 7200	412702 > 7200	399582 > 7200
geom. mean (solved: 49): 552.68	9226 555.2	4993 552.6	4805 550.9	4628 558.7	4799 529.3	4681 571.9
geom. mean (all): 1551.98	- 1554.6	- 1557.3	- 1515.9	- 1551.8	- 1512.0	- 1622.8
geom. mean (solved: 53): 617.52	- -	4368 629.7	4097 607.8	4158 624.8	4319 604.8	4126 632.6
solved/timeout/abort	58/21/8	56/28/3	58/25/4	56/27/4	59/23/5	57/24/6
speedup (solved: 49): 1.005	- -	1.00	1.01	0.99	1.05	0.97



Table 14: Variation of solving time and number of nodes when doing only racing with communication of incumbents for the 63 instances that were solved at least once. The number of the cases an instance was solved is shown in parenthesis in the first column, if it is less than five. (Four SOLVER Threads)

Name	Number of enumerated nodes				Computing Time (sec.)			
	Mean	Std.Dev.	Min.	Max.	Mean	Std.Dev.	Min.	Max.
acc-tight5	39.0	0.00	39(100.00%)	39(100.00%)	61.4	0.49	61 (99.35%)	62(100.98%)
aflow40b	183831.4	7896.10	175610 (95.53%)	198942(108.22%)	1764.4	114.67	1611 (91.31%)	1875(106.27%)
air04	49.0	0.00	49(100.00%)	49(100.00%)	96.2	0.40	96 (99.79%)	97(100.83%)
app1-2	47.0	0.00	47(100.00%)	47(100.00%)	1920.2	21.22	1893 (98.58%)	1953(101.71%)
ash608gpia-3col	7.0	0.00	7(100.00%)	7(100.00%)	100.2	0.75	99 (98.80%)	101(100.80%)
biella1	1964.8	430.18	1575 (80.16%)	2654(135.08%)	1255.6	126.50	1062 (84.58%)	1408(112.14%)
bienst2	100753.8	3857.55	94998 (94.29%)	104990(104.20%)	504.8	22.96	465 (92.12%)	531(105.19%)
binkar10.1	128476.0	20946.90	107798 (83.91%)	165250(128.62%)	311.2	51.15	259 (83.23%)	395(126.93%)
bley_xl1	1.0	0.00	1(100.00%)	1(100.00%)	347.8	5.04	338 (97.18%)	352(101.21%)
bnatt350	5058.0	0.00	5058(100.00%)	5058(100.00%)	853.2	19.63	814 (95.41%)	864(101.27%)
core2536-691	864.6	44.58	810 (93.68%)	901(104.21%)	1438.8	124.69	1335 (92.79%)	1607(111.69%)
danoint	704140.0	0.00	704140(100.00%)	704140(100.00%)	6652.2	21.42	6619 (99.50%)	6684(100.48%)
dfn-gwin-UUM	63299.4	1167.43	61020 (96.40%)	64307(101.59%)	197.6	5.85	186 (94.13%)	201(101.72%)
eil33-2	9557.2	332.80	8975 (93.91%)	9879(103.37%)	205.4	5.54	197 (95.91%)	212(103.21%)
eilB101	4964.6	419.66	4402 (88.67%)	5689(114.59%)	659.0	65.61	562 (85.28%)	758(115.02%)
enlight13	367322.0	0.00	367322(100.00%)	367322(100.00%)	471.8	38.49	395 (83.72%)	496(105.13%)
enlight14	259155.0	0.00	259155(100.00%)	259155(100.00%)	407.4	81.65	305 (74.86%)	556(136.48%)
ex9	1.0	0.00	1(100.00%)	1(100.00%)	192.4	2.33	191 (99.27%)	197(102.39%)
glass4	1731352.6	1064311.33	702114 (40.55%)	3421535(197.62%)	2561.0	1441.00	1167 (45.57%)	4949(193.24%)
iis-100-0-cov	98703.0	5202.38	91513 (92.72%)	104420(105.79%)	2707.4	145.45	2490 (91.97%)	2863(105.75%)
iis-pima-cov	7124.0	0.00	7124(100.00%)	7124(100.00%)	1146.4	1.85	1144 (99.79%)	1149(100.23%)
lectsched-4-obj	2348.0	1647.73	337 (14.35%)	4540(193.36%)	228.6	27.22	184 (80.49%)	264(115.49%)
map18	493.0	0.00	493(100.00%)	493(100.00%)	1426.6	21.49	1403 (98.35%)	1465(102.69%)
map20	399.0	0.00	399(100.00%)	399(100.00%)	1225.8	174.60	1097 (89.49%)	1567(127.83%)
mcsched	16278.6	2320.79	13704 (84.18%)	20407(125.36%)	341.4	34.99	309 (90.51%)	406(118.92%)
mik-250-1-100-1	1421995.0	0.00	1421995(100.00%)	1421995(100.00%)	495.0	3.22	490 (98.99%)	500(101.01%)
mine-166-5	3359.4	1379.87	1028 (30.60%)	5138(152.94%)	84.2	1.72	82 (97.39%)	87(103.33%)
mine-90-10	170467.4	81044.62	65635 (38.50%)	291363(170.92%)	1460.4	721.83	494 (33.83%)	2503(171.39%)
mzzv11	4892.0	1083.26	4048 (82.75%)	6993(142.95%)	1311.0	159.25	1147 (87.49%)	1612(122.96%)
n4-3	49209.8	1935.42	46044 (93.57%)	51789(105.24%)	1351.6	48.18	1293 (95.66%)	1406(104.02%)
neos-1109824	8164.0	0.00	8164(100.00%)	8164(100.00%)	194.6	45.23	171 (87.87%)	285(146.45%)
neos-1396125	42297.0	1609.07	39799 (94.09%)	44725(105.74%)	4613.4	279.53	4152 (90.00%)	4925(106.75%)
neos-1601936	4454.7	1278.26	3191 (71.63%)	6206(139.31%)	4605.0	1519.69	3404 (73.92%)	6749(146.56%)
neos-686190	3712.4	428.31	3018 (81.30%)	4306(115.99%)	120.6	6.77	109 (90.38%)	129(106.97%)
neos-849702	20907.0	0.00	20907(100.00%)	20907(100.00%)	788.0	1.26	786 (99.75%)	790(100.25%)
neos-916792	66974.8	1851.16	64479 (96.27%)	69786(104.20%)	647.2	96.84	581 (89.77%)	836(129.17%)
neos13	2381.0	2927.68	45 ( 1.89%)	6882(289.04%)	3571.6	621.33	2895 (81.06%)	4596(128.68%)
neos18	6292.0	0.00	6292(100.00%)	6292(100.00%)	70.2	0.40	70 (99.72%)	71(101.14%)
net12	3915.0	613.01	3056 (78.06%)	4721(120.59%)	4005.2	366.92	3314 (82.74%)	4383(109.43%)
newdano	2488967.2	385660.72	1898642 (76.28%)	2870908(115.35%)	6353.8	1027.37	4595 (72.32%)	7152(112.56%)
noswot	301829.0	0.00	301829(100.00%)	301829(100.00%)	162.8	4.26	158 (97.05%)	170(104.42%)
ns1208400	691.0	0.00	691(100.00%)	691(100.00%)	507.4	1.36	506 (99.72%)	510(100.51%)
ns1688347	3811.8	569.26	2944 (77.23%)	4538(119.05%)	476.6	51.26	383 (80.36%)	536(112.46%)
ns1766074	934754.0	0.00	934754(100.00%)	934754(100.00%)	1184.4	8.52	1170 (98.78%)	1194(100.81%)
ns1830653	41373.6	3927.34	37962 (91.75%)	48232(116.58%)	713.8	57.35	655 (91.76%)	810(113.48%)
opm2-z7-s2	2496.0	383.15	2156 (86.38%)	3233(129.53%)	2951.2	576.49	2416 (81.87%)	4070(137.91%)
pg5_34	299669.6	18197.10	267308 (89.20%)	318401(106.25%)	2344.4	333.80	1752 (74.73%)	2726(116.28%)
qiu	9487.0	28.51	9467 (99.79%)	9543(100.59%)	85.8	0.75	85 (99.07%)	87(101.40%)
rail507	1274.0	60.13	1191 (93.49%)	1334(104.71%)	4203.8	260.70	3920 (93.25%)	4519(107.50%)
ran16x16	372274.2	11566.69	361003 (96.97%)	392537(105.44%)	373.6	7.68	365 (97.70%)	385(103.05%)
reblock67	104810.6	6946.07	91057 (86.88%)	110107(105.05%)	504.6	67.10	438 (86.80%)	610(120.89%)
rmatr100-p10	901.0	0.00	901(100.00%)	901(100.00%)	305.8	3.54	299 (97.78%)	309(101.05%)
rmatr100-p5	397.0	0.00	397(100.00%)	397(100.00%)	882.6	1.36	881 (99.82%)	885(100.27%)
rmine6	577906.0	18495.68	561803 (97.21%)	607822(105.18%)	6462.0	699.14	5305 (82.10%)	7126(110.28%)
rocII-4-11	12568.2	2410.16	9250 (73.60%)	16131(128.35%)	356.6	39.04	306 (85.81%)	413(115.82%)
rococoC10-001000	542359.2	106786.75	359182 (66.23%)	650113(119.87%)	4463.4	678.23	3362 (75.32%)	5183(116.12%)
satellites1-25	11745.0	0.00	11745(100.00%)	11745(100.00%)	4266.4	77.96	4124 (96.66%)	4354(102.05%)
sp98ir	5425.2	369.93	4831 (89.05%)	5902(108.79%)	134.4	5.57	128 (95.24%)	142(105.65%)
tanglegram1	27.0	0.00	27(100.00%)	27(100.00%)	4210.6	463.73	3914 (92.96%)	5135(121.95%)
tanglegram2	3.0	0.00	3(100.00%)	3(100.00%)	13.4	0.49	13 (97.01%)	14(104.48%)
timtab1	738269.4	31348.99	697892 (94.53%)	781984(105.92%)	633.8	47.55	573 (90.41%)	715(112.81%)
unitcal.7	14613.8	1558.80	12599 (86.21%)	16640(113.86%)	4044.4	360.53	3570 (88.27%)	4499(111.24%)
zib54-UUE	555062.2	10172.13	546544 (98.47%)	570034(102.70%)	7047.6	38.24	7015 (99.54%)	7111(100.90%)

Table 15: Variation of solving time and number of nodes when doing only racing with communication of incumbents for the 59 instances that were solved at least once. The number of the cases an instance was solved is shown in parenthesis in the first column, if it is less than five. (Eight SOLVER Threads)

Name	Number of enumerated nodes				Computing Time (sec.)			
	Mean	Std.Dev.	Min.	Max.	Mean	Std.Dev.	Min.	Max.
acc-tight5	39.0	0.00	39(100.00%)	39(100.00%)	68.8	3.82	63 (91.57%)	75(109.01%)
afflow40b	142914.0	3372.54	136915 (95.80%)	146859(102.76%)	1745.2	55.30	1650 (94.55%)	1816(104.06%)
air04	56.4	19.83	41 (72.70%)	94(166.67%)	115.0	8.02	99 (86.09%)	120(104.35%)
app1-2	88.4	82.80	47 (53.17%)	254(287.33%)	3300.0	687.63	2439 (73.91%)	3905(118.33%)
ash608gpia-3col	7.0	0.00	7(100.00%)	7(100.00%)	296.8	89.20	247 (83.22%)	475(160.04%)
biella1	1940.6	349.66	1605 (82.71%)	2564(132.12%)	1301.4	253.49	1048 (80.53%)	1741(133.78%)
bienst2	85199.0	3627.03	81682 (95.87%)	91266(107.12%)	491.6	42.33	431 (87.67%)	539(109.64%)
binkar10.1	130748.4	10046.42	119952 (91.74%)	142863(109.27%)	477.2	60.17	371 (77.75%)	536(112.32%)
bley_xl1	1.0	0.00	1(100.00%)	1(100.00%)	370.0	15.54	361 (97.57%)	401(108.38%)
bnatt350	2831.0	0.00	2831(100.00%)	2831(100.00%)	1037.8	272.71	693 (66.78%)	1533(147.72%)
core2536-691	132.6	98.06	49 (36.95%)	325(245.10%)	1469.6	333.29	1258 (85.60%)	2134(145.21%)
dfn-gwin-UUM	32528.6	15465.71	19914 (61.22%)	58127(178.70%)	152.2	44.00	107 (70.30%)	224(147.17%)
eil33-2	9492.4	928.34	8207 (86.46%)	10508(110.70%)	350.8	10.91	335 (95.50%)	366(104.33%)
eilB101	6131.4	1717.20	3626 (59.14%)	8227(134.18%)	695.4	103.94	565 (81.25%)	881(126.69%)
enlight13	154754.4	22130.75	125558 (81.13%)	188996(122.13%)	351.2	82.08	201 (57.23%)	434(123.58%)
enlight14	100054.0	0.00	100054(100.00%)	100054(100.00%)	299.8	6.10	292 (97.41%)	309(103.09%)
ex9	1.0	0.00	1(100.00%)	1(100.00%)	190.8	1.33	189 (99.06%)	193(101.15%)
glass4	947903.2	506096.39	450004 (47.47%)	1748611(184.47%)	2594.2	1613.75	932 (35.93%)	5001(192.78%)
iis-100-0-cov	97696.2	4218.23	93341 (95.54%)	104531(107.00%)	3306.6	68.28	3249 (98.26%)	3438(103.97%)
iis-pima-cov	7186.6	348.75	6547 (91.10%)	7589(105.60%)	2205.0	303.04	2021 (91.66%)	2810(127.44%)
lectsched-4-obj	625.8	355.41	162 (25.89%)	1184(189.20%)	112.6	9.85	102 (90.59%)	131(116.34%)
map18	345.4	3.20	339 (98.15%)	347(100.46%)	3480.2	55.58	3421 (98.30%)	3571(102.61%)
map20	333.0	0.00	333(100.00%)	333(100.00%)	2023.6	457.93	1117 (55.20%)	2363(116.77%)
mcsched	13671.8	1282.41	12239 (89.52%)	15356(112.32%)	338.0	18.64	302 (89.35%)	355(105.03%)
mik-250-1-100-1	1424033.4	4076.80	1421995 (99.86%)	1432187(100.57%)	559.0	20.36	519 (92.84%)	575(102.86%)
mine-166-5	2112.2	543.22	1494 (70.73%)	3028(143.36%)	103.4	7.14	96 (92.84%)	112(108.32%)
mine-90-10	104970.8	34790.71	60457 (57.59%)	167794(159.85%)	1181.2	489.45	719 (60.87%)	2074(175.58%)
mzzv11	5396.2	1405.62	4131 (76.55%)	8043(149.05%)	2829.0	360.66	2496 (88.23%)	3392(119.90%)
n4-3	37296.2	1051.19	36245 (97.18%)	39036(104.66%)	1399.4	108.95	1195 (85.39%)	1504(107.47%)
neos-1109824	8093.2	141.60	7810 (96.50%)	8164(100.87%)	316.2	55.93	245 (77.48%)	370(117.01%)
neos-1396125	32800.8	2312.25	28818 (87.86%)	35099(107.01%)	2787.8	46.53	2699 (96.81%)	2834(101.66%)
neos-1601936	3839.8	1089.96	2123 (55.29%)	4969(129.41%)	4396.5	911.66	3326 (75.65%)	5463(124.26%)
neos-476283	444.2	31.05	397 (89.37%)	495(111.44%)	2555.0	61.35	2473 (96.79%)	2631(102.97%)
neos-686190	2723.8	29.54	2692 (98.83%)	2767(101.59%)	142.2	2.71	138 (97.05%)	145(101.97%)
neos-849702	18785.4	1732.28	17371 (92.47%)	20907(111.29%)	848.0	22.61	803 (94.69%)	863(101.77%)
neos-916792	64397.6	3621.31	57690 (89.58%)	67925(105.48%)	1106.0	260.05	931 (84.18%)	1618(146.29%)
neos13	266.2	181.17	63 (23.67%)	559(209.99%)	2071.8	207.97	1862 (89.87%)	2439(117.72%)
neos18	6021.4	371.97	5450 (90.51%)	6318(104.93%)	71.0	9.10	54 (76.06%)	78(109.86%)
net12	2237.5	182.35	2001 (89.43%)	2418(108.07%)	6490.0	284.72	6237 (96.10%)	6973(107.44%)
newdano	1907750.0	191501.49	1659115 (86.97%)	2176391(114.08%)	6006.0	341.79	5683 (94.62%)	6580(109.56%)
noswot	343335.0	31777.95	281390 (81.96%)	365152(106.35%)	213.4	19.73	185 (86.69%)	238(111.53%)
ns1208400	691.0	0.00	691(100.00%)	691(100.00%)	707.2	12.12	691 (97.71%)	722(102.09%)
ns1688347	1858.0	344.66	1435 (77.23%)	2192(117.98%)	317.2	50.17	237 (74.72%)	382(120.43%)
ns1766074	934754.0	0.00	934754(100.00%)	934754(100.00%)	1884.4	27.75	1833 (97.27%)	1916(101.68%)
ns1830653	40335.2	5838.33	33323 (82.62%)	48303(119.75%)	856.4	98.78	747 (87.23%)	1034(120.74%)
opm2-z7-s2	1615.2	138.58	1365 (84.51%)	1768(109.46%)	5225.4	734.08	3799 (72.70%)	5762(110.27%)
pg5_34	273084.2	20811.52	250574 (91.76%)	304596(111.54%)	3378.8	312.23	3126 (92.52%)	3885(114.98%)
qiu	9851.6	123.41	9692 (98.38%)	9975(101.25%)	87.6	0.80	87 (99.32%)	89(101.60%)
ran16x16	352068.2	56553.42	299623 (85.10%)	423285(120.23%)	437.0	65.99	346 (79.18%)	546(124.94%)
reblock67	86000.4	5509.79	81377 (94.62%)	96807(112.57%)	477.0	31.36	439 (92.03%)	529(110.90%)
rmatr100-p10	859.4	45.74	768 (89.36%)	886(103.10%)	435.6	43.44	405 (92.98%)	521(119.61%)
rmatr100-p5	398.2	2.40	397 (99.70%)	403(101.21%)	2238.4	110.03	2098 (93.73%)	2377(106.19%)
rocII-4-11	10523.6	1104.03	9107 (86.54%)	12366(117.51%)	433.8	34.02	397 (91.52%)	486(112.03%)
rococoC10-001000	486387.5	129168.15	351486 (72.26%)	633055(130.15%)	4665.8	1065.87	3613 (77.44%)	6006(128.73%)
satellites1-25	11745.0	0.00	11745(100.00%)	11745(100.00%)	6990.0	0.00	6990(100.00%)	6990(100.00%)
sp98ir	4987.0	365.89	4416 (88.55%)	5555(111.39%)	167.6	4.45	161 (96.06%)	173(103.22%)
tanglegram2	3.0	0.00	3(100.00%)	3(100.00%)	18.2	2.14	14 (76.92%)	20(109.89%)
tintab1	488886.0	12503.65	464378 (94.99%)	498709(102.01%)	474.2	34.89	429 (90.47%)	530(111.77%)
triptim1	9.0	0.00	9(100.00%)	9(100.00%)	3731.4	40.64	3678 (98.57%)	3783(101.38%)

Table 16: Racing ramp-up (Four SOLVER Threads)

Name	One thread		Run - 1		Run - 2		Run - 3		Run - 4		Run - 5	
	Nodes	Time	Nodes	Time	Nodes	Time	Nodes	Time	Nodes	Time	Nodes	Time
30n20b8	4639	> 7219	82016	> 7264	52395	4203	56947	5196	89225	> 7264	71511	6099
acc-tight5	1808	353	39	61	39	61	39	61	39	61	39	61
aflow40b	688667	6444	164816	655	122697	596	77394	468	63537	582	147765	653
air04	215	149	49	96	49	96	44	97	49	96	49	96
app1-2	392	2163	47	1940	47	1943	44	2769	47	1899	47	1905
ash608gpia-3col	7	77	7	103	7	103	7	101	7	102	7	100
bab5	12846	> 7201	147018	> 7313	131523	> 7312	96201	> 7313	75320	> 7313	107256	> 7312
beasleyC3	992738	> 7203	4068580	> 7260	3633095	> 7260	2583438	> 7260	3643541	> 7260	3831586	> 7260
biella1	3270	1554	19168	2988	22710	3427	24806	3464	20208	3374	29093	3762
bienst2	86468	439	127363	396	121624	457	120472	479	121156	455	116227	457
binkar10.1	135435	280	16391	354	17191	375	17485	375	17424	383	16424	370
bley_x11	1	342	1	350	1	350	1	349	1	349	1	350
bnatt350	4134	859	5058	860	5058	861	5058	859	5058	820	5058	863
core2536-691	810	1487	810	1564	810	1562	462	1267	901	1273	901	1351
cov1075	976932	> 7201	1269446	> 7260	1204434	> 7260	1249083	> 7260	1220968	> 7260	1245627	> 7260
csched010	684362	> 7200	1379112	4178	1215300	3975	1179608	3894	1308398	4163	1096865	3682
danoint	870942	> 7201	733418	1988	703213	1950	718611	2021	700568	1940	754964	2072
dfn-gwin-UUM	87613	239	6489	174	10677	180	6442	167	6532	176	6384	169
eil33-2	10571	190	11172	227	7928	169	6398	213	7041	227	4759	219
eilB101	9239	1292	4069	846	5322	639	5752	736	5739	767	4750	804
enlight13	745476	857	4285351	1903	3517588	1712	10317209	6611	2641311	1356	3403198	1718
enlight14	259155	316	259155	303	259155	379	259155	387	259155	311	259155	391
ex9	1	194	1	192	1	193	1	190	1	191	1	192
glass4	2990992	! 4138	17278266	> 7260	17334282	> 7260	19570349	> 7260	13187482	5588	25731787	> 7260
gmu-35-40	1970052	! 1785	14913239	! 2286	32530467	! 3997	28594116	! 3518	17856936	! 2602	16319902	! 2477
iis-100-0-cov	106874	2669	55739	1247	55712	1207	56185	1207	57079	1198	55801	1187
iis-bupa-cov	113309	> 7202	149362	3728	149433	3728	149295	3736	143644	3817	143527	3822
iis-pima-cov	12469	1526	2882	1765	2882	1763	2882	1808	2882	1765	2882	1766
lectsched-4-obj	21026	826	3347	214	36875	507	5785	211	5919	217	3366	214
m100n500k4r1	5050160	> 7201	20703390	> 7260	20732526	> 7260	20519577	> 7260	20699432	> 7260	20537627	> 7260
macrophage	541612	> 7201	3334860	> 7261	4114547	> 7260	2395517	> 7260	3996963	> 7260	4238186	> 7260
map18	261	1182	493	1421	493	1386	493	1445	493	1419	493	1405
map20	526	926	399	1197	399	1176	399	1104	399	1112	399	766
mcsched	16113	341	16299	332	17329	374	19160	378	14068	327	15144	349
mik-250-1-100-1	1421995	457	295811	216	295253	211	269619	212	269993	211	295423	215
mine-166-5	6170	109	3361	76	4573	82	3239	78	3362	81	3745	83
mine-90-10	189285	1364	28948	230	281440	388	190705	323	101852	303	190755	364
msc98-ip	485	> 7212	103	> 7267	467	> 7264	5970	> 7265	4144	> 7266	4248	> 7265
mspp16	1	! 144	1	! 2545	1	! 2610	1	! 2538	1	! 2532	1	! 2538
mzsv11	8361	1868	3507	1198	5455	1344	7493	1425	7486	1427	3853	1186
n3div36	37993	! 2825	720314	> 7266	680770	> 7266	534695	> 7266	774418	> 7266	512355	> 7266
n3seq24	1	! 72	366	> 7308	1	! 774	204	> 7308	1	! 794	1	! 1431
n4-3	57354	1466	47663	969	36082	958	37746	934	49170	983	49819	995
neos-1109824	20142	283	5063	345	5079	285	5061	345	5063	341	5072	346
neos-1337307	239423	> 7201	846805	> 7261	823037	> 7261	829211	> 7261	818196	> 7261	887078	> 7261
neos-1396125	40087	4125	63396	2436	71912	2794	72474	2789	72474	2746	69883	2724
neos13	17847	> 7201	4772	3689	7	1404	709	6813	111	2326	89	3229
neos-1601936	7771	5311	61131	> 7262	75961	> 7262	49998	> 7262	94694	> 7262	49041	> 7262
neos18	6827	81	6292	72	6292	71	6292	71	6292	71	6292	71
neos-476283	1	! 273	411	1246	363	1230	327	! 1282	14	! 879	38	! 1070
neos-686196	4739	134	3859	126	3411	162	3741	118	3856	119	3372	99
neos-849702	126716	3193	20907	767	19445	785	18633	787	18747	789	19365	786
neos-916792	66213	511	1929977	> 7262	1971421	> 7262	2114777	> 7262	1963079	> 7262	2037323	> 7262
neos-934278	2755	> 7206	1215	3540	1239	> 7261	1280	3526	1263	3585	1422	> 7261
net12	3678	4536	4168	5858	2098	3614	4037	5219	5358	6490	2675	4103
netdiversion	26	> 7295	14	> 7355	15	> 7315	14	> 7434	14	> 7369	14	> 7359
newdano	2842106	> 7201	3207739	4307	3266717	2825	3745968	3776	3637999	3007	3330535	3592
noswot	575618	217	578076	165	605292	168	590844	168	592198	168	566218	165
ns1208400	4817	1361	691	508	691	510	691	506	691	494	691	504
ns1688347	4538	528	1752	399	12457	648	3451	487	2325	434	2378	399
ns1758913	1	! 3132	1	! 4774	-	-	-	-	1	! 4600	-	-
ns1766074	945109	1318	934754	1201	934754	992	934754	1189	934754	1191	934754	1486
ns1830653	88276	1111	54156	583	74846	654	53766	592	53695	587	60156	628
opm2-z7-s2	1978	1142	2900	1375	1518	2534	3165	1473	1051	2147	1360	2271
pg5_34	318742	2339	352765	1785	362969	1809	382798	1845	378131	1849	345258	1785
pigeon-10	2955734	> 7200	2	! 145	8550515	> 7260	8490984	> 7260	8080905	> 7260	7678656	> 7260
pw-myciel4	488828	> 7201	1599672	7166	1307118	6766	885110	4618	749182	3657	872659	3860
qiu	9811	83	6774	122	6888	123	7112	120	6930	124	7057	119
rail507	1319	2126	628	3299	845	3325	979	4211	773	3207	630	3376
ran16x16	441109	396	42832	294	45162	315	56901	316	56267	314	70935	321
reblock67	83043	339	118426	179	91280	128	165962	178	148683	168	108363	148
rmatr100-p10	901	298	901	308	805	317	901	308	901	306	901	307
rmatr100-p5	397	855	397	882	397	884	397	880	397	887	397	878
rmine6	687364	6508	886012	1866	1012940	2081	1011117	2016	1086584	2052	1046427	2290
roch_4-11	13194	399	25494	431	16409	382	14252	356	17087	347	18075	447
rococoC10-001000	1075742	> 7201	1346999	3430	1321586	3381	1161137	3226	1289085	3384	1345795	3479
roll3000	1322672	> 7201	288676	972	805173	2265	358465	1135	282969	1012	302479	1024
satellites1-25	16711	4956	5175	> 7326	13426	6086	36324	> 7326	8498	> 7326	7575	> 7326
sp98ic	40930	! 5053	682537	4071	1050617	6495	1007465	6502	1231151	6868	1169778	6645
sp98ir	8984	202	2719	429	4120	392	4440	420	3959	438	3509	478
tanglegram1	27	2358	3115	> 7264	4160	> 7264	3253	> 7264	4397	> 7264	4194	> 7264
tanglegram2	3	13	3	14	3	13	3	14	3	14	3	14
timtab1	1014862	746	934481	914	1441921	1130	1626211	1216	1291078	1162	811181	980
triptim1	39	> 7207	31	> 7291	35	> 7356	30	> 7325	38	> 7323	39	> 7357
unitcal_7	12785	2501	8472	> 7360	2749	6333	3331	> 7355	3710	> 7355	13174	6113
vpphard	3693	> 7206	2987	> 7280	22982	> 7280	911	> 7280	4417	> 7281	1144	> 7282
zib54-UUE	565989	6971	749814	3217	743738	3209	749926	3214	742726	3215	749814	3218
geom. mean (solved: 53): 511.82	10514	645.1	6215	499.5	7065	518.7	6823	525.4	6439	506.7	6321	508.8
geom. mean (all): 1301.82	-	1554.6	-	1271.1	-	1295.5	-	1341.0	-	1290.7	-	1310.8
geom. mean (solved: 62): 671.85			11621	657.3	11878	676.5	12175	692.5	11229	655.4	11017	663.1
solved/timeout/abort		58/21/8		64/19/4		66/17/4		64/19/4		64/18/5		64/18/5
speedup (solved: 53):	1.261		1.29		1.24		1.23		1.27		1.27	

Table 17: Racing ramp-up (Eight SOLVER Threads)

Name	One thread Nodes Time	Run - 1 Nodes Time	Run - 2 Nodes Time	Run - 3 Nodes Time	Run - 4 Nodes Time	Run - 5 Nodes Time
30n20b8	4639 > 7219	29279 > 7264	31435 > 7264	40653 > 7264	51489 > 7264	34872 > 7264
acc-tight5	1808 353	39 69	39 68	39 69	39 68	39 69
aflo40b	684667 6444	50010 387	51392 388	63069 392	49686 390	53691 390
air04	215 149	94 119	121 118	44 118	94 114	44 119
app1-2	392 2163	254 2480	47 3778	47 3818	47 3908	254 3894
ash608gpia-3col	7 77	7 254	7 252	7 242	7 253	7 250
bab5	12846 > 7201	40699 > 7316	48101 > 7316	117415 > 7316	4296 > 7316	73236 > 7316
beasleyC3	992738 > 7203	4163497 > 7260	4537236 > 7260	4159752 > 7260	4223344 > 7260	4218954 > 7260
biella1	3270 1554	17315 2627	51138 5454	61487 6412	28280 3269	1 ! 2697
bienst2	86468 439	96810 226	115405 255	111005 252	120284 254	112816 234
binkar10.1	135435 280	13152 207	11665 182	13596 188	18369 235	12339 194
bley_x11	1 342	1 364	1 361	1 361	1 335	1 363
bnatt350	4134 859	2883 945	3057 988	2831 1005	2831 965	2831 976
core2536-691	810 1487	101 1319	101 1366	587 1570	85 544	92 1130
cov1075	976932 > 7201	1419783 7016	1412202 6983	1317749 6324	1447273 6917	1427398 7067
csched010	684362 > 7200	1228004 3796	1099838 3595	1028131 3075	1037169 3144	1065496 3561
danoimt	870942 > 7201	708555 1092	908777 1282	857283 1198	698945 1081	1 ! 1
dfn-gwin-UUM	87613 239	5926 112	7077 112	6670 108	6643 109	6388 109
eil33-2	10571 190	4575 385	9168 339	4160 355	4717 290	5001 302
eilB101	9239 1292	8065 793	7557 652	7543 661	2929 617	3642 570
enlight13	745476 857	1493063 571	10088388 > 7260	3445307 1456	3254196 1974	1795035 721
enlight14	259155 316	100054 302	100054 296	100054 297	100054 306	100054 297
ex9	1 194	1 191	1 192	1 183	1 194	1 191
glass4	2990992 ! 4138	925791 392	835344 269	13164686 3581	730633 235	1254667 362
gmu-35-40	1970052 ! 1785	57685343 ! 5169	29127724 ! 2821	65683670 ! 5430	53379097 ! 5267	63852223 ! 5675
iis-100-0-cov	106874 2669	56623 724	56098 711	56588 691	56705 724	55055 702
iis-bupa-cov	113309 > 7202	133620 2271	134302 2268	135700 2073	133586 2274	135506 2228
iis-pima-cov	12469 1526	3061 1320	3260 1407	3056 1326	2949 1362	3056 1341
lectsched-4-obj	21026 826	819 107	55 104	162 113	130 97	161 106
m100n500k4r1	5050160 > 7201	23927950 > 7260	25687439 > 7260	20745571 > 7260	20372478 > 7260	40291034 > 7260
macrophage	541612 > 7201	2901767 > 7260	2837778 > 7260	2954520 > 7260	2634932 > 7260	2643068 > 7261
map18	261 1182	228 2917	341 1945	229 2849	217 2942	227 2946
map20	526 926	304 2246	306 2265	301 2262	313 2211	308 2218
mcsched	16113 341	13119 349	11443 291	14218 342	13421 351	11633 303
mik-250-1-100-1	1421995 457	201651 120	196231 121	203907 122	201536 120	200197 122
mine-166-5	6170 109	2172 102	2042 102	2801 111	1843 102	1800 109
mine-90-10	189285 1364	203796 345	210412 334	284973 343	247719 316	210008 356
msec98-ip	485 > 7212	126 > 7266	127 > 7266	312 > 7265	130 > 7266	290 > 7266
mspp16	1 ! 144	1 ! 2583	1 ! 2567	1 ! 2577	1 ! 2567	1 ! 2561
mzsv11	8361 1868	4073 3562	13493 4371	8675 5099	4202 3809	3675 3087
n3div36	37993 ! 2825	375674 > 7266	351501 > 7269	79861 > 7266	329138 > 7266	349069 > 7266
n3seq24	1 72	6 > 7271	5 > 7313	5 > 7336	5 > 7288	5 > 7350
n4-3	57354 1466	39034 502	34888 541	32110 533	38771 757	27312 499
ne05-1109824	20142 283	5004 457	5005 451	5057 448	7594 370	5013 444
neos-1337307	239423 > 7201	1271688 6639	1019426 > 7261	999690 > 7261	1003723 > 7261	915206 > 7261
neos-1396125	40087 4125	46434 1172	42493 1122	43682 999	47905 1197	44035 1137
neos13	17847 > 7201	49 2381	9 1990	109 2378	2334 > 7263	416 3185
neos-1601936	7771 5311	366 1222	72724 3818	12389 2323	6577 1859	53151 5699
neos18	6827 81	6333 137	5436 143	5035 143	5367 152	5524 136
neos-476283	1 ! 273	170 ! 3260	49 ! 2498	41 ! 2623	290 ! 4413	310 ! 3616
neos-686190	4739 134	2617 146	2734 143	2665 141	2578 144	2672 142
neos-849702	126716 3193	17371 857	17099 857	17077 855	17224 860	16206 863
neos-916792	66213 511	2350938 > 7262	2106718 > 7262	2230441 > 7262	2373289 > 7262	2246125 > 7262
neos-934278	2755 > 7206	58 > 7261	137 > 7261	9 > 7219	343 > 7261	10 > 7261
net12	3678 4536	4506 6330	4195 5131	4181 5142	3694 5595	3841 5131
netdiversion	26 > 7295	1 > 7556	1 > 7467	1 > 7512	1 > 7453	1 > 7358
newdano	2842106 > 7201	3521739 1988	4420636 2278	3666312 2126	4024671 2186	4190551 2146
noswot	575618 217	1164879 184	758217 152	675010 135	626020 130	849453 148
ns1208400	4817 1361	691 545	691 703	691 708	691 732	691 717
ns1688347	4538 528	1355 310	1658 310	2088 362	3494 449	1946 387
ns1758913	1 ! 3132	-	-	-	-	-
ns1766074	945109 1318	934754 1908	934754 1888	934754 1887	934754 1371	934754 1893
ns1830653	88276 1111	56707 341	46901 338	62877 428	58534 355	57455 392
opm2-z7-s2	1978 1142	734 3102	681 3126	10609 > 7293	723 3130	721 3391
pg5_34	318742 2339	194960 759	119808 620	153676 655	177763 710	230330 944
pigeon-10	2955734 > 7200	9290583 > 7260	10476462 > 7260	8916280 > 7260	8885860 > 7260	12870820 > 7260
pw-myciel4	488828 > 7201	1003255 3013	1011506 2903	1038567 3273	1028942 3315	983796 3282
qiu	9811 83	6930 80	7004 79	7557 82	7143 76	7164 87
rail507	1319 2126	913 3912	1422 6470	1361 6189	1238 6430	1566 6644
ran16x16	441109 396	24746 180	40850 206	25188 178	30706 189	35222 190
reblock67	83043 339	112381 125	141633 151	104642 117	119474 127	100338 132
rmatr100-p10	901 298	881 410	881 398	835 440	881 306	800 421
rmatr100-p5	397 855	396 1848	436 1845	399 1844	375 1844	435 1844
rmine6	687364 6508	693739 1927	748724 1843	787625 2183	717891 1360	702162 2058
rocH-4-11	13194 399	15352 285	20052 379	15318 347	17397 373	13042 313
rococoC10-001000	1075742 > 7201	672561 1668	547314 1520	1074370 2581	1141007 2644	319131 897
roll3000	1322672 > 7201	136085 440	157371 456	392001 1192	252389 869	332340 1522
satellites1-25	16711 4956	7901 > 7333	6439 > 7326	8946 > 7326	7818 > 7326	4588 > 7326
sp98ic	40930 ! 5053	863052 6259	1162802 > 7264	893500 7149	796554 5983	868740 6018
sp98ir	8984 202	3491 322	3605 301	3721 327	3527 329	3470 317
tanglegram1	27 2358	299 > 7264	224 > 7267	505 > 7264	744 > 7264	398 > 7264
tanglegram2	3 13	3 19	3 19	3 19	3 19	3 19
timtab1	1014862 746	786299 457	811442 486	710921 461	718671 488	791352 469
triptim1	39 > 7207	9 3669	9 3658	9 3690	9 3686	9 3677
unitcal_7	12785 2501	4311 > 7360	2938 4779	3639 5840	2491 > 7359	4225 > 7358
vpghard	3693 > 7206	91 > 7280	338 > 7280	190 > 7280	653 > 7280	835 > 7280
zib54-UUE	565989 6971	649007 2325	639751 2293	623506 1868	654120 2666	620298 2314
geom. mean (solved: 51): 463.70	10165 649.8	4501 453.5	4864 467.6	4739 469.8	4487 453.6	4653 474.0
geom. mean (all): 1198.24	- 1554.6	- 1139.0	- 1195.6	- 1248.1	- 1182.1	- 1226.4
geom. mean (solved: 60): 587.75		7980 563.9	8517 574.8	8914 614.8	8081 569.8	8274 591.6
solved/timeout/abort	58/21/8	67/16/4	65/18/4	66/17/4	65/18/4	64/17/6
speedup (solved: 51): 1.402		1.43	1.39	1.38	1.43	1.37

Table 18: Normal ramp-up (Four SOLVER Threads)

Name	One thread Nodes Time	Run - 1 Nodes Time	Run - 2 Nodes Time	Run - 3 Nodes Time	Run - 4 Nodes Time	Run - 5 Nodes Time
30n20b8	4639 > 7219	81963 5286	41885 > 7264	68158 5385	52136 6529	66997 6956
acc-tight5	1808 353	324 69	323 69	324 69	324 69	324 69
aflow40b	688667 6444	199766 1697	227115 1815	203343 1651	220194 1758	213336 1782
air04	215 149	117 123	129 129	117 123	111 121	113 118
app1-2	392 2163	1256 3515	1222 3371	1311 3451	1224 3412	1224 3570
ash608gpia-3col	7 77	19 138	19 136	19 137	19 137	19 135
bab5	12846 > 7201	64152 > 7313	51915 > 7313	54112 > 7313	21346 > 7313	77307 > 7308
beasleyC3	992738 > 7203	4195344 > 7260	4294521 > 7260	3941075 > 7260	4293587 > 7260	4166184 > 7260
biella1	3270 1554	3989 885	5224 923	5815 1051	6390 1057	4397 982
bienst2	86468 439	129234 343	115570 305	119105 305	121934 338	116683 278
binkar10.1	135435 280	99426 158	108890 179	106746 173	90778 153	105955 167
bley_x11	1 342	1 347	1 348	1 347	1 347	1 347
bnatt350	4134 859	7212 404	7183 403	7038 399	7033 398	7196 404
core2536-691	810 1487	390 802	725 886	460 761	337 710	407 718
cov1075	976932 > 7201	1484506 > 7260	1392562 > 7260	1506849 > 7260	1445224 > 7260	1462785 > 7260
csched010	684362 > 7200	647186 4176	647907 4090	674938 4341	622854 4114	616394 3932
danoimt	870942 > 7201	947533 2514	946838 2510	953678 2560	951045 2523	966768 2613
dfn-gwin-UUM	87613 239	73400 99	67125 95	68306 93	61762 101	72443 97
eil33-2	10571 190	4384 556	4917 388	5073 395	4779 442	4535 641
eilB101	9239 1292	5198 330	7350 395	3622 466	6240 418	3866 455
enlight13	745476 857	2054888 ! 807	12753630 > 7260	10078148 6413	9306378 5812	12487312 > 7260
enlight14	259155 316	4074498 2050	3479374 1803	3857738 1900	13296118 > 7260	5671053 3531
ex9	1 190	1 190	1 190	1 190	1 190	1 190
glass4	2909092 ! 4138	7494170 3031	6498497 2386	4991904 ! 1836	5501925 2081	3529068 1620
gmu-35-40	1970052 ! 1785	7591430 ! 1726	9649466 ! 2063	8754046 ! 1847	8762998 ! 1910	8343312 ! 1824
iis-100-0-cov	106874 2669	80479 851	82497 891	80438 852	82551 890	80413 851
iis-bupa-cov	113309 > 7202	172833 3344	173358 3350	172829 3338	173098 3354	172724 3365
iis-pima-cov	12469 1526	17638 802	17499 789	17554 814	17553 798	17503 790
lectsched-4-obj	21026 826	37101 443	29303 369	33035 442	40165 490	24187 313
m100n500k4r1	5050160 > 7201	12812885 > 7260	11926306 > 7260	14651645 > 7260	14235241 > 7260	18058502 > 7260
macrophage	541612 > 7201	1726584 > 7260	1807982 > 7260	1966116 > 7260	1772585 > 7260	1833770 > 7260
map18	261 1182	194 1285	214 1227	216 1421	252 1464	210 1454
map20	526 926	216 773	185 746	187 885	185 721	216 803
mcsched	16113 341	22471 246	25540 259	22788 243	28191 247	24914 259
mik-250-1-100-1	1421995 457	680433 138	672858 136	671790 132	675404 135	678234 133
mine-166-5	6170 109	1724 51	1868 50	2378 55	2062 55	1868 50
mine-90-10	189285 1364	142375 297	112080 326	157639 428	110894 243	141964 446
msec98-ip	485 > 7212	1205 > 7265	585 > 7264	1198 > 7265	527 > 7265	1626 > 7265
mspp16	1 ! 144	1 ! 2543	1 ! 2530	1 ! 2533	1 ! 2543	1 ! 2539
mzsv11	8361 1868	6171 930	7110 980	7149 1186	4348 877	6219 859
n3div36	37993 ! 8225	486338 > 7266	445521 > 7266	310499 ! 5725	423125 ! 7003	521435 > 7266
n3seq24	1 1	350 > 7309	138 > 7308	91 > 7308	354 > 7308	67 > 7309
n4-3	57354 1466	42573 787	41952 790	42741 803	43395 822	44618 837
neos-1109824	20142 283	7986 109	9959 153	5187 104	6880 150	7451 109
neos-1337307	239423 > 7201	324925 > 7261	598538 > 7261	528393 > 7261	517255 > 7261	522242 > 7261
neos-1396125	40087 4125	35295 1882	36492 1934	34652 1847	34977 1880	35474 1865
neos13	17847 > 7201	923 2790	1460 2151	364 2426	1291 1962	5585 3692
neos-1601936	7771 5311	9979 2127	13551 2823	13747 2825	13545 2825	9495 2145
neos18	6827 81	5208 63	5070 65	9468 70	4460 55	5346 55
neos-476283	1 ! 273	1129 ! 2357	796 ! 1847	1038 2661	761 ! 2062	772 ! 1948
neos-686190	4739 134	9545 96	5678 82	4692 78	6766 86	9338 100
neos-849702	126716 3193	13501 277	13505 278	13412 278	13526 278	13478 277
neos-916792	66213 511	1449303 > 7262	980620 5898	1466680 > 7262	853944 5070	1498253 > 7262
neos-934278	2755 > 7206	3862 > 7261	4455 > 7261	1309 > 7261	2019 > 7261	3587 > 7261
net12	3678 4536	5939 3263	6287 4118	5821 3092	7449 4164	6544 3799
netdiversion	26 > 7295	16 > 7315	25 > 7315	25 > 7316	26 > 7315	50 > 7315
newdano	2842106 > 7201	3648675 3318	3250287 3381	4043488 3785	3283351 3182	3212696 3159
noswot	575618 217	719673 111	704807 123	690812 126	730983 125	740649 118
ns1208400	4817 1361	35267 2390	25811 2189	208125 > 7260	90499 6161	35968 2588
ns1688347	4538 528	4157 357	7339 427	5104 390	6182 461	10917 484
ns1758913	1 ! 3132	- -	- -	- -	- -	- -
ns1766074	945109 1318	661665 421	667310 416	677790 379	661708 431	668777 386
ns1830653	88276 1111	115923 1062	147070 1400	146625 1208	118807 1197	139496 1243
opm2-z7-s2	1978 1142	2689 1318	2346 1354	1833 1680	2410 1317	1563 1262
pg5_34	318742 2339	305029 1062	317551 1090	353814 1186	326189 1131	311572 1061
pigeon-10	2955734 > 7200	7263076 > 7260	4605693 ! 4384	8127279 > 7260	7150034 > 7260	7192792 > 7260
pw-myciel4	488828 > 7201	1030009 4773	1020457 4858	1019259 4723	1011804 4486	1131200 > 7261
qiu	9811 83	13066 56	13238 58	13134 59	13116 58	13220 58
rail507	1319 2126	1365 1764	1347 2664	1192 2579	1212 2667	1238 2605
ran16x16	441109 396	407862 234	396327 237	398390 254	395543 232	396936 242
reblock67	83043 339	157768 345	153298 323	127601 184	200477 210	115787 236
rmatr100-p10	901 298	494 155	551 145	551 142	513 157	550 145
rmatr100-p5	397 855	240 443	257 388	240 443	259 388	246 443
rmine6	687364 6508	560402 2201	599044 2396	639800 2155	633707 2319	580808 2228
roch-4-11	13194 399	16390 262	16023 256	12967 201	14862 242	13414 237
rococoC10-001000	1075742 > 7201	686793 3971	1015720 5149	977730 4872	689741 4048	758232 4203
roll3000	1322672 > 7201	1175475 6077	998800 4924	908010 4715	906029 4624	759170 3786
satellites1-25	16711 4956	22448 > 7326	50530 4838	51454 6964	20464 > 7326	42250 7082
sp98ic	40930 ! 5053	1090082 > 7264	818385 > 7264	860923 > 7264	682807 > 7264	700612 > 7264
sp98ir	8984 202	5986 102	6776 109	5431 107	5864 109	5720 107
tanglegram1	27 2358	524 > 7264	463 > 7264	582 > 7264	436 > 7264	369 > 7264
tanglegram2	3 13	3 12	3 12	3 12	3 12	3 12
timtabl	1014862 746	1313918 401	1230278 401	1235504 353	1199520 366	1587546 461
triptim1	39 > 7207	269 > 7265	269 > 7265	244 > 7274	211 > 7266	218 > 7407
unitcal.7	12785 2501	9766 3676	11222 4228	8459 3349	11404 3450	27647 6237
vpghard	3693 > 7206	12118 > 7284	9024 > 7284	10409 > 7281	10969 > 7281	7768 > 7283
zib54-UUE	565989 6971	665451 5835	643949 5952	733288 7020	658769 5822	656183 5786
geom. mean (solved: 52): 411.03	9227 685.3	7872 402.7	8229 416.6	7875 410.9	7993 410.0	8024 414.9
geom. mean (all): 1178.30	- 1554.6	- 1161.4	- 1172.2	- 1185.5	- 1184.0	- 1188.4
geom. mean (solved: 59): 531.69		12182 522.4	12791 536.1	12045 531.6	12334 524.7	12666 534.3
solved/timeout/abort	58/21/8	64/18/5	65/17/5	65/17/5	65/17/5	64/19/4
speedup (solved: 52): 1.668		1.70	1.65	1.67	1.67	1.65

Table 19: Normal ramp-up (Eight SOLVER Threads)

Name	One thread Nodes Time	Run - 1 Nodes Time	Run - 2 Nodes Time	Run - 3 Nodes Time	Run - 4 Nodes Time	Run - 5 Nodes Time
30n20b8	4639 > 7219	50758 > 7264	86983 5450	166578 6715	65305 > 7264	162060 7199
acc-tight5	1808 353	348 75	341 75	330 76	347 75	349 75
aflow40b	668667 6444	180560 635	163980 636	189685 639	157344 539	180625 598
air04	215 149	232 158	182 164	162 157	166 154	206 160
app1-2	392 2163	534 4924	534 4837	544 4975	543 4831	538 4916
ash608gpia-3col	7 77	19 137	19 137	19 137	19 137	19 139
bab5	12846 > 7201	20310 > 7316	15370 > 7316	5532 > 7316	24007 > 7316	25943 > 7316
beasleyC3	992738 > 7203	4266670 > 7260	4328413 > 7260	4333290 > 7260	4178910 > 7260	4420647 > 7260
biella1	3270 1554	8934 1140	6342 1034	7637 1230	10017 1592	11014 1772
bienst2	86468 439	129503 148	128972 157	140029 158	137437 173	128241 164
binkar10.1	135435 280	58792 61	56644 71	53559 58	68584 90	57738 79
bley_x11	1 342	1 353	1 349	1 347	1 350	1 350
bnatt350	4134 859	22276 546	22353 693	22015 688	44324 1348	22125 705
core2536-691	810 1487	246 1113	358 1430	205 1089	517 1783	249 1191
cov1075	976932 > 7201	1764076 6087	1748105 6158	1778973 6551	1777983 5969	1737144 6648
csched010	684362 > 7200	970006 3716	948493 3559	1032955 3602	912473 3424	1095223 3994
danoimt	870942 > 7201	779000 1447	792158 1460	784396 1453	782157 1475	790119 1439
dfn-gwin-UUM	87613 239	62082 80	1 ! 1	53107 77	52526 78	51764 78
eil33-2	10571 190	3456 464	4359 560	3890 524	3872 390	3890 474
eilB101	9239 1292	1949 369	1281 391	1853 345	1446 290	1467 410
enlight13	745476 857	7957824 3482	17353672 > 7260	14355830 > 7260	4740224 2192	13073027 > 7260
enlight14	259155 316	20407853 > 7260	9069390 > 7260	17426513 > 7260	19755862 > 7260	10815820 5010
ex9	1 194	1 190	1 190	1 193	1 190	1 191
glass4	2990992 ! 4138	11075826 3336	17113644 > 7263	20968618 > 7260	19838625 > 7260	17091658 3732
gmu-35-40	1970052 ! 1785	16949335 ! 2501	18551379 ! 2608	17154064 ! 2362	15877660 ! 2266	16520291 ! 2317
iis-100-0-cov	106874 2669	77671 573	78201 575	74428 567	75795 563	76990 567
iis-bupa-cov	113300 > 7202	155435 2629	157047 2643	158469 2670	157055 2670	156627 2668
iis-pima-cov	12469 1526	7941 457	7374 463	7794 477	7529 442	7668 463
lectsched-4-obj	21026 826	15268 257	16402 262	18470 277	14434 249	17876 278
m100n500k4r1	5050160 > 7201	19080177 > 7260	23487435 > 7260	26538761 > 7260	28922081 > 7260	25832322 > 7260
macrophage	541612 > 7201	1842048 > 7260	1549242 > 7260	1845397 > 7260	1766582 > 7260	1800379 > 7260
map18	261 1182	186 1649	180 1552	180 1619	167 1427	185 1614
map20	526 926	157 1102	191 1283	176 649	192 1210	191 1129
mcsched	16113 341	29768 237	27926 235	29565 232	31750 234	30011 239
mik-250-1-100-1	1421995 457	535864 72	533951 70	567185 69	554630 68	564939 73
mine-166-5	6170 109	2165 54	1296 56	2161 60	2803 54	1429 60
mine-90-10	189285 1364	216914 412	155984 296	174236 268	199973 257	91622 176
msec98-ip	485 > 7212	511 > 7266	568 > 7266	329 > 7265	67 > 7265	107 > 7265
mssp16	1 ! 144	1 ! 4689	1 ! 4711	1 ! 4468	1 ! 4679	1 ! 4691
mzsv11	8361 1868	7662 1313	9844 2058	14643 2604	8749 1854	10964 2416
n3div36	37993 ! 2825	35540 > 7267	329159 > 7266	391599 > 7266	357239 > 7266	68918 > 7266
n3seq24	1 72	328 > 7334	56 > 7311	262 > 7312	27 > 7314	51 > 7311
n4-3	57354 1466	44323 608	51743 724	47043 631	40777 645	43231 598
neoi-1109824	20142 283	3618 90	2038 100	3558 100	4281 136	7469 138
neos-1337307	239423 > 7201	857799 > 7261	568652 > 7261	782860 > 7261	791665 > 7261	750376 > 7261
neos-1396125	40087 4125	52022 946	52324 942	50162 898	48977 901	52561 928
neos13	17847 > 7201	516 2631	2128 3107	711 2544	1579 2883	1439 2917
neos-1601936	7771 5311	11962 2201	9788 1961	6344 1640	23304 2312	27558 3487
neos18	6827 81	10503 78	11812 74	13963 76	14076 88	9011 89
neos-476283	1 ! 273	634 ! 4068	531 4818	691 ! 3406	453 ! 3145	485 ! 4031
neos-686190	4739 134	755 55	605 51	1273 57	711 54	580 52
neos-849702	126716 3193	7039 129	7160 130	7029 129	7092 129	7185 130
neos-916792	66213 511	2418476 > 7262	2481609 > 7262	2272150 > 7262	1763322 > 7262	2048871 > 7262
neos-934278	2755 > 7206	7975 5810	486 > 7261	486 > 7261	147 > 7261	302 > 7261
net12	3678 4536	5516 > 7275	6183 > 7275	6781 > 7275	6724 > 7275	6973 > 7275
netdiversion	26 > 7295	35 > 7317	39 > 7350	41 > 7397	41 > 7327	33 > 7317
newdano	2842106 > 7201	3275726 1419	3209603 1779	3522105 1651	3469205 1740	3337785 1775
noswot	575618 217	849292 95	765034 86	814779 98	891314 109	1050260 130
ns1208400	4817 1361	68762 4029	208778 6570	49730 3572	101722 5376	51655 2574
ns1688347	4538 528	1419 189	2989 200	1824 223	5484 304	2387 204
ns1758913	1 ! 3132	- -	- -	- -	- -	- -
ns1766074	945109 1318	623409 298	633261 278	654862 273	631705 291	631187 283
ns1830653	88276 1111	107756 512	103066 432	97787 549	113045 572	96843 486
opm2-z7-s2	1978 1142	626 1675	672 1601	808 1722	507 1769	854 1601
pg5_34	318742 2339	326399 664	255659 591	307432 650	262733 598	317089 642
pigeon-10	2955734 > 7200	10094457 > 7260	3313541 > 7260	8919522 ! 4713	10200522 > 7260	5155955 ! 3065
pw-myciel4	488828 > 7201	1998937 6339	2187613 6920	1877371 6024	2939040 > 7261	2379164 6733
qiu	9811 83	11762 35	11840 32	12209 33	10780 35	11729 33
rail507	1319 2126	719 3416	1466 5200	1164 4467	1392 4997	836 3865
ran16x16	441109 396	336208 194	460150 209	380988 207	329889 195	381008 175
reblock67	83043 339	254753 352	157230 267	115359 137	167176 227	123175 157
rmatr100-p10	901 298	370 135	373 125	359 142	398 137	353 136
rmatr100-p5	397 855	226 455	225 453	223 453	238 451	223 453
rmine6	687364 6508	584026 1595	672698 1787	558257 1618	586858 1609	619667 1377
roch_4-11	13194 399	18178 250	13344 216	18565 242	16025 295	14339 246
rococoC10-001000	1075742 > 7201	642320 1830	553704 1411	468019 1375	502728 1474	469472 1530
roll3000	1322672 > 7201	425597 1357	415860 1385	282730 1054	344322 1136	294706 1035
satellites1-25	16711 4956	8389 > 7326	15738 5793	9065 6149	25491 7170	22624 > 7326
sp98ic	40930 ! 5053	211217 6120	258183 > 7264	320602 6881	251310 5786	258098 6476
sp98ir	8984 202	4207 113	3841 103	4329 98	4217 109	4744 111
tanglegram1	27 2358	343 > 7264	273 > 7264	235 > 7264	311 > 7264	334 > 7264
tanglegram2	3 13	3 12	3 12	3 12	3 12	3 12
timtabl	1014862 746	1240404 331	1455376 386	1379817 394	1390633 391	1316559 347
triptim1	39 > 7207	166 > 7266	165 > 7278	164 > 7278	167 > 7394	107 > 7268
unitcal_7	12785 2501	4159 > 7359	11406 > 7357	11338 > 7358	7113 > 7360	7880 > 7359
vpphard	3693 > 7206	5256 > 7281	4416 > 7284	4325 > 7281	4538 > 7281	5326 > 7281
zib54-UUE	565989 6971	571699 4406	661284 5040	600480 4594	603252 4606	580244 4391
geom. mean (solved: 50): 351.10	8811 665.8	6708 344.1	6762 353.8	6738 340.9	7282 366.4	6795 350.3
geom. mean (all): 1080.47	- 1554.6	- 1048.1	- 1137.2	- 1056.4	- 1091.6	- 1069.1
geom. mean (solved: 58): 456.45		11404 447.3	11728 459.3	11402 441.0	12385 470.9	11630 454.7
solved/timeout/abort	58/21/8	64/19/4	62/21/4	63/19/5	62/21/4	64/18/5
speedup (solved: 50): 1.898		1.94	1.88	1.95	1.82	1.90

Table 20: Deterministic runs (Four SOLVER threads)

Name	One thread		Comm		Racing		Normal	
	Nodes	Time	Nodes	Time	Nodes	Time	Nodes	Time
30n20b8	4639	> 7219	447	> 7203	445	> 7239	18145	> 7265
acc-tight5	1808	353	72	147	72	147	3794	691
aFlow40b	668667	6444	58258	! 2688	168035	2322	238996	! 3506
air04	215	149	49	251	49	251	178	218
app1-2	392	2163	47	3388	47	3299	2705	7157
ash608gpia-3col	7	77	7	231	7	228	19	169
bab5	12846	> 7201	4352	> 7201	18716	> 7312	11643	> 7313
beasleyC3	992738	> 7203	127919	! 3820	461521	! 3336	450397	! 3240
biella1	3270	1554	2854	2793	2854	2796	4386	2111
bienst2	86468	439	95433	1515	96858	2085	139404	786
binkar10.1	135435	280	144577	1121	11933	1046	92369	245
bley_x11	1	342	1	411	1	410	1	352
bnatt350	4134	859	4134	2140	4134	2167	18865	2573
core2536-691	810	1487	313	1443	313	1436	1928	2601
cov1075	976932	> 7201	229954	> 7201	273275	> 7261	705549	> 7260
csched010	684362	> 7200	100830	! 5267	457088	! 4910	517559	> 7260
dancint	870942	> 7201	211546	> 7201	438911	> 7261	986745	6043
dfn-gwin-UUM	87613	239	64391	518	10272	732	69917	262
eil33-2	10571	190	9984	459	9984	470	7300	595
eilB101	9239	1292	7571	1719	7571	1718	5395	995
enlight13	745476	857	367322	1256	2195391	! 3160	5057077	! 6019
enlight14	259155	316	259155	916	259155	909	5077785	> 7261
ex9	1	194	1	192	1	189	1	191
glass4	2990992	! 4138	468754	! 3582	-	-	2099207	! 2202
gmu-35-40	1970052	! 1785	299818	! 1006	1175507	! 655	1074030	! 692
iis-100-0-cov	106874	2669	98454	> 7200	52225	6213	68698	5128
iis-bupa-cov	113309	> 7202	44866	> 7200	80058	> 7260	156623	> 7261
iis-pima-cov	12469	1526	8920	2424	4138	5436	27161	3224
lectsched-4-obj	21026	826	10199	963	8207	637	22274	961
m100n500k4r1	5050160	> 7201	429553	! 2215	1523014	! 1727	1595007	! 1444
macrophage	541612	> 7201	138396	> 7201	1	! 3784	352322	! 7108
map18	261	1182	493	2281	493	2276	246	2836
map20	526	926	399	1512	399	1512	246	1637
mcsched	16113	341	14948	619	14948	619	24303	578
mik-250-1-100-1	1421995	457	808088	! 685	345850	813	889615	341
mine-166-5	6170	109	3278	169	3278	170	4766	124
mine-90-10	189285	1364	178919	3117	217764	849	440563	2603
msc98-ip	485	> 7212	432	> 7209	439	> 7234	1	> 7266
msp16	1	! 144	1	! 2541	1	! 2544	1	! 2536
mzv11	8361	1868	5064	4441	8568	! 7427	15524	! 3392
n3div36	37993	! 2825	9129	! 2401	35485	! 2794	44137	! 2787
n3seq24	1	! 72	1	> 7208	1	> 7233	541	> 7319
n4-3	57354	1466	50613	3263	20777	4841	37813	1196
neos-1109824	20142	283	10058	420	3495	1020	23009	415
neos-1337307	239423	> 7201	107488	> 7201	212402	> 7262	255456	> 7263
neos-1396125	40087	4125	13223	> 7201	22407	> 7260	31323	6010
neos13	17847	> 7201	1519	3254	1519	3245	16912	> 7263
neos-1601936	7771	5311	5412	> 7201	4176	> 7262	7266	> 7263
neos18	6827	81	7855	169	5019	731	17765	220
neos-476283	1	! 273	51	1398	51	1397	146	> 7508
neos-686190	4739	134	3676	256	3676	257	12529	341
neos-849702	126716	3193	20907	2473	20907	2474	111640	2464
neos-916792	66213	511	67156	2487	566959	! 6253	549452	! 4712
neos-934278	2755	> 7206	1	> 7219	1	> 7208	2739	> 7262
net12	3678	4536	3770	> 7203	3703	> 7272	4570	> 7276
netdiversion	26	> 7295	-	-	-	-	161	> 7563
newdano	2842106	> 7201	448819	! 6098	1529148	> 7260	1711583	! 3618
noswot	575618	217	403652	1126	928475	510	547869	216
ns1208400	4817	1361	4817	2561	4817	2567	22369	> 7260
ns1688347	4538	528	3633	1283	2810	1201	9578	1307
ns1758913	1	! 3132	1	> 7898	1	> 7734	-	-
ns1766074	945109	1318	907103	3205	907103	3192	838665	1210
ns1830653	88276	1111	70621	2545	142230	5572	131170	1944
opm2-z7-s2	1978	1142	2461	2768	1938	3056	5420	2623
pg5_34	318742	2339	70272	! 2938	277995	> 7261	320562	2365
pigeon-10	2955734	> 7200	1	> 7200	1	> 7200	2055339	! 2209
pw-myciel4	488828	> 7201	114161	> 7200	407777	> 7261	625101	> 7261
qui	9811	83	9525	246	8965	328	13385	415
rail507	1319	2126	1174	4137	1174	4023	1517	4507
ran16x16	441109	396	392938	1444	36995	1109	429457	463
reblock67	83043	339	88623	751	187620	1074	130467	643
rmatr100-p10	901	298	893	467	893	464	544	531
rmatr100-p5	397	855	403	1722	403	1715	249	1188
rmine6	687364	6508	188361	! 6328	732559	! 4223	582738	4707
rocll-4-11	13194	399	11711	829	19806	1281	18472	752
rococoC10-001000	1075742	> 7201	88488	! 3414	120082	2316	355951	! 3655
roll3000	1322672	> 7201	173583	! 5164	72191	2304	763075	5485
satellites1-25	16711	4956	5787	> 7200	5813	> 7201	9636	> 7326
sp98ic	40930	! 5053	19035	! 4746	60527	! 2498	61767	! 4565
sp98ir	8984	202	5239	296	5346	1563	4945	203
tanglegram1	27	2358	18	> 7322	22	> 7264	258	> 7265
tanglegram2	3	13	3	19	3	19	3	14
timtab1	1014862	746	778328	2513	1905393	2849	1815457	1275
triptim1	39	> 7207	11	> 7564	11	> 7567	224	> 7502
unitcal.7	12785	2501	15040	> 7208	2548	> 7356	28243	> 7359
vpphard	3693	> 7206	300	> 7204	300	> 7212	5122	> 7287
zib54-UUE	565989	6971	67815	! 2744	141304	! 2149	162715	! 1741
geom. mean (solved: 43)	5576	460.3	4003	880.4	3426	989.0	8355	793.3
geom. mean (all)	-	1554.6	-	2386.0	-	2457.1	-	2273.0
geom. mean (solved: 44)			3625	889.7	3113	996.8	9268	829.1
solved/timeout/abort	58/21/8		48/22/17		50/23/14		49/22/16	
speedup (solved: 43)			0.52		0.47		0.64	

Table 21: Deterministic runs (Eight SOLVER threads)

Name	One thread		Comm		Racing		Normal	
	Nodes	Time	Nodes	Time	Nodes	Time	Nodes	Time
30n20b8	4639	> 7219	347	> 7206	346	> 7220	4582	> 7265
acc-tight5	1808	353	310	330	310	330	1741	537
aFlow40b	668667	6444	73054	! 3664	94045	2244	283445	5214
air04	215	149	11	359	11	350	191	324
app1-2	392	2163	79	6475	79	6445	617	> 7285
ash608gpia-3col	7	77	7	484	7	422	19	183
bab5	12846	> 7201	1670	> 7216	10582	> 7312	10619	> 7317
beasleyC3	992738	> 7203	120315	! 6085	803204	! 4835	795977	! 5507
biella1	3270	1554	4242	5391	4242	5426	7727	3827
bienst2	86468	439	88341	2251	81525	1996	141730	631
binkar10.1	135435	280	135816	1901	12270	1082	105139	451
bley_x11	1	342	1	466	1	465	1	350
bnatt350	4134	859	2831	2666	2831	2666	29574	3957
core2536-691	810	1487	167	2672	167	2670	1969	3874
cov1075	976932	> 7201	127550	> 7200	882921	> 7260	879769	> 7260
csched010	684362	> 7200	76215	! 7009	442503	> 7260	794212	> 7261
dancint	870942	> 7201	126984	> 7201	418710	> 7260	1016569	> 7260
dfn-gwin-UUM	87613	239	20880	628	10250	790	64020	337
eil33-2	10571	190	9727	817	9727	814	5458	569
eilB101	9239	1292	5598	2741	5598	2757	6543	1261
enlight13	745476	857	168971	1018	3349375	6610	3891279	! 6716
enlight14	259155	316	100054	636	100054	631	5435865	> 7260
ex9	1	194	1	193	1	191	1	191
glass4	2990992	! 4138	443722	! 5771	2486063	3884	-	-
gmu-35-40	1970052	! 1785	252817	! 2068	1978327	! 1284	1930314	! 1145
iis-100-0-cov	106874	2669	54637	> 7201	52111	6299	77800	1887
iis-bupa-cov	113309	> 7202	28012	> 7201	80329	> 7261	143979	> 7260
iis-pima-cov	12469	1526	8920	4126	4097	5731	23780	3631
lectsched-4-obj	21026	826	4580	881	18650	1289	30085	846
m100n500k4r1	5050160	> 7201	1	! 3404	2591489	! 2545	2734885	! 2010
macrophage	541612	> 7201	131945	> 7201	1	! 6360	464013	> 7261
map18	261	1182	347	1497	347	1482	185	3301
map20	526	926	399	1859	399	1838	231	2109
mcsched	16113	341	12961	1123	12961	1111	41810	1180
mik-250-1-100-1	1421995	457	682671	! 1073	211378	691	546627	269
mine-166-5	6170	109	2332	244	2332	244	3617	149
mine-90-10	189285	1364	92041	2880	267561	1276	234543	1314
msc98-ip	485	> 7212	414	> 7327	414	> 7322	823	> 7270
mspp16	1	! 144	1	! 2560	1	! 2559	1	! 4970
mzsv11	8361	1868	3359	5385	3359	5372	15010	3626
n3div36	37993	! 2825	9789	! 4086	53986	! 3811	72402	! 3652
n3seq24	1	! 72	1	> 7210	1	> 7206	588	> 7311
n4-3	57354	1466	38529	3935	24528	6759	41518	1417
neos-1109824	20142	283	10058	811	4012	1263	21572	427
neos-1337307	239423	> 7201	49208	> 7201	272893	> 7262	289948	> 7262
neos-1396125	40087	4125	3208	> 7200	15028	> 7260	58921	6408
neos13	17847	> 7201	9	5033	9	4999	3239	4395
neos-1601936	7771	5311	2447	> 7200	3192	> 7262	7662	> 7262
neos18	6827	81	6141	245	4155	702	14517	197
neos-476283	1	! 273	27	2199	27	2044	647	! 6049
neos-686190	4739	134	2194	386	2194	386	4924	288
neos-849702	126716	3193	17371	4367	20575	4371	230617	4017
neos-916792	66213	511	61166	3766	744050	> 7263	917823	! 6968
neos-934278	2755	> 7206	201	> 7219	201	> 7203	3013	> 7265
net12	3678	4536	1956	> 7200	3226	> 7275	3639	> 7275
netdiversion	26	> 7295	-	-	-	-	271	> 7489
newdano	2842106	> 7201	269610	> 7202	2348882	> 7261	2974156	! 5739
noswot	575618	217	347127	1652	925777	505	800662	436
ns1208400	4817	1361	1932	2823	1932	2813	28556	> 7261
ns1688347	4538	528	2824	2188	2867	2116	8300	954
ns1758913	1	! 3132	1	> 7687	1	> 7689	-	-
ns1766074	945109	1318	903761	5184	903761	5183	799620	920
ns1830653	88276	1111	63027	3541	44557	2046	121423	2158
opm2-z7-s2	1978	1142	1555	4314	1555	4330	2808	3244
pg5_34	318742	2339	55189	! 4576	250591	> 7260	329582	2717
pigeon-10	2955734	> 7200	1	> 7200	1	> 7200	1090801	! 921
pw-myciel4	488828	> 7201	51757	> 7200	467276	> 7261	631072	> 7262
qiu	9811	83	9757	396	9757	397	8263	427
rai1507	1319	2126	1065	> 7202	1063	> 7202	1227	6155
ran16x16	441109	396	304484	2172	44900	977	391666	415
reblock67	83043	339	74015	1073	105347	896	128671	698
rmatr100-p10	901	298	851	647	851	647	504	618
rmatr100-p5	397	855	437	2867	437	2866	243	1228
rmine6	687364	6508	124995	> 7201	1180463	! 6113	546948	4294
rocl1-4-11	13194	399	11728	1424	18210	1469	13759	1012
rococoC10-001000	1075742	> 7201	78646	! 5113	370821	5206	586323	! 4989
roll3000	1322672	> 7201	147918	> 7201	182877	4150	868439	> 7261
satellites1-25	16711	4956	626	> 7893	626	> 7891	6485	> 7327
sp98ic	40930	! 5053	18354	> 7201	99677	! 4637	112019	! 6401
sp98ir	8984	202	5662	496	5662	495	3537	282
tanglegram1	27	2358	18	> 7289	18	> 7220	288	> 7269
tanglegram2	3	13	3	108	3	109	3	16
timtab1	1014862	746	591562	3370	1887068	2424	1414433	1712
triptim1	39	> 7207	1	> 7265	1	> 7335	-	-
unitcal.7	12785	2501	4390	> 7232	3021	> 7367	19923	> 7359
vpphard	3693	> 7206	204	> 7221	204	! 7234	3491	> 7291
zib54-UUE	565989	6971	54628	! 3776	278505	! 6518	291722	! 3160
geom. mean (solved: 43)	5820	459.0	3354	1306.7	3171	1253.9	9175	832.9
geom. mean (all)	-	1554.6	-	2953.2	-	2805.4	-	2381.4
geom. mean (solved: 44)			3006	1322.2	2846	1267.9	9175	832.9
solved/timeout/abort	58/21/8		47/27/13		52/24/11		48/23/16	
speedup (solved: 43)			0.35		0.37		0.61	



Table 22: 5 runs with four SOLVER threads on selected instances from MINLPLib

Name	One thread		Run - 1		Run - 2		Run - 3		Run - 4		Run - 5	
	Nodes	Time	Nodes	Time	Nodes	Time	Nodes	Time	Nodes	Time	Nodes	Time
4stufen	2455190	> 7200	13911395	> 7200	16548286	> 7200	19034269	> 7652	15645529	> 7565	12304282	> 7567
beuster	2019633	> 7200	13014702	> 7200	18364128	> 7200	6791064	! 7200	26906183	> 7200	15487388	> 7200
cecil_l3	1608177	> 7200	7542778	> 7200	7626310	> 7200	7469557	> 7200	7472804	> 7200	7531383	> 7200
chp_partload	8353	> 7200	1	! 1	1	! 1	6077	> 7200	6077	> 7200	6077	> 7200
csched2a	1235475	> 7200	7775333	> 7200	7764494	> 7200	605	> 7200	9439345	> 7200	7784271	> 7200
csched2b	182072	> 7200	4147624	> 7200	4165828	> 7200	4171026	> 7200	4166937	> 7200	4166972	> 7200
eg_all_s	139	> 7200	290	> 7200	155	> 7200	381	> 7200	272	> 7200	183	> 7200
eg_disc2_s	133	> 7200	133	> 7200	133	> 7200	133	> 7200	133	> 7200	133	> 7200
eg_int_s	1	> 7200	65	> 7200	65	> 7200	65	> 7200	65	> 7200	65	> 7200
enpro48pb	4	> 7200	4	> 7200	4	> 7200	4	> 7200	4	> 7200	4	> 7200
ex1233	279848	70	237	1	247	1	230	1	210	1	155	1
fac2	7960984	> 7200	186408	! 7200	220588	! 7200	216410	! 7200	186358	! 7200	216244	! 7200
feedtray	4565461	> 7200	147	! 7200	30861424	> 7200	30671920	> 7200	25970158	> 7200	30167018	> 7200
fo7	274621	> 7200	1719088	> 7200	1632670	> 7200	1624430	> 7200	1715885	> 7200	1629798	> 7200
fo8_ar2_1	201538	132	224835	69	260981	75	261451	76	222269	68	263872	76
fo8_ar25_1	435919	259	1365702	262	1444653	278	1641153	266	1496715	286	1399248	265
fo8_ar3_1	269179	157	733697	138	730500	137	729980	138	729918	137	729903	138
fo8_ar4_1	202993	109	191768	46	182710	43	182371	44	182340	44	180710	44
fo8_ar5_1	140062	120	150836	53	136182	65	145590	72	126452	64	92835	52
fo9_ar2_1	182645	133	544302	120	475015	124	597211	135	501529	127	519301	117
fo9_ar25_1	226582	180	594971	167	598557	169	631827	176	620740	174	618466	173
fo9_ar3_1	3763883	2779	5811784	1148	8739087	1358	5839421	1136	6386396	1244	5573359	1065
fo9_ar4_1	10780884	> 7200	35779189	6243	35684117	6228	36104803	6364	35447904	6353	36794119	6759
fo9_ar5_1	121189	113	630474	191	471243	147	782951	227	508882	164	567036	177
fuzzy	559215	484	1462533	465	1929344	553	968852	346	1676248	511	1810449	525
ghg_1veh	2457271	1982	2850095	1045	2510947	959	2007240	791	2218384	860	2837909	1056
ghg_3veh	2357571	2030	2041971	557	5021402	1166	1861546	515	1849769	513	1921768	532
hda	1585116	> 7200	10023015	> 7200	8462365	> 7200	6948795	> 7200	8738087	> 7200	8115071	> 7200
lop97ic	8935058	> 7200	18594	! 7200	28933	! 7200	280997	! 7200	14047	! 7200	13950	! 7200
lop97icx	287687	> 7200	2555840	> 7200	2406659	> 7200	2405426	> 7200	1968285	> 7200	3592804	> 7200
mbtd	354972	> 7200	1319819	7200	1898941	> 7200	1970578	> 7200	1680755	> 7200	1624566	> 7200
netmod_doll	120167	> 7200	527440	> 7200	762745	> 7200	568072	> 7200	619989	> 7200	620526	> 7200
no7_ar3_1	4155061	> 7200	20501488	> 7200	20323880	> 7200	20067847	> 7200	20430108	> 7200	20150643	> 7200
no7_ar4_1	238	> 7200	22	> 7200	1	> 7200	1	> 7200	32	> 7200	22	> 7200
no7_ar5_1	60544	2431	831440	> 7200	829894	> 7200	797756	> 7200	830953	> 7200	829147	> 7200
nous1	334433	215	1139459	257	1151387	259	1145184	258	1152217	258	1138864	257
nuclear10a	196757	146	912547	202	850199	201	920112	203	914816	202	856896	204
nuclear10b	100305	71	292324	78	306521	81	304009	80	308110	79	303954	79
nuclear14a	3246625	> 7200	573133	! 7200	273645	! 7200	539698	! 7200	344206	! 7200	4611479	! 7200
nuclear14b	1	> 7200	53	> 7200	53	> 7200	53	> 7200	53	> 7200	53	> 7200
nuclear14c	1	> 7200	17	> 7200	16	> 7200	16	> 7200	17	> 7200	16	> 7200
nuclear14d	20547	> 7200	2747	> 7200	2747	> 7200	1882	> 7200	5078	> 7200	2747	> 7200
nuclear25a	27545	> 7200	97802	> 7200	97964	> 7200	97972	> 7200	98036	> 7200	98013	> 7200
nuclear25b	22200	> 7200	2824	> 7200	2464	> 7200	6569	> 7200	5117	> 7200	5367	> 7200
nuclear49a	19011	> 7200	84105	> 7200	84101	> 7200	84153	> 7200	84209	> 7200	84139	> 7200
nuclear49b	1423	> 7200	180	> 7200	178	> 7200	181	> 7200	180	> 7200	178	> 7200
nvs09	2135	> 7200	3426	> 7200	4843	> 7200	4565	> 7200	6102	> 7200	1886	> 7200
o7_2	18167003	> 7200	256235	! 7200	240053	! 7200	250168	! 7200	375048	! 7200	305545	! 7200
o7_ar2_1	1712445	1268	1440404	332	1443884	334	1444696	332	1446732	332	1441533	332
o7_ar25_1	136342	88	388692	84	386113	78	399248	85	256046	68	246555	64
o7_ar3_1	571227	429	1008091	221	1011031	222	1012629	222	1010864	222	1007948	222
o7_ar4_1	1070205	811	2178610	474	1886281	464	2165857	468	2159799	465	2180282	474
o7_ar5_1	1826075	1478	1286052	732	1214438	691	1243887	717	1238410	717	1256653	711
o8_ar4_1	692346	514	1651732	418	1623912	393	1804285	426	1744544	428	1645883	418
o9_ar4_1	2514799	1765	3670381	776	3666527	774	3665744	776	3675888	776	3673982	778
oil2	7880052	> 7200	18318695	4426	18473306	4474	18387973	4439	18359604	4447	18322512	4427
oil	7430950	> 7200	10756715	7191	10776074	> 7200	10879109	> 7200	10297478	> 7200	10672331	> 7200
pb302035	900257	> 7200	6905564	> 7200	4978548	> 7200	6457890	> 7200	5754460	> 7200	7804032	> 7200
pb302055	174359	> 7200	345769	> 7200	416704	> 7200	1002907	> 7200	999362	> 7200	757104	> 7200
pb302075	982598	> 7200	4039918	> 7200	4141148	> 7200	4191117	> 7200	4268354	> 7200	4069185	> 7200
pb302095	935753	> 7200	5431636	> 7200	4268845	> 7200	4185877	> 7200	4161476	> 7200	4058472	> 7200
pb351535	1003884	> 7200	4444158	> 7200	4441808	> 7200	4443191	> 7200	4444259	> 7200	4432590	> 7200
pb351555	1330925	> 7200	9015095	> 7200	9063748	> 7200	8986409	> 7200	9048688	> 7200	9067327	> 7200
pb351575	1084866	> 7200	4787791	> 7200	4788423	> 7200	5858564	> 7200	4790986	> 7200	4781073	> 7200
pb351595	1382010	> 7200	4644701	> 7200	4640221	> 7200	4630128	> 7200	4631447	> 7200	4637019	> 7200
product2	1140277	> 7200	4878882	> 7200	4876086	> 7200	4882624	> 7200	4517807	> 7200	4879988	> 7200
qap	1312069	> 7200	6486937	> 7200	5972223	> 7200	6642799	> 7200	6476313	> 7200	6440787	> 7200
qapw	2053746	> 7200	20653254	> 7200	21339260	> 7200	21703194	> 7200	22408926	> 7200	21464437	> 7200
saa_2	6819196	> 7200	23288193	> 7200	24689088	> 7200	27289323	> 7200	26340681	> 7200	22864190	> 7200
space25a	1624641	6912	5967547	> 7200	6585605	> 7200	5962659	> 7200	7136379	> 7200	6138323	> 7200
space960	1066	> 7200	2	> 7200	926	! 7200	938	! 7200	2	> 7200	840	! 7200
stockcycle	417210	> 7200	9904663	> 7200	509172	> 7200	587471	> 7200	2103903	> 7200	547764	> 7200
super1	2535	> 7200	22204	> 7200	22172	> 7200	2640	> 7200	22213	> 7200	3380	> 7200
super2	26114	179	59487	112	64710	117	66098	119	69454	122	78847	135
super3	57058	> 7200	1	! 1	1	! 1	1	! 1	1	! 1	1	! 1
super3t	62412	> 7200	1	! 1	1	! 1	1	! 1	1	! 1	1	! 1
synheat	89036	> 7200	1	! 1	1	! 1	1	! 1	1	! 1	1	! 1
tin12	84138	> 7200	357425	> 7200								

Table 23: 5 runs with eight SOLVER threads on selected instances from MINLPLib

Name	One thread		Run - 1		Run - 2		Run - 3		Run - 4		Run - 5	
	Nodes	Time	Nodes	Time	Nodes	Time	Nodes	Time	Nodes	Time	Nodes	Time
4stufen	2455190	> 7200	12033095	> 7200	15852047	> 7200	22286235	> 7656	23020391	> 7476	34203808	> 7467
beuster	2019633	> 7200	4135192	! 7200	223181	! 7200	56872033	> 7200	3026206	! 7200	67651660	> 7200
cecil_13	1608177	> 7200	10984760	> 7200	11183498	> 7200	11073979	> 7200	11139108	> 7200	11028381	> 7200
chp_partload	8353	> 7200	56079	> 7200	1	! 1	9045	> 7200	1	! 1	62	9057
csched2a	1235475	> 7200	3091464	> 7200	3095075	> 7200	3149039	> 7200	3089886	> 7200	3163849	> 7200
csched2	182072	> 7200	822985	> 7200	1140405	> 7200	544494	> 7200	533560	> 7200	938737	> 7200
eg_all_s	139	> 7200	312	> 7200	574	> 7200	261	> 7200	62	> 7200	1068	> 7200
eg_disc2_s	133	> 7200	117	> 7200	116	> 7200	86	> 7200	117	> 7200	117	> 7200
eg_disc_s	1	> 7200	65	> 7200	65	> 7200	65	> 7200	65	> 7200	65	> 7200
eg_int_s	4	> 7200	4	> 7200	4	> 7200	4	> 7200	4	> 7200	4	> 7200
enpro48pb	279848	70	30	1	30	1	30	1	30	1	30	1
ex1233	7960984	> 7200	107083	! 7200	100841	! 7200	81258	! 7200	407826	! 7200	125777	! 7200
fac2	4565461	> 7200	4145	! 7200	97651387	> 7200	79494184	> 7200	235	! 7200	653786	! 7200
feedtray	274621	> 7200	3950717	> 7200	3752993	> 7200	3096609	> 7200	3701396	> 7200	3895314	> 7200
fo7	201538	132	246752	43	236999	43	224567	42	247206	43	248810	45
fo8_ar2_1	435919	259	1321109	160	1315191	158	1302143	148	1234877	146	1416874	152
fo8_ar25_1	269179	157	731066	108	608888	82	647065	92	771176	116	809433	95
fo8_ar3_1	202993	109	144347	26	151387	25	153571	28	201626	27	154877	27
fo8_ar4_1	140062	120	101315	41	149892	54	182673	58	96818	38	198120	57
fo8_ar5_1	182645	133	604771	87	646099	114	532854	84	578545	86	505181	78
fo8	226582	180	577162	97	576158	93	576919	93	580117	98	574081	95
fo9_ar2_1	3763883	2779	5192236	708	5152661	! 7200	4846507	729	5503414	761	4399944	598
fo9_ar25_1	10780884	> 7200	33304444	3427	35043974	3615	30292659	3173	34994196	3680	38235650	4366
fo9_ar3_1	121189	113	1062324	163	1138025	172	1377085	199	1000274	167	1369034	211
fo9_ar4_1	559215	484	1778287	341	1927962	361	2052871	378	1906236	375	2308804	409
fo9_ar5_1	2457271	1982	2019190	490	3114197	681	1804832	451	3194335	682	3343729	672
fo9	2357571	2030	1864856	306	1936322	318	1660398	281	1524991	269	2013510	321
fuzzy	1585116	> 7200	17123093	> 7200	16728957	> 7200	13741904	> 7200	9825960	> 7200	14736156	> 7200
ghg_1veh	8935058	> 7200	9927	! 7200	15769	! 7200	25385	! 7200	23082	! 7200	10304	! 7200
ghg_3veh	287687	> 7200	1339122	> 7200	1383414	> 7200	3278664	> 7200	1524479	> 7200	2056687	> 7200
hda	354972	> 7200	2332139	> 7200	2298413	> 7200	2451015	> 7200	2450766	> 7200	2254485	> 7200
lop97ic	120167	> 7200	646199	> 7200	650835	> 7200	573431	> 7200	588521	> 7200	557847	> 7200
lop97icx	4155061	> 7200	30538789	> 7200	31299204	> 7200	31691975	> 7200	30954987	> 7200	31078684	> 7200
mbtd	238	> 7200	1	> 7200	1	> 7200	1	> 7200	1	> 7200	1	> 7200
netmod_doll	60544	2431	1450368	> 7200	1425750	> 7200	1431416	> 7200	1207269	6507	1438466	> 7200
no7_ar3_1	334433	215	1136073	164	1109829	152	1165448	161	1128204	155	1116733	157
no7_ar4_1	196757	146	537976	89	592435	93	549183	84	545558	82	626282	99
no7_ar5_1	100305	71	279909	55	280088	56	275427	59	256007	48	277131	56
nous1	3246625	> 7200	1394092	! 7200	523996	! 7200	764004	! 7200	1844853	! 7200	178850	! 7200
nuclear10a	1	> 7200	26	> 7200	26	> 7200	28	> 7200	27	> 7200	27	> 7200
nuclear10b	1	> 7200	14	> 7200	16	> 7200	15	> 7200	11	> 7200	15	> 7200
nuclear14a	20547	> 7200	7056	> 7200	11672	> 7200	11672	> 7200	6619	> 7200	7207	> 7200
nuclear14b	27545	> 7200	159323	> 7200	151675	> 7200	21760	> 7200	151426	> 7200	159545	> 7200
nuclear25a	22200	> 7200	6386	> 7200	6390	> 7200	6384	> 7200	6324	> 7200	6380	> 7200
nuclear25b	19011	> 7200	164895	> 7200	164956	> 7200	164964	> 7200	164932	> 7200	105484	> 7200
nuclear49a	1423	> 7200	956	> 7200	962	> 7200	946	> 7200	946	> 7200	884	> 7200
nuclear49b	2135	> 7200	54	> 7200	54	> 7200	60	> 7200	60	> 7200	54	> 7200
nvs09	18167003	> 7200	7996	! 7200	105279	! 7200	5663	! 7200	4238	! 7200	89704	! 7200
o7_2	1712445	1268	1662135	205	1612626	202	1623607	218	1627693	208	1625435	209
o7_ar2_1	136342	88	240563	44	317402	! 7200	318530	! 7200	248355	44	251244	46
o7_ar25_1	571227	429	1049534	150	1173570	! 7200	961521	139	1038808	156	1055023	156
o7_ar3_1	1072205	811	1957794	324	1878914	291	1913462	319	1907804	304	2054804	323
o7_ar4_1	1826075	1478	1381503	507	1159115	451	1197005	467	1320063	482	1141514	449
o7_ar5_1	692346	514	1761340	285	2206006	352	1471924	240	2576377	365	2493977	354
o7	2514799	1765	3499660	439	3456239	444	3442085	456	3525205	463	3501460	441
o8_ar4_1	7880052	> 7200	19067153	3419	19690506	3340	19457535	3478	20611322	3463	21533468	4255
o9_ar4_1	7430950	> 7200	12158990	4215	11407137	4076	11818736	4282	10397984	3961	12086431	4326
oil2	900257	> 7200	323124	532	25736	131	6728710	> 7200	7568222	> 7200	207369	745
oil	174359	> 7200	1178218	> 7200	1108114	> 7200	1036154	> 7200	1	! 1	1	! 1
pb302035	982598	> 7200	4920362	> 7200	5014100	> 7200	5023188	> 7200	4918437	> 7200	5116637	> 7200
pb302055	935753	> 7200	5028859	> 7200	5031086	> 7200	5027951	> 7200	5021697	> 7200	5009082	> 7200
pb302075	1003884	> 7200	5584437	> 7200	5587891	> 7200	5588603	> 7200	5576462	> 7200	5586124	> 7200
pb302095	1330925	> 7200	8614776	> 7200	7403973	> 7200	7267930	> 7200	7312612	> 7200	8663940	> 7200
pb351535	1084866	> 7200	6211008	> 7200	6234805	> 7200	6213995	> 7200	6551712	> 7200	6252899	> 7200
pb351555	1382010	> 7200	6616606	> 7200	6291594	> 7200	6505900	> 7200	6481530	> 7200	6289345	> 7200
pb351575	1140277	> 7200	6581971	> 7200	6291427	> 7200	6307275	> 7200	6302357	> 7200	6602648	> 7200
pb351595	1312069	> 7200	6871874	> 7200	6887632	> 7200	6882440	> 7200	6878978	> 7200	6886228	> 7200
product2	2053746	> 7200	34360899	> 7200	32558591	> 7200	33115708	> 7200	33870590	> 7200	32832781	> 7200
qap	6819196	> 7200	35277773	> 7200	35587971	> 7200	33834718	> 7200	34623296	> 7200	30006983	> 7200
qapw	1624641	6912	10146832	> 7200	10820443	> 7200	8658298	> 7200	12100861	> 7200	10830118	> 7200
saas_2	1066	> 7200	313	> 7200	564	> 7200	220	> 7200	1405	> 7200	98	> 7200
space25a	417210	> 7200	9085675	> 7200	6156412	> 7200	14361749	> 7200	8878438	> 7200	9490889	> 7200
space960	2535	> 7200	3350	> 7200	4294	> 7200	3350	> 7200	3350	> 7200	9404	> 7200
stockcycle	26114	179	82634	89	42952	64	79105	86	89020	93	61910	75
super1	57058	> 7200	1	! 1	1	! 1	1	! 1	1	! 1	1	! 1
super2	62412	> 7200	1	! 1	1	! 1	1	! 1	1	! 1	1	! 1
super3	89036	> 7200	1	! 1	1	! 1	1	! 1	1	! 1	1	! 1
super3t	84138	> 7200	626321	> 7200	490952	> 7200	554117	> 7200	583393	> 7		