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## MIPLIB 2010

## Mixed Integer Programming Library version 5

## http://miplib.zib.de/

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#### Abstract

This paper reports on the fifth version of the Mixed Integer Programming Library. The miplib 2010 is the first miplib release that has been assembled by a large group from academia and from industry, all of whom work in integer programming. There was mutual consent that the concept of the library had to be expanded in order to fulfill the needs of the community. The new version comprises 361 instances sorted into several groups. This includes the main benchmark test set of 87 instances, which are all solvable by today's codes, and also the challenge test set with 164 instances, many of which are currently unsolved. For the first time, we include scripts to run automated tests in a predefined way. Further, there is a solution checker to test the accuracy of provided solutions using exact arithmetic.


Keywords Mixed Integer Programming • Problem Instances • IP • MIP • MIPLIB
Mathematics Subject Classification (2000) 90C11 • 90C10 • 90C90

[^1]
## 1 Introduction

The miplib is now going into its fifth incarnation. Starting in 1992 with the first two versions by Bixby, Boyd, and Indovina [23], the update to miPlib 3 by Bixby, McZeal, Ceria, and Savelsbergh [24] in 1996, and the compilation of miplib 2003 by Achterberg, Koch, and Martin [3], we have finally arrived at miplib 2010. The motivation for this update is the same as in the previous versions: the continuous progress in the field of mixed integer programming.

A mixed integer (linear) program (MIP) is an optimization problem in which a linear objective function is minimized subject to linear constraints over real- and integer-valued variables. For details on mixed integer programming, see, e. g., 69, 106. The miplib is a diverse collection of challenging real-world MIP instances from various academic and industrial applications suited for benchmarking and testing of MIP solution algorithms.

In this paper, we provide a detailed description of the instances in mIPLIB 2010, including their origin, information on the coefficient matrices, and the types of constraints and variables they contain. The complete library is available online at http://miplib.zib.de, where we have collected further information, such as references to papers that have used the miplib as a test set for their algorithms. If available, we also provide a problem description in an algebraic modeling language, such as ampl [57] or ZIMPL [70]. In addition to the role of miplib as a test suite for integer programming algorithms, we strongly encourage investigation of alternative models for the given problems.
miplib classifies instances into three categories: easy for those that can be solved within an hour on a contemporary PC with a state-of-the-art solver, hard for those that are solvable but take a longer time or require specialized algorithms, and finally open instances for which the optimal solution is not known. This classification is kept up-to-date on the website, and we ask for notification whenever an optimal solution is determined for an open instance. The website also contains details if specific settings have been used to solve an instance.


Fig. 1: Number of miplib 2003 instances classified as easy, hard, and open over time

The progress in solving real-world mip instances has been exceptional over the last decades. It is recorded in various articles [22,72,77] and numerous talks. One example is the solvability of the miplib 2003 instances. As shown in Figure 1, at the start of miplib 2003 there were 22 easy, three
hard, and 35 open instances. By the end of 2010, 41 were classified as easy, 15 as hard, and only four open instances remained.

Another showcase is the speedup of commercial MIP solvers. Figure 2 depicts the progress made by two of the commercial solver vendors with long traditions, cplex and xpress. These figures are based on their internal test sets and record purely the speedup due to algorithmic improvements. For cPlex the geometric mean of the speedup is drawn and for xpress the reduction in total solution time. Though these measures cannot be compared directly, they both show the impressive performance improvements gained during the last years.

Combining a pure algorithmic speedup of 55,000 with the speedup in computing machinery, we see that solving miPs has become something like 100 million times faster in the last 20 years. This easily translates into the difference between considering an instance to be trivial versus unsolvable.


1991199319951997199920012003200520072009
(a) Geometric mean speedup and number of instances solved by CPLEX versions 1.2 to 12.2 for an internal test set of 1,852 instances.

(b) Total solution time and number of instances solved by XPRESS versions 2003 B to 7.1 for an internal test set of 329 instances.

Fig. 2: Performance improvements of Cplex and xpress

This might give the misleading impression that all mixed integer programs are easy to solve nowadays. However, keep in mind that practitioners often experiment with tractable instances. In this sense, mip codes tend to be tuned to more efficiently solve those models that are already known to be solvable. In order to compensate for this, we added a large set of instances to miplib 2010 that are out-of-scope for today's solvers. As of this writing, the 361 instances of miplib 2010 are classified as follows: 185 easy, 42 hard, and 134 open.

## 2 The test sets

During the initial discussions among the authors, it became evident that a single test set that also includes many very hard or even unsolved instances was not going to be sufficient. Researchers have often focused their attention on subsets of the miplib 2003 instances that were suited to their particular topic of study. This often resulted in inadequate test sets because the full library only contained 60 instances, and added restrictions further reduced this size.

Therefore, we identified several areas for which dedicated test sets should be made available. Please note that a particular instance can be part of more than one test set. Table 1 gives an overview of all test sets.

Table 1: Overview of different test sets and the number of instances contained in each of them

```
B BENCHMARK (87 instances)
    contains only instances that can be solved to optimality by at least one solver within two hours on a high-end PC.
    Except for the test sets challenge and unstable, at least one instance from each of the other test sets is included
    in this one
    I infeasible (20 instances)
    contains instances that are infeasible.
\(P\) PRIMAL (40 instances)
    contains instances for which the solution of the root LP relaxation has the same objective value as the optimal
    solution, i. e., the solver "only" has to find an optimal solution; the proof of optimality comes for free.
X xxl (11 instances)
    contains very large instances with respect to the number of variables, constraints, and non-zeros.
R REOPTIMIZE ( 66 instances)
    contains instances for which the reoptimization of the sub-LPs takes an unusually long time.
T TREE (52 instances)
    contains instances that (empirically) lead to large enumeration trees.
\(U\) Unstable (21 instances)
    contains instances that have bad numerical properties and are likely to cause numerical troubles in the solver. This
    set is intended to test solver robustness.
C Challenge (164 instances)
    is a compilation of hard-to-solve instances as well as instances that to our knowledge have not been solved to
    optimality. There are 21 instances in this set for which we have not yet been able to compute any feasible solution.
    Some of these may of course be infeasible.
```

2.1 What are the sources of the instances?

We started a call for instances on March 26, 2010. Submission was closed in October 2010. In total we received over 1,108 instances from 57 contributors. Thanks to all of them! All contributed instances, unchanged, can be found at the miplib homepage ${ }^{1}$. Additionally, we had access to a large number of instances from the NEOS server. Problems submitted to the solvers SCIP, FEASPUMP, QSOPT_EX in various formats were translated to MPS format. For problems originally stated as AMPL model files, these files are preserved on the miplib website.

Finally, we collected publicly available instances from the internet including instances available from the Berkeley Computational Optimization Lab [108, the Computational Optimization Research at Lehigh test set (COR@L) [109, and the DEIS - Operations Research Group Library of Instances [111. Table 2 shows the distribution of instances according to their origin.

### 2.2 How were the instances selected?

In the following sections, we often mention that instances can be solved within certain time limits. Unless mentioned otherwise, this refers to experiments that were performed on dual core Intel Xeon E5420 2.5 GHz computers with 4 mb cache and 16 GB of main memory, running Linux in 64 bit mode.

After the submission of contributed instances was closed and the data mining of the public domain was finished, the initial candidate set contained about 2,000 instances.

Exclusion of trivial instances and (near) duplicates. In a first filtering step, duplicates were eliminated, homogeneous problem subsets were reduced, and instances which were too easy, i.e., could be solved by either SCIP or CBC in less than one minute, were removed. The typical case for homogeneous test sets was that many variations of the same model with different data were submitted. When comprising these sets of similar problems, we tried to keep the variety while reducing the set to less than ten instances.
1 http://miplib.zib.de/contrib/submission2010

Table 2: Origin of instances

| MIPLIB | 2 |
| :--- | ---: |
| MIPLIB 3 (excluding those from MIPLIB) | 7 |
| MIPLIB 2003 (excluding those from MIPLIB 3) | 17 |
| other publicly available | 180 |
| new contributions | 155 |

Examination and pre-selection by eight groups. The 659 remaining instances were examined independently by eight teams formed by the authors. Two instances entered the final test sets on short notice, as it was realized that certain classes of problems were not well represented in the candidate set. These were unitcal_7, a unit commitment model, and cov1075, a highly symmetric problem. Except for these two, all instances contained in the final test sets were part of this list of 659.

After the responses from the different groups had been evaluated, a first proposal of 100 instances plus 45 potential substitutes for the Benchmark set was compiled and circulated again. The minimal requirements for the benchmark set were that first every instance could be solved to proven optimality within 24 hours by at least one solver and second that each of the other test sets except the unstable and the challenge set, were represented in the benchmark set by at least one instance.

Final refinement of the benchmark set. Starting from this proposal, several instances had to be exchanged or eliminated for one of the following reasons:

- problem classes were over- or underrepresented,
- instances proved to be too easy or too hard when checking them on different machines with the current developer versions of the involved software, or
- instances were discovered to be numerically difficult.

In cases where we had to choose between two instances, newly contributed ones were favored and instances for which the application was unknown, e. g., instances that have been provided via the neos server, were disfavored. Also, instances that showed a stable performance (see also Section 5) were favored. Finally, we tried to keep the overall running time of the benchmark set reasonable.

It was far easier to exclude instances for the reasons named above than to include new ones that fulfilled all hard and soft requirements. We are satisfied to have arrived at a final benchmark set with 87 instances. We believe that this test set is well-suited for benchmarking purposes: nearly all instances can be solved in less than one hour by at least one solver, but only a few of them can be solved within less than a minute by any current solver.

Most of the other test sets were created by predefined rules rather than dynamically, as with the benchmark set. Because many criteria at least partially depend on the computational environment, e. g., number of simplex iterations, the numbers listed in the following paragraphs are only guiding values. The different test sets were double checked with different software packages on different machines to minimize the risk that some instance entered a particular test set just by chance.

The reoptimize test set. Warm-starting the simplex algorithm is one of the key requirements for efficiency in LP-based branch-and-bound algorithms. Often, reoptimizing an lP after changing a bound can be done in less than ten simplex iterations, whereas the initial Lp solve takes thousands of iterations. However, there are a few cases when this advantage of the simplex vanishes. The reoptimize set is a collection of them. It contains instances for which LP reoptimization takes at least 500 simplex iterations on average. This does not include simplex iterations that have been performed at the root node. Furthermore, instances were only included if they required at least 100 nodes to solve.

The tree test set. In the development of mip solvers, many algorithmic improvements aim at reducing the size of the branch-and-bound tree. As a consequence, MIP solvers are often able to solve instances to proven optimality in the root node or after only a few hundred nodes. The test set tree, however, comprises instances for which state-of-the-art MIP solvers perform a large amount of enumeration. The criterion applied for this test set was that the branch-and-bound tree created when solving the instance contains at least $1,000,000$ nodes.

The xxl test set. Predicting the performance of a miP solver just by knowing the dimensions of an instance is impossible. The markshare examples [1] show that problems with 60 variables and 6 constraints may be extremely hard to solve for state-of-the-art software packages. On the other hand, there are instances that contain 100,000 or more variables that can be solved in less than a minute. The test set xxl is dedicated to mips that are large-scale, but not too easy. It consists of problems with either more than a million variables, more than a million constraints, or more than 10 million non-zeros. Instances for which the majority of the variables and constraints can be eliminated by standard presolving methods were not considered.

The primal and infeasible test sets. A typical experience in solving a mip is that finding an optimal solution is often much easier than proving its optimality. The test set PRIMAL is set up for instances for which the reverse holds. We included problems for which the bound given by the initial LP relaxation after presolving is equal to the MIP optimum. The only thing left for the solver to do is to find an optimal solution - the proof of optimality comes for free. We only included instances for which this appeared to be challenging.

Most MIP solvers are tuned for optimization problems, typically not for feasibility problems, such as the primal instances, and to our knowledge not at all for infeasible problems. The test set infeasible should help to investigate the behavior of mip solvers for this kind of problem setting.

The challenge and unstable test sets. The new submissions contained several instances that are currently rather hard to solve. The challenge set contains problems that we could not solve in less than two hours with any of the solvers. For some of them, the optimal solution is known; for many, it is not. As of this writing, no feasible solution is known, if one exists, for 21 of these instances.

Finally, we compiled the numerics test set unstable. mips are identified as numerically unstable if they exhibit some of the following properties: ill-conditioned basis matrices, large coefficients close to the internal numerical infinity values of the solvers, drastic performance changes with different choices of numerical tolerances, or different results reported by different solvers. See also the Paragraph 'Condition numbers and numerical reliability' on Page 16.

## 3 The solution checker

Together with the miplib, a consistency checker is provided to validate the answers produced by floating-point based mip solvers. It tries to recognize incorrect results, while, to a certain extent taking into account the different feasibility policies of the codes.

### 3.1 Floating-point arithmetic and tolerances

Most mip solvers (in particular, all codes considered in this paper) are based on floating-point arithmetic and work with tolerances to check solutions for feasibility and to decide on optimality. In their feasibility tests, solvers typically consider absolute tolerances for the integrality constraints and relative ones for linear constraints. Some normalize the activity of linear constraints individually, others directly scale the constraint matrix.

The tolerances affect solution times and solution accuracy, normally in opposite ways, and the solvers apply different strategies here. As an example, consider the instance rocll-4-11. Some solvers compute an optimal objective function value of -6.6556387 , while others report -6.65275574 . If one fixes all integer variables from the reported solution to the closest integer value and recomputes the continuous variables by solving the resulting LP with exact arithmetic, some of these post-processed solutions turn out to be infeasible with respect to exact arithmetic and zero tolerances.

It should be clear that this does not mean that any of the solvers made a mistake. It only means that the computed solution lies outside the feasible area described by the input file, but inside the extended feasible area created by reading in the problem and introducing tolerances. It is only solutions that are feasible in the latter sense that solvers attempt to deliver, and those are the solutions the checker checks. More precisely, the operation that rounds the reported value of the integer variables to the closest integer is only applied to compute fully reliable primal bounds for the mips as described in the paragraph 'miP and lp solution values' in Section 6 .

### 3.2 What do MIP solvers actually try to solve?

A binary double-precision number is represented in the form

$$
(-1)^{s i g n} \cdot\left(1+\sum_{i=1}^{52} 2^{-i} b_{i}\right) \cdot 2^{e}
$$

where sign is a single bit indicating the sign, $b_{i}$ are 52 binary digits used to represent the significant figures of the number $i$ digits after the first binary digit and $e$ defines the exponent, taking integer values in $e \in[-1022,1023]$. The IEEE [117] standard defines which results should be returned by the basic arithmetic operations in order to maintain consistent behavior across different platforms.

Floating-point computations can be performed quickly on computers but the limited size of this representation has its disadvantages. The error incurred by a single operation is usually small but algorithms requiring many operations can accumulate and propagate these small errors, leading to errors of significant magnitude. A survey of the issues that can arise in floating-point computation can be found in [60]. mIP solvers implement techniques to handle these issues. We now discuss those techniques relevant to the solution checker for that phase of the process that precedes the actual solution of the problem.

The mps file format which is used as a standard to define MIP instances requires the input numbers to be written in base 10 ASCII representation. Furthermore, the definition of the MPS file format specifies that each entry uses only 12 characters, so if a problem cannot be expressed exactly in this format, even the input file will be an approximation of the intended problem. Suppose a problem is defined in an MPS file as having the feasible region

$$
\left\{x: A x \leq b, x \geq 0, x \in \mathbb{Z}^{n}\right\} .
$$

As this problem is read in by the solver, the entries in $A, b$ will be transformed to a binary representation, possibly modifying their values and changing the feasible region to $\left\{x: \widetilde{A} x \leq \widetilde{b}, x \geq 0, x \in \mathbb{Z}^{n}\right\}$.

In addition, due to inexact floating-point computation, the solvers need to introduce tolerances, hence relaxing (introducing a perturbation of) the feasible region. Typically relative tolerances are used. In order to do this efficiently and to improve the numerical properties of the model, the constraint matrix is usually scaled. As a result, solvers operate on something similar to

$$
\left\{x:(\widetilde{Q \widetilde{A}}) x \leq \widetilde{Q \widetilde{b}}+\mathbf{1} \varepsilon, x \geq-\mathbf{1} \varepsilon, x \in(\mathbb{Z}+[-\delta, \delta])^{n}\right\}
$$

where $\varepsilon$ and $\delta$ are tolerances for feasibility and integrality and $\mathbf{1}$ is the vector of all ones. As we can see, even the steps of parsing and scaling the problem can change its description. The entire solution procedure is then applied to this transformed problem.

Note that we have not even mentioned other preprocessing techniques that are applied by the solver in order to simplify the problem, such as removing redundant constraints and variables, tightening bounds and coefficients, or aggregating variables. All of this may lead to further modifications of the problem before the branch-and-bound and cutting plane phases are actually started.

In this regard, it is important to note that even though an instance is infeasible, it can become feasible by the extension of the feasible area due to the tolerances. This is one of the reasons why the solution checker does not try to test optimality and infeasibility but makes all tests by using solutions as returned by the solvers and with respect to the tolerances. Some different practice-oriented tests performed outside the checker are described in Section 4.

### 3.3 What does the solution checker test?

Given a linear programming problem, the combinatorial nature of the bases provides an efficient way to check both the optimality and the feasibility of a given solution: this is not the case for mixed integer programming problems. In the MIP setting, we cannot expect polynomially sized certificates of optimality to exist in general (assuming $\mathcal{P} \neq \mathcal{N} \mathcal{P}$ ). However, it is possible to check the feasibility of a given solution in polynomial time and this is exactly the goal of our solution checker. Although conceptually simple, the implementation of such a checker still poses some questions:

- In which kind of arithmetic should we perform our calculations?
- Should we take our data from the internal floating-point representation of a solver or should we use the original text-based one?
- What tolerances should we use?

Concerning the first two questions, we decided to perform all of our computation with an arbitrary precision arithmetic package, namely GMP [114], taking the problem specification from a text-based file. In particular, we decided to use the industry standard MPS format. Note that reading the input from the MPS file, we perform no risky or potentially unsafe simplification of the coefficients; for example, if the input file contains the coefficient 0.3333333 we do not try to infer the "nicer" rational representation $1 / 3$, but we stick to the original $3,333,333 / 10,000,000$. As far as the solution to check is concerned, in order to keep the solution checker independent of the particular solvers and the language in which they are implemented, we decided also to read the solution from a text-based input file, whose very simple format is described in the miplib package.

The solution checker performs two tests: a feasibility test of the computed solution and a consistency check of the corresponding objective value. For the feasibility test, we followed the common habit of using two, possibly different, absolute tolerances. One tolerance is used to check the satisfaction of linear constraints, including bounds on the variables, and the other tolerance is used to check integrality constraints. For its default settings, the code uses an absolute tolerance of $10^{-4}$ for both cases.

In addition to the solution computed by the solver, the solution file contains the computed objective value. Checking its precision is conceptually trivial, at least for pure integer programming problems. However, given the potentially large absolute value of the objective function coefficients, sometimes larger than $10^{10}$, it quickly becomes a delicate matter, if one insists on using only absolute tolerances. Therefore, the checker accepts the objective value if the absolute value of the difference between the objective value computed by the checker and that read from the input file is less than $10^{-4}$ or if the relative error, i. e., the absolute error divided by the maximum of the absolute value of the checker's result and 1 , is less than $10^{-7}$.

Finally, the solution checker reports the maximum violation of the linear and integrality constraints and the absolute value of the difference between the solver's and checker's objective values.

4 How to run a test, add a solver, and what the scripts do
For the first time, miplib comes with a test engine to run different solvers in a defined way, to check the answers for consistency, and to generate a table summarizing the results. In this section, we briefly explain how this engine works, enabling users to incorporate new solvers, and to adjust the scripts to their needs.

In order to allow meaningful benchmarks, the test engine runs each solver in deterministic mode ${ }^{2}$ if possible and applies comparable termination criteria, i. e., the relative gap cutoff is set to 0 . Concerning the performance evaluation, the wall-clock time is measured externally and solution times are reported rounded up to the second. This means the time for parsing the input file and creating the model is included. The primal-dual gap at termination is computed, assuming minimization, as

$$
\text { gap }=\frac{p b-d b}{\inf \{|z|, z \in[d b, p b]\}}
$$

where $p b$ and $d b$ are primal bound and dual bound, respectively. In case either no feasible solution was found, the problem was reported as infeasible, or $d b \leq 0 \leq p b$, the gap is not computed and is marked as "--". In case $d b=p b=0$ a gap of 0 is reported. We chose this gap calculation since it is monotonically decreasing if the dual bound increases and the primal bound decreases. Moreover, this measure gives a worst case bound on the relative gap normalized by the optimal solution value.

The resulting table presents for each instance the name, the primal and dual bound along with the gap at termination, the number of branch-and-bound nodes, and the solution time. Additionally, the status of the mip solver and the result of the solution check are displayed. The solver status is ok for instances where the solver claims optimality, stopped if the solving process was stopped due to imposed limits, and abort otherwise, e. g., for termination due to errors in the mip solver. Each solver is expected to write the best solution found into a solution file. If a solution file was generated, the solution gets checked and the solution status is ok or fail depending on whether or not the solution passed all tests of the solution checker (see Section 33). In case no solution was found, e. g., for infeasible problems, we report "--" as the solution status.

Optionally, a file with known primal bounds can be given. If such a file is provided and only after the solution passed the tests of the solution checker, the primal bound reported by the solver will be compared with the value given in the file. If a finite primal bound is stated in the file and the solver reports either infeasibility or an optimal solution with a significantly worse objective value, the solution status is set to mismatch. In case the solution file reports infeasibility, but the solver returns a solution within the tolerances of the solution checker, no mismatch is reported. Finally, if the solution checker code encountered internal problems, the solution status is set to error.

It is important to note that the comparison with respect to a primal solution from a file is independent of the solution checker, and requires a primal bound that is fully reliable. Here we computed the primal bounds by rounding the integer variables to the closest integer and then used exact arithmetic for solving the resulting LPS as described in Paragraph 'miP and LP solution values' of Section 6

At the end, we state how many instances were solved to optimality and passed the solution tests (solved), the number of failed instances (solution process was aborted or solution test failed), and the remaining number of stopped instances.

We now briefly sketch how the test engine is organized. The engine assumes a Linux environment, adoption to other UNIX-like operating systems should be possible with minor modifications. The main folder contains the files "Makefile" and "README" and the folders "bin", "checker", "instances", "scripts", and "testsets". After running the first automated test, there will be a folder named "results".

[^2]The "Makefile" provides all the functionality of the test engine and the "README" is an introduction to the environment. The folder "bin" should contain the solver binaries or a (soft) link to them. The environment will check this folder for the requested solver binary. The sources for the solution checker, mentioned in Section 33 are stored in the folder "checker". The solution checker can be compiled via the provided "Makefile" of the test engine using the command make checker. All miplib 2010 instances are stored in "instances". The folder "testsets" includes, for each test set described in Section 2, a file with the location of its instances, and for the benchmark set a file with known primal bounds that are believed to be optimal. Log files and solution files of test runs and corresponding tables will be stored in a folder called "results" and all relevant scripts can be found in the folder "scripts".

The complete evaluation process is triggered by the test target in "Makefile". For example,

```
make SOLVER=xyz TEST=benchmark TIME=3600 test
```

runs solver XYZ on the benchmark test set with a time limit of one hour. More precisely, in this way, the main driver "run.sh" is invoked. It calls the MIP solver for every instance listed in the file "benchmark.test", asks for the best solution, and applies the solution checker. However, the solver-specific part, such as setting the time limit and getting the solution, is encapsulated in a separate script "run_xyz.sh". After running the solver, "run.sh" starts "parse.awk", which parses the generated log file and produces the summary table. The evaluation, including primal-dual gap computation, time measurements, and determination of the solution status, is standardized and directly implemented in "parse.awk", whereas the information from the solver-specific log files, e. g., dual bound and node count, is actually obtained via auxiliary scripts such as "parse_xyz.awk".

Currently, we support CbC, CPLEX, GUROBI, MOSEK, SCIP, and XPress. In order to include other miP solvers, only the solver-specific information for running the solver and evaluating its log files have to be provided by "run_mysolver.sh" and "parse_mysolver.awk". The template files "parse_xyz.awk" and "run_xyz.sh" can be used as a basis. They are located in the "scripts" folder. In order to test instances that are not shipped with miplib 2010 a file "mytestset.test" with their locations has to be added to the "testsets" folder.

## 5 Variability of MIP Solver performance

When running computational experiments, we often experience differences in behavior on different platforms when optimizing the same model with the same solver. The input format, e.g., the order of the constraints, can also change the solution process. We use the term performance variability 42 to denote such changes in performance measures for the same problem that are caused by seemingly performance-neutral changes in the environment or the input format. Loosely speaking, performance variability comprises unexpected changes in performance.

Note that other changes, such as minor variations in the model formulation, also affect performance in a way that is difficult to predict. Adding or removing redundant constraints or variable bounds can have a major impact on the performance of modern miP solvers [4]. Some of these changes are also automatically applied by preprocessing, in which case their effects are compounded with other sources of variability.

### 5.1 Reasons for performance variability

One root cause of performance variability is imperfect tie-breaking. When solving a MIP, most decisions are taken by computing a score for several candidates and choosing the candidate with the highest score. For example, a score based on pseudocosts may be computed for several variables that are candidates for branching and the variable with the highest score is chosen [20]. If there
is a tie among the top candidates, then a series of secondary criteria should be used to make the final decision [2]. If tie-breaking is imperfect, selections may be made arbitrarily, based on the order in which the candidates are considered or influenced by rounding errors in the score computation, which will differ from platform to platform. Similarly, some decisions consider a subset of candidates: for example, strong branching [76] is typically applied to the top $N$ branching variable candidates according to some criterion. If there are more than $N$ candidates tied for the best score, then the order in which candidates are considered will determine the variables for which strong branching is performed. Another factor is that compiler optimizations may reorder arithmetic operations and influence the outcome of floating-point computations; this might introduce a tie-breaking effect for values that should be equal or it might lead to tied values that should not be the same. ${ }^{3}$

Once the path in the branch-and-cut tree diverges, the entire subsequent resolution is affected. Altering the choice of a single branching variable may cause entirely different subtrees to be explored; the LP solutions at the child nodes could be different, leading to different cuts and different starting points for primal heuristics, which in turn leads to different integer solutions being found, the objective cutoff being updated differently, different nodes being pruned, etc. As we see from such a cascade of events, even a small divergence may lead to a completely different behavior of the solver and hence to a significant performance difference.

Also, for many models, the optimal basis of the root LP is not unique. If the LP basis is different, then cuts and Lp-based primal heuristics applied at the nodes to find additional feasible solutions will be applied differently, and consequently the whole solution process will change. It is currently unknown whether the variability is correlated in any way with the number of alternate optimal LP bases for the root node.

Performance variability also depends on the intrinsic characteristics of the model; some structures may create more variability than others. It also depends on the characteristics of the miP solver; some solvers may have more robust tie-breaking mechanisms or more sophisticated algorithms to recover from a bad decision. Many questions are open. In particular, what is the importance of each factor to variability and how should we change MIP solvers and MIP models so as to reduce variability. It is not even clear whether performance variability should exclusively be seen as a disturbing factor. For massive parallel MIP solvers, see, e.g., 97, it can even be exploited.

### 5.2 Generating and measuring performance variability

In order to study performance variability, we need a way to generate a large number of observations for the same model. Clearly, it is neither sufficient nor practical to run experiments on many different computers. Previous studies [42] have shown that a good variability generator is to permute columns and rows in the original model. This generator affects all types of problems and all components of a typical MIP solver. For instances of practically relevant size, many different permutations can be applied to create as many observations as needed.

For comparison reasons, it is desirable to summarize the performance variability into one number per model and solver. We choose as the performance variability score the coefficient of variation of $X$, where $X$ is the random variable representing the performance of the given solver for the given model. For example, the performance can be measured as the solution time to optimality or the time to the first solution. The coefficient of variation is simply the standard deviation divided by the average: it captures the variations in performance and its normalization allows us to compare the variability independent of the computational difficulty of the model. This definition is quite natural and allows us to interpret the variability score in relationship with the probability of a given performance degradation.

[^3]In practice, the coefficient of variation is estimated on a sample of observations provided by solving multiple permutations of the model: the quality of the estimate increases with the number of permutations. Given $n$ permutations and corresponding running times $t_{i}, i=1, \ldots, n$, we compute the variability score $V S$ as follows:

$$
V S=\frac{1}{\sum_{i=1}^{n} t_{i}} \cdot \sqrt{\sum_{i=1}^{n}\left(t_{i}-\frac{\sum_{i=1}^{n} t_{i}}{n}\right)^{2}}
$$

In Column VS of Table 7 starting on Page 40 the performance variability score for time to optimality with SCIP/SPX is shown. It is sampled from 100 different permutations for each model. However, we calculated the score only for models that SCIP/SPX could solve in less than four hours, using the original formulation. In addition, we imposed a time limit of ten hours, which, of course, influences the variability score whenever a permutation hits this limit. In Table 7 those scores that are affected by the time limit are printed in italic.

We present variability for solution time rather than number of simplex iterations, as in 42], because time is easier to compare across solvers. Indeed, solvers may count iterations differently; for example, iterations in sub-mips may or may not be counted, which makes the comparison difficult. Besides, not all the work done in a MIP solver is based on the simplex algorithm, so counting iterations gives a less comprehensive picture than measuring time.

Note that the variability score is an estimator over a limited sample of the true variability. Therefore, small differences in variability scores should not be given too much consideration.

### 5.3 Results on performance variability

Performance variability due to permutations can be observed for all tested instances. There was no instance for which all 100 permutations showed the same behavior. The minimum observed impact was for the instance mik-250-1-100-1, where the ratio of the maximal and the minimal solution times was 1.29 . The largest ratio was 915 for the instance tanglegram 2 ; the fastest permutation took a few seconds, the slowest nearly two hours.

The total running time of all 67 original, unpermuted instances for which we performed this test was 45.1 hours. If we had an oracle that, hypothetically, always selected the best permutation for each individual instance, the total running time would be reduced to 25.5 hours, which corresponds to a speedup factor of 1.77 . On the other hand, always using the worst permutation would increase the running time by a factor of 3.82 . This indicates that the negative outliers are more "extreme", i. e., the distribution is not symmetric.

It seems to be a natural question whether the original formulation has an advantage over the permuted ones. Indeed, if we compare the solution time of the unpermuted instances to the average solution time taken over the 100 permutations, we observe a speedup of $14 \%$. There is evidence that this might be mainly due to the more extreme behavior of negative outliers. If we compare the performance of the original formulations to the median, this advantage shrinks to $4 \%$ improvement. Said differently, the probability of improving performance by permuting the instance is about as high as the probability to deteriorate performance, but the average improvement is smaller than the average deterioration.

Overall, the range of variability scores is between 0.05 for the instance mik-250-1-100-1 and 2.23 for neos-916792, as can be seen in Column VS of Table 7. Figures 3a to 3e show the distribution of performance for specific instances. For the instances ex9, pg5_34, neos13, bnatt350, and enlight13, each of the dots in the corresponding diagram depicts the performance of one permutation when being solved with SCIP/SPX. They have been sorted by non-decreasing solution time; the black dot corresponds to the performance of the original formulation.

In Figure 3a, the vast majority of the permuted instances perform very similar, with only a few outliers. The original formulation is superior to the others. The most common case, however, is illustrated in Figure 3b. The different solution times are nearly uniformly distributed around the median value. There are a few negative outliers. The original formulation is "somewhere in the middle". Figure 3 c shows the interesting case of clusters. Most of the permutations need around 12 minutes, but there is a significant accumulation point at 1:40 h. In order to have a smaller scale to make the accumulation point better visible in the picture, all permutations that took three hours or longer are treated as if they hit a time limit of three hours. Figures 3d and 3e depict bad cases for which permuting the model can lead to nearly arbitrary changes in the performance. For the instance enlight13, the best ten permutations need less than three minutes, but nearly twenty percent hit the time limit of ten hours.

Another source of variability is depicted in Figure 4 which shows the performance variability of a single instance depending on the number of threads. The computations where done on a 32 core machine with 8 AMD Opteron 8384 processors at 2.7 GHz . As can be seen, both performance measures go up and down quite arbitrary with no visible pattern. If we compare neighboring bars, we see that adding one additional thread leads to fewer evaluated nodes in 17 cases, in 14 cases it results in more search nodes. The same holds for the solution time: in 14 cases the solver got faster when using one more thread, in 17 cases it slowed down.

### 5.4 Consequences for benchmarking

Performance variability affects all standard objectives of benchmarking, such as comparing different solvers, comparing different parameter settings for the same solver, or comparing a new algorithm to an existing algorithm. In particular, it is important to take performance variability into account during the analysis of experimental results when the performance difference is small, the variability of the models is high, or the stopping criterion is highly variable. Small test sets are more prone to disturbances caused by performance variability. This is one reason why miplib 2010 provides more instances than its predecessors.

Performance is not deterministic. Instead, it is a random variable that can be sampled with computational experiments. In order to isolate the signal from the noise and draw robust conclusions, performance needs to be studied with appropriate statistical tools. First, it is useful to obtain a large data sample, by running experiments on a large set of models or by artificially multiplying the number of observations by running experiments on permuted models for multiple permutations. Secondly, descriptive statistics such as the average or the geometric mean give limited insights. Instead, robust indicators such as truncated averages and rank statistics are more resistant to outliers. Performance profiles [47] are also useful. Finally, inferential statistics, such as statistical tests and confidence intervals, give the most insight and allow questions such as "how likely is it that the performance change is created by variability rather than by genuine algorithmic changes?" to be answered.

Variability should be taken into account not only when studying performance, but also when studying the correctness of computation. A different path in the branch-and-cut tree often leads the MIP solver to find a different integral solution because most models have several alternate optimal solutions. In all cases, the integral solution returned should have the expected objective value and respect all tolerances. It is a good idea to verify this on several permutations of the same model.

## 6 The instance catalog

In this section, we give an overview of all miplib 2010 instances. Table 5 on Page 25 provides information about their origin and application. For each instance, we list originators or submitters,


Fig. 3: Solution times for 100 permutations


Fig. 4: Example of performance variability depending on the number of threads. Instance rolli3000 on a 32 core computer. Filled bar indicates minimum
a short description of the application and references to publications in which the instance was used. Additionally, there are a large number of instances from NEOS and COR@L for which, unfortunately, no information is available to us. Instances with the same originator and application are grouped in one row. The 26 instances from previous versions of mIPLIB are marked by italic names.

Problem statistics. Table 6 starting on Page 32 gives statistics about the instances. In particular, for each instance, we give the number of Rows, Columns, and Non-Zeros. Furthermore, the number of variables is divided into the number of Binary, general Integer, and Continuous variables. Table 3 shows a distribution of instances based upon variables types. Only 13 instances do not have any binary variables, while only 72 of 361 instances have general integer variables.

Table 3: Distribution of instances based upon variable types

| Type | Binary | Integer | Continuous | Instances |
| :--- | :---: | :---: | ---: | ---: |
| Binary Programs | X |  |  | 116 |
| Integer Programs |  | X |  | 1 |
|  | X | X |  | 29 |
| Mixed Integer Programs | X |  | $X$ | 173 |
|  |  | X | X | 12 |
|  | X | X | X | 30 |

MIP and LP solution values. If known, the objective values of an optimal mIP Solution and the LP relaxation (LP Solution) are listed. The rational LP solver QSOPT_EX [12,52,123 was used to solve the Lp relaxation of the instances with exact arithmetic. We report up to 16 digits, last digit rounded, in the table. For those instances that could not be solved by qSopt_ex within a reasonable amount of time, we print the optimal solution value of the LP relaxation reported by CPLEX in italic. Note that we used the pure LP relaxation without applying MIP presolving, so the root LP bound computed during MIP solution might be better, even before cutting planes are added.

Although first steps have been taken in developing exact miP solvers [12,38, current implementations are not yet capable of computing provably optimal solutions for most of the instances
in miplib 2010. Therefore, we post-processed the mip solutions generated by the inexact solvers. The solution values of all integer variables were rounded and fixed to the nearest integer. The remaining LP was solved with QSOPT_Ex. This does not give an optimality proof, but can provide a mip solution that is truly feasible. Again, if this LP could not be solved by QSOPt_Ex, we state in italic the objective value of an inexact optimal solution that passed the test of the solution checker. Instances where no optimal MIP solution is known, i.e., open instances, are labeled with a question mark '?'.

For the instances in the challenge set, we invested limited time to try to solve them with one of the available solvers. Four instances, $50 \mathrm{v}-10$, probportfolio, reblock354, and rmatr200-p20, could be solved by UG[SCIP/SPX] 97, a distributed massively parallel version of SCIP run on 2,000 cores at the HLRN-II super computer facility. To finally solve reblock354 about 42 billion nodes had to be processed. This took approximately 36 CPU years.

Condition numbers and numerical reliability. Column Att.-Level lists the numerical attention level calculated using the set mip strategy kappastats 2 command of CPlex 12.2.0.2. This gathers statistics about the condition numbers of sub-problem basis matrices during CPLEX's solution process and is explained below in more detail. Vaguely speaking, a higher attention level indicates larger condition numbers of LP basis matrices, which in turn points to a higher probability of numerical instabilities during the solution process. A node limit of 1,000 and a time limit of two days was used to get a reliable data base for this computation. Those few instances that did not finish the root node within this time limit, are marked by "-", for those instances with attention level 0.0, the value is omitted.

The condition number $\kappa\left(A_{B}\right)$ is a well-known measure of how errors in the input of a linear system of equations $A_{B} x=b$ are propagated to the solution $x$; for further details see, e.g., 62. The condition numbers $\kappa\left(A_{B}\right)$ of the basis matrices $A_{B}$ that are used to calculate optimal solutions of the sub-problem lP relaxations provide some insight into the origin of potential numerical inaccuracies that may have arisen during the solution process.

Double-precision arithmetic, as employed in the solvers at hand, provides roughly 16 significant decimal digits. Given that we used a feasibility tolerance of $10^{-6}$, condition numbers larger than $10^{10}$ suggest that the errors encountered when calculating optimal LP solutions of the sub-problems may be larger than the feasibility tolerance. CPLEX classifies the condition numbers by the following four categories and outputs a histogram of the condition number distribution of optimal LP bases encountered during the MIP search:

- stable if $\kappa\left(A_{B}\right)<10^{7}$,
- suspicious if $\kappa\left(A_{B}\right) \in\left[10^{7}, 10^{10}\right)$,
- unstable if $\kappa\left(A_{B}\right) \in\left[10^{10}, 10^{14}\right)$, and
- ill-posed if $\kappa\left(A_{B}\right) \geq 10^{14}$.

The attention level $A L \in[0,1]$ summarizes this histogram as

$$
A L=p_{\text {ill-posed }}+0.3 \cdot p_{\text {unstable }}+0.01 \cdot p_{\text {suspicious }}
$$

with $p$... being the relative frequencies of the sampled condition number categories. Thus, the attention level provides an estimate of the probability that the solver has encountered numerical issues during the solution process and their severity.

The attention level is not a property inherent to the model, but a measure for a specific algorithm applied to a certain instance and will even vary for one solver when different parameter settings are used. Since all solvers tested are based on the same paradigm of branch-and-bound-and-cut, we still believe that the attention level is a measure that can be of use in predicting numerical difficulties during the solution of an instance, though by no means the only one.

Category and status. The last two columns denote the test sets in which an instance is contained by giving the first letter of Benchmark, Challenge, Infeasible, Primal, Unstable, Resolve, Tree, XxL, as well as the status of the instance as of this writing, i.e., easy (solvable within one hour), hard (solvable in a longer time or with a specialized algorithm), or open (optimal solution unknown).

Size, structure and sparsity. The coefficient matrices vary largely in size and proportion. Figure 5 shows their distribution according to number of rows and columns. It can be seen that instances with more columns than rows are slightly in the majority (199 vs. 160 instances). Two instances, namely ramos3 and go19, have an equal number of columns and rows.


Fig. 5: Size distribution of instances in miplib 2010

Apart from all the randomness involved, the instances typically show a strong structure, see, e. g., [80]. To underline this, we provide pictures representing the non-zero distribution in the coefficient matrices on the miplib website. Figure 6 shows the sparsity patterns for instances cov1075 and triptim2.

Note that the structure shown in the pictures is intensified, i. e., the instances are usually sparser than they appear here. This is especially true for large instances where the ratio of zero to non-zero elements of the matrix is as small as $2.3 \cdot 10^{6}$ to one (for instance zib02). Only 11 instances show a density larger than $10 \%$ and the average density over all 361 instances is $1.6 \%$; see also Figure 5 a

## 7 State-of-the-art MIP solving

In this section, we try to provide a snapshot of the state-of-the art in mip solving as of March 2011. We emphasize that the goal of this section is not to compare the performance of the solvers, but rather to introduce the instances of the miplib 2010 test set. We hope to reveal characteristics of the problems and give an impression of what is possible with today's codes, giving a point of reference for future research and investigation.


Fig. 6: Two examples of sparsity patterns

All of the solvers are in continuous development, often experiencing significant improvements from release to release. After having assembled a preliminary version of the test sets between December 2010 and mid January 2011, each development group was asked to send the latest version of their code, even if it was not yet officially released. While it is relatively easy for CBC and SCIP to make new releases on short notice, the commercial vendors require more thorough testing. For GUROBI, we used the very latest beta and from XPRESS, the first release candidate. Both will be officially released soon. cPlex provided its most recent public version, which was released in January 2011. Table 4 lists the solvers used.

Table 4: Solvers used for the computations

| Solver | Version | Status | Website |
| :--- | :--- | :--- | :--- |
| CBC | 2.6 .4 R1630 | Release | http://projects.coin-or.org/Cbc |
| CPLEX | 12.2 .0 .2 | Release | http://www.cplex.com |
| GUROBI | 4.5 beta0 | Beta | http://www.gurobi.com |
| SCIP/SPX | $2.0 .1 .3 / 1.5 .0 .3$ | Internal Version | http://zibopt.zib.de |
| XPRESS | 7.2 RC | Release Candidate | http://www.fico.com/xpress |

We also investigated other solvers like GLPK [113] and LP_Solve [119, but since neither of them was able to solve more than $20 \%$ of the instances within the time limit and no multithreaded versions were available, we omitted the results. For a recent survey of mip software we refer to [75].

For computations in this section, a computer with two Intel Xeon X5680 cpus, each providing 6 cores at 3.33 GHz , was used. Hyperthreading and Turboboost were disabled. The machine has 32 gb ram. All computations were done using the benchmark test set.

Table 7, starting on Page 40, lists the results for computations using one thread with a time limit of one hour and a memory limit of 8 GB. The solvers are ordered by release date, commercial ones first, non-commercial ones in a second block. For each solver, the number of branch-and-bound nodes used and the wall clock time in seconds are listed. If the time limit was reached before the solver finished, the optimality gap is given instead. If the gap at termination is infinite, i.e., if no primal solution was found or if $0 \in[d b, p b]$ and $d b \neq p b$, we write inf\%. Italics indicate that the solution (as printed in the output file by the solver) did not pass the tolerances for the solution checker described in Section 3. If a solver aborted, we write abort across the columns for nodes and time. In the latter two cases, a footnote gives details, if available.

The column Best lists the minimum number of nodes and the best time taken over all solvers that solved the instance to optimality and provided a solution accepted by the solution checker. In this respect, minimum tree size and solution times may have been taken from different solvers. The column VS lists the variability score of the instance as described in Section 5 . Higher numbers indicate higher performance variability. In order to indicate special properties of the instances, the additional test sets containing an instance, other than benchmark, are listed in column Sets.

While each solver hits the time limit for at least 12 instances, there are only four benchmark instances that none of the solvers was capable of solving within one hour, using only one thread. These are iis-bupa-cov, m100n500k4r1, neos-1337307, and newdano. Furthermore, for each solver there is at least one instance for which this solver is faster than all the other solvers. The geometric mean of the times in the Best column actually is less than half of the geometric mean of the numbers in any of the solvers Time columns.

Table 8, starting on Page 43, gives the results for computations using 12 threads with a time limit of one hour and a memory limit of 24 GB . Except for the last column, we list the same numbers as for the single thread computations. The last column lists the speedup between the Best Time column from the single thread and from the 12 thread results.

Using 12 threads, all instances with the exception of m100n500k4r1 can be solved by at least one of the solvers within one hour. The speedup between the best of all solvers and any particular solver is now even more significant. The average overall speedup for going from 1 to 12 threads is approximately a factor of 3 . In some of the cases where the speedup is less than 1 this is due to rounding the time up to the second on instances which do not benefit from using multiple threads. This rounding is also the reason for the super linear speedup reported for binkar10_1.

We purposely refrained from directly comparing the individual solvers based on measures of average solution times. There are a number of reasons for this:

- As stated in Section 5, we would have to sample over a sufficient number of permuted instances to decrease the impact of performance variability.
When redoing the single thread computations on a $14 \%$ faster machine with a different memory/cache system, the speedup of the geometric mean solution time was between $8.5 \%$ and nearly $20 \%$, depending on the particular solver.
When redoing the 12 thread computations, even though the codes ran in deterministic mode on an empty machine, differences in wall clock time up to 73 seconds between two runs of the same instance could be observed.
- The result depends on several quite arbitrary choices, like the time limit, the number of threads, and the particular computer system. If we changed any of them, the results would change.
- The fact that each solver was the single fastest on some instances and only a few instances could not be solved by any solver, strongly indicates that if one wants to know which solver is the fastest for a particular problem, the only way to find out is to try them all.
- While the geometric mean of the solution times in the 12 thread setting for the commercial solvers is the same within measurement precision, the ratio between the slowest and the fastest of the three solvers can be over 1,000 on an individual instance. The geometric mean of this ratio is over 5 , and the median is more than 3 , i.e., for more than half of the instances the fastest solver is at least three times faster than the slowest one. (We are not giving precise numbers here because due to the time limit there are several possibilities for computing the numbers or lower bounds.)
- We were "only" using default settings. Each of the solvers has at least 50 parameters to tune it. This often allows considerable improvements in performance, especially on instances were a certain solver has difficulties.
- Finally, there are many performance measures that could be used to decide which solver is best, like lowest number of timeouts, highest number of fastest solves, minimum total time, lowest geometric mean of solution time, etc. Interestingly, regarding the commercial solvers, depending on the measure and the number of threads used, each solver wins at least once.


## 8 Final remarks

Since the first release of miplib, nearly 20 years ago, we have seen impressive advances in computational mixed integer programming. To support the ongoing progress, we have compiled miplib 2010 to help provide a basis for evaluating future developments and to stimulate continuing algorithmic improvements.

The common efforts of collecting, experimenting with, selecting, and categorizing relevant problem instances have proven to be very insightful. Getting everybody involved and agreeing on common limits and tolerances for testing already led to beneficial discussions, code improvements, and new ideas.

Last but not least, one important insight after literally spending decades of cpu time is that one should not try to boil down the result tables to a single number. We hope that our detailed computational experiments provide an accurate snapshot of the current state-of-the-art in mixed integer programming.

> To be continued...

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108. Berkeley Computational Optimization Lab - Data Sets. http://ieor.berkeley.edu/~atamturk/data/
109. COR@L MIP Instances. http://coral.ie.lehigh.edu/data-sets/mixed-integer-instances/.
110. Convex Optimization of Eternity II. http://www.convexoptimization.com/wikimization/index.php/ Dattorro_Convex_Optimization_of_Eternity_II
111. DEIS - Operations Research Group Library of Instances. http://www.or.deis.unibo.it/research_pages/ ORinstances/MIPs.html
112. Eternity II puzzle. http://www.eternityii.com
113. GNU linear programming toolkit version 4.45. http://www.gnu.org/software/glpk
114. GMP, GNU multiple precision arithmetic library. http://gmplib.org
115. Management of Inter-Warehouse-Logistics for Stochastic Demand. http://www.tu-chemnitz.de/mathematik/ discrete/projects/warehouse_trucks/index.html
116. ICC, Intel C++ compiler. http://software.intel.com/en-us/articles/intel-compilers/
117. IEEE standard 754-2008 for floating-point arithmetic, 2008.
118. Challenge Problems: Independent Sets in Graphs. http://www2.research.att.com/~njas/doc/graphs.html
119. lp_solve 5.5.2. http://lpsolve.sourceforge.net
120. MULTILSB: Multi-Item Lot-Sizing with Backlogging. http://personal.strath.ac.uk/kerem.akartunali/ research/multi-lsb/
121. NEOS Server for Optimization. http://www.neos-server.org
122. Pseudo-Boolean Competition 2010. http://www.cril.univ-artois.fr/PB10/
123. QSopt_ex. http://www.dii.uchile.cl/~daespino/ESolver_doc/main.html
124. IBM Ponder This - August 2008. http://domino.research.ibm.com/comm/wwwr_ponder.nsf/challenges/ August2008.html.
125. SNDlib. http://sndlib.zib.de
126. TSPLIB. http://comopt.ifi.uni-heidelberg.de/software/TSPLIB95/

Table 5: Descriptions and references for miplib instances. Instances coming from a previous version of miplib are listed in italic

| Name | Originator and description |
| :---: | :---: |
| 30n20b8 | E. Coughlan, M. Lübbecke, J. Schulz [40] <br> Multi-mode resource leveling with availability constraints; precedence and resource constrained scheduling problem |
| 30_70_45_095_100 | J. Walser 102103 Geographic radar station allocation |
| 50v-10 | S. Bisaillon Network loading instance |
| a1c1s1, b2c1s1 | M. Vyve, Y. Pochet 55 91. Lot sizing instances |
| acc-tight4, acc-tight5, acc-tight6 | J. Walser 83104 ACC basketball scheduling instances |
| aflow40b | T. Achterberg 89] <br> Arborescence flow problem on a graph with 40 nodes and edge density 0.9 |
| air04 | G. Astfalk $\qquad$ <br> Airline crew scheduling set partitioning problem |
| app1-2 | E. Danna <br> Undisclosed industrial application from Google |
| ash608gpia-3col | M. Pfetsch Infeasible and highly symmetric graph 3-coloring assignment formulation |
| atlanta-ip, msc98-ip | E-Plus, D. Bienstock, A. Bley, R. Wessäly [26] <br> Min-cost network dimensioning problems with a finite set of link capacities for each bidirected link, unsplittable shortest path routing, path restoration for single node failures, and routing path length restrictions |
| $\operatorname{atm} 20-100$ | M. Galati 59] <br> ATM cash management problem |
| bab1 | E. Swarat, L. Traverso, J. Buwaya <br> Integrated vehicle routing and crew scheduling of toll inspectors on German highways |
| bab3, bab5 | E. Swarat <br> Vehicle routing with profits and an integrated crew scheduling problem formulated by two coupled multi-commodity flow problems |
| beasleyC3, g200x740i, k16x240, mc11, p80×400b, p100×588b, r80×800 | F. Ortega, L. Wolsey [85] Fixed cost network flow problems |
| berlin_5_8_0, usAbbrv-8-25_70 | G. Klau 54 <br> Railway optimization problems |
| bg512142, dg012142 | A. Miller 85498 Multilevel lot-sizing instances |
| biella1, dc1c, dc1l, dolom1, nsr8k, siena1 | Double-Click SAS [54 [55] Crew scheduling instances |
| bienst2, binkar10_1 | H. Mittelmann Relaxed versions of problems bienst and binkar10 |
| bley_xl1 | A. Bley <br> Min-cost network dimensioning problem with finite sets of link capacities and unsplittable flow routing |
| blp-ar98, blp-ic97 | M. Lübbecke 3454 Railway line planning instances |
| bnatt350, bnatt400 | T. Akutsu (9] <br> Model to identify a singleton attractor in a Boolean network, applications in computational systems biology |

Table 5 continued

| Name | Originator and description |
| :---: | :---: |
| buildingenergy | K. Pruitt <br> Model to determine the minimum cost design and dispatch of a distributed generation system for a commercial building |
| cdma | S. Bisaillon 3G wireless multiplexing communication model |
| circ10-3 | [122] <br> Instance from the 2010 SAT conference pseudo-Boolean competition |
| co-100 | A. Werner 21 <br> Model from optical access network planning |
| $\begin{aligned} & \text { core2536-691, } \\ & \text { core4872-1529 } \end{aligned}$ | A. Caprara, M. Fischetti, P. Toth 35] <br> Set covering instances coming from Italian railway models |
| cov1075 | F. Margot [37 79] <br> Problem of selecting a minimum collection of 7 -subsets containing all 5 -subsets of a ground set of 10 elements. |
| csched007, csched008, csched010 | T. Yunes 107 <br> Cumulative scheduling problem instances |
| d10200, d20200, leo1, leo2 | COR@L test set 109 <br> Instances coming from the COR@L test set with unknown origin |
| dano3mip, danoint, newdano | D. Bienstock 65 Telecommunications applications |
| datt256 | J. Dattorro 43 110] Model to find solution to the "Eternity II" puzzle [112] |
| dfn-gwin-UUM, germany50-DBM, janos-us-DDM, nobel-eu-DBE, zib54-UUE | C. Raack 593 <br> Network design, link dimensioning models for problems in the SNDlib 84 125 |
| ds-big | R. Borndörfer 64] Bus driver duty scheduling problem |
| eil33-2, eilA101-2, eilB101 | J. Linderoth 74 126 <br> Set partitioning problem approximations for capacitated vehicle routing problem instances from TSPLIB |
| enlight9, enlight13, enlight14, enlight15, enlight16 | A. Zymolka <br> Model to solve instances of a combinatorial game "EnLight" |
| ex9, ex10 | I. Ober Formulations of Boolean SAT instances |
| ex1010-pi | 122. <br> Logic synthesis problem from the 2010 SAT conference pseudo-Boolean competition |
| f2000, hanoi5 | $122$ <br> Reformulated SAT instances from the 2010 SAT conference pseudo-Boolean competition |
| ger50_17_trans | C. Raack 27] <br> Multi-layer network design problem using a link-flow formulation over a path-flow formulation |
| germanrr | Q. Chen 109 <br> Model from a German railroad company |
| glass4 | I. Luzzi (78] Nesting instance |
| $\begin{aligned} & \text { gmu-35-40, gmu-35-50, } \\ & \text { gmut-75-50, gmut-77-40 } \end{aligned}$ | N. Konnyu Timber harvest scheduling models |
| go19 | R. Miyashiro, Y. Yano, M. Muramatsu [82] Instance of the maximum string problem in the Go board game: to find a position of stones that maximizes the number of live "strings" on the board |

## Table 5 continued

| Name | Originator and description |
| :--- | :--- |
| harp2 | M. Savelsbergh [24] <br>  <br> Unknown application |
| hawaiiv10-130 | U. van Dinter <br> Unit commitment model |
| ic97_potential | L. Peeters [88] <br>  <br> A model for cyclic railway timetable optimization |
| iis-100-0-cov, iis-bupa-cov, | M. Pfetsch [11 90] <br> iis-pima-cov |
| Set covering instances arising from irreducible infeasible subsystem covering problems |  |
| in | A. Fügenschuh <br> Packing of paths, multicommodity flow formulation |
| ivu06-big, ivu52, rvb-sub | S. Weider [32, 105] <br> Set partitioning instances resulting from a column generation algorithm used for duty <br> scheduling in public transportation |
|  |  |

lectsched-1, lectsched-1-obj, H. Schilly 95
lectsched-2, lectsched-3, University lecture scheduling instances
lectsched-4-obj

| liu | X. Liu [3] <br> Floorplan and placement problem in the physical design of VLSI circuits |
| :---: | :---: |
| lotsize | D. Gade, S. Küçükyavuz $\square$ Multi-item lot sizing with service level constraints |
| Irsa120 | M. Atlihan <br> Model to break a 120 bit RSA key |
| m100n500k4r1 | L. Torres 100 <br> Set packing problem with 4 ones per column |
| macrophage, <br> methanosarcina, <br> tanglegram1, tanglegram2, <br> toll-like | F. Hüffner 28 68] <br> Balanced subgraph instances coming from applications in bio-informatics: finding monotone subsystems in gene regulatory networks and finding optimal layouts of tanglegrams |
| map06, map10, map14, map18, map20 | K. Ahmadizadeh [6\|96] <br> Land parcel selection problems motivated by Red-Cockaded Woodpecker conservation problem |
| markshare_5_0 | G. Cornuéjols, M. Dawande 139 Market sharing problem |
| maxgasflow, transportmoment | G. Gamrath <br> Transport momentum maximization in a capacitated gas network, transportmoment forbids cycles by pseudo pressures |
| mcsched, npmv07 | Q. Chen [109] Unknown application |
| mik-250-1-100-1 | A. Atamtürk 14 108 <br> Problem with mixed integer knapsack constraints |

mine-90-10, mine-166-5, A. Bley [25]
reblock67, reblock166, Multi-period mine production scheduling instances
reblock354, reblock420
mining K. Eurek
Unspecified mining application
mkc J. Kalagnanam, M. Dawande [45 56]
Multiple knapsack problem with color constraints
momentum1, momentum2, T. Koch 51
momentum3 Snapshot based UMTS planning problems, having a very wide dynamic range in the matrix coefficients and tending to be numerically unstable

Table 5 continued

| Name | Originator and description |
| :---: | :---: |
| mspp16 | P. Troubil, P. Holub, M. Liška, H. Rudová 67 101 <br> Media Streams Planning Problem - A network optimization problem regarding routing of multiple concurrent multimedia streams with bandwidth close to capacity of network links |
| mzzv11 | S. Lukac 94 Railway slot allocation problems |
| n3-3, n4-3, n9-3, n15-3 | A. Atamtürk 13108 . Capacitated network design problems |
| n370a, n3700, n3705, ran14×18, ran14×18-disj-8, ran16x16 | J. Aronson 99 Fixed charge transportation problems |
| n3div36, n3seq24 | R. Meirich 81] <br> Static line planning models on the Dutch IC network |
| nag | N. Shenoy [109] Unknown Application |
| nb10tb | S. Bisaillon Forestry industry model |
| net12 | P. Belotti 1955 Network design instance |
| netdiversion | C. Cullenbine 41] <br> Directed network diversion problem |
| noswot | J. Gregory, L. Schrage [23] Unknown application |
| ns4-pr3, ns4-pr9, nu60-pr9, nu120-pr3 | A. Atamtürk, D. Rajan 15108 Multicommodity flow capacitated network design problems |
| ns1111636, ns1158817 | H. Mittelmann, neos Server 121 Network routing problems |
| ns1631475, ns2137859 | H. Mittelmann, neos Server 121] Traveling salesman problem models |
| ns1702808, ns1905797, ns1905800, ns2118727 | H. Mittelmann, neos Server 121 Vehicle routing problems |
| ns1853823, ns1854840 | H. Mittelmann, neos Server 121 Network flow problems |
| ns1856153, ns1904248 | H. Mittelmann, NeOS Server 121] Sensor placement problems |
| ns2081729 | H. Mittelmann, neos Server 121] <br> Short-term scheduling in a multiproduct sequence dependent facility |
| ofi | L. Poderico <br> Natural gas supply portfolio optimization |
| opm2-z7-s2, opm2-z10-s2, opm2-z11-s8, opm2-z12-s7, opm2-z12-s14 | D. Espinoza Problems coming from precedence constrained knapsacks arising in mining applications |
| p2m2p1m1p0n100 | B. Krishnamoorthy, G. Pataki A 0-1 knapsack problem constructed to be difficult |
| p6b | B. Borchers <br> Maximum independent set problem on a component of the graph 1et. 2048 from the collection of N. Sloane 118 |
| pb-simp-nonunif | 122 <br> Retrieving haplotype information from DNA samples using Haplotype Inference by Pure Parsimony |
| pg, pg5_34 | M. Dawande 44] <br> Multiproduct partial shipment models |

## Table 5 continued

| Name | Originator and description |
| :---: | :---: |
| pigeon-10, pigeon-11, pigeon-12, pigeon-13, pigeon-19 | S. Allen 10 Instances of 3D packing (container loading) problems |
| probportfolio | S. Ahmed, S. Dey, F. Qiu <br> Sample average approximation formulation of a probabilistic portfolio optimization problem |
| protfold | A. Fügenschuh 46] Protein folding instance |
| pw-myciel4 | A. Koster <br> Model to compute the pathwidth of Mycielski-4 instance from DIMACS graph coloring database |
| qiu | Y. Chiu, J. Eckstein 484950 <br> Fiber-optic network design, logical SONET ring level |
| queens-30 | A. Mahajan [124] <br> Models the problem of placing as many queens on a 30 by 30 chess board as possible so that each queen threatens at most one other queen |
| rail01, rail02, rail03 | T. Schlechte 33] <br> Track allocation problem modeled as arc coupling problem |
| rail507 | A. Caprara, M. Fischetti, P. Toth [35 55] Railway crew scheduling |
| ramos3 | F. Ramos <br> Set covering problem from a product manufacturing application |

rmatr100-p5, rmatr100-p10, D. Krushinsky [61]
rmatr200-p5, rmatr200-p10, Instances coming from a formulation of the $p$-Median problem using square cost matrices rmatr200-p20
rmine6, rmine10, rmine14, D. Espinoza
rmine21, rmine25 Set of instances coming from open pit mining over a cube considering multiple time periods and two knapsack constraints per period
rococoB10-011000, A. Chabrier, E. Danna, C. Le Pape, L. Perron 36
rococoC10-001000, Models for dimensioning the arc capacities in a telecommunication network
rococoC11-011100,
rococoC12-111000
rocll-4-11, rocll-7-11, J. Rambau
rocll-9-11 Optimal control of opinion dynamics
roll3000
L. Kroon 55

Rolling stock and line planning instances
satellites1-25, satellites2-60, A. Ceselli, R. He
satellites2-60-fs, Satellite scheduling instances
satellites3-40,
satellites3-40-fs
sct1, sct5, sct32
Siemens
Assembly line balancing for printed circuit board production
set3-10, set3-15, set3-20 K. Akartunalı, A. Miller 788120
Multi-item lot-sizing with backlogging
seymour W. Cook, P. Seymour
A set-covering problem that arose from work related to the proof of the 4-color theorem
seymour-disj-10 M. Ferris, G. Pataki, S. Schmieta [53]
The seymour instance after adding 10 rounds of disjunctive cuts
shipsched E. Günther, M. Lübbecke
A ship scheduling problem on the Kiel Canal
shs1023
C. Helmberg 66115

Joint online truck scheduling and inventory management for multiple warehouses

Table 5 continued

| Name | Originator and description |
| :---: | :---: |
| sing2, sing161, sing245, sing359, uc-case3, uc-case11 | D. Espinoza <br> Unit commitment problems (electricity production planning problems) coming from the Chilean electricity system, they have either one or two week planning horizons, and include constraints on minimum on-off time for the power plants, ensure some reserve energy in the system, and minimize global operation costs. |
| sp97ar, sp98ic, sp98ir | J. Goessens, S. v. Hoessel, L. Kroon [55 63 Railway line planning instances |
| splan1 | C. Helmberg, A. Lau (71] <br> University course timetabling instances |
| stockholm | L. Bai, P. Rubin 16 17] <br> Toll booth placement problem |
| stp3d | T. Koch 70] <br> Steiner tree packing instance in a 3 dimensional grid-graph, LP relaxation is highly degenerate |
| sts 405 , sts 729 | J. Linderoth 86] Steiner triple system problems |
| swath | D. Panton 87 <br> Model arising from the defense industry, involves planning missions for radar surveillance |
| t1717, t1722 | R. Borndörfer 2930 <br> Vehicle scheduling set partitioning problems from Berlin's Telebus handicapped people's transportation system |
| timtab1 | C. Liebchen, R. Möhring 73] Public transport scheduling problems |
| triptim1, triptim2, triptim3 | R. Borndörfer (31] <br> Trip timetable optimization problems |
| tw-myciel4 | A. Koster <br> Model to compute the treewidth of the Mycielski-4 instance from the DIMACS graph coloring database |
| uct-subprob | G. Lach Subproblem of a university course timetabling problem |
| umts | C. Polo 55 92] <br> Telecommunications network model |
| unitcal_7 | R. O'Neill California seven day unit commitment problem |
| van | C. Mannino, E. Parrello 55] <br> Telecommunications network model |
| vpphard, vpphard2 | C. Cardonha Vehicle positioning problem instances |
| wachplan | S. Orlowski <br> Shift planning model to assign crew members to shifts for a sail training trip |
| wnq-n100-mw99-14 | 122 <br> Weighted n -queens problem with an additional separation constraint |
| zib01, zib02 | T. Koch Group channel routing on a 3D grid graph |

Table 5 continued
Name $\quad$ Originator and description
neos6, neos13, neos15, neos16, neos18, neos-476283, neos-506422, neos-506428, neos-520729, neos-555424, neos631710, neos-686190, neos-693347, neos-738098, neos-777800, neos-785912, neos788725, neos-799711, neos-807456, neos808444, neos-820146, neos-820157, neos-824661, neos-824695, neos-826650, neos-826694, neos-826812, neos826841, neos-847302, neos-849702, neos858960, neos-859770, neos-885086, neos-885524, neos-911880, neos-916792, neos-932816, neos-933638, neos-933966, neos-934278, neos-935627, neos-935769, neos-937511, neos-937815, neos941262, neos-941313, neos-942830, neos-948126, neos-952987, neos-957389, neos-984165, neos-1109824, neos-1112782, neos-1112787, neos-1140050, neos-1171692, neos-1171737, neos-1224597, neos-1225589, neos-1311124, neos-1337307, neos-1396125, neos-1426635, neos-1426662, neos-1429212, neos-1436709, neos-1440225, neos-1440460, neos-1442119, neos-1442657, neos-1601936, neos-1605061, neos-1605075, neos-1616732, neos-1620770, ns894236, ns894244, ns894786, ns894788, ns903616, ns930473, ns1116954, ns1208400, ns1456591, ns1606230, ns1644855, ns1663818, ns1685374, ns1686196, ns1688347, ns1696083, ns1745726, ns1758913, ns1766074, ns1769397, ns1778858, ns1830653, ns1952667, ns2124243, ns2017839
Table 6: Problem statistics

| Name | Rows | Columns | Non-Zeros | Binary | Integer | Continuous | MIP Solution | LP Solution | Att.-level | Sets | Status |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 30_70_45_095_100 | 12,526 | 10,976 | 46,640 | 10,975 |  | 1 | 3 | 3 |  | P | easy |
| 30 n 20 b 8 | 576 | 18,380 | 109,706 | 11,036 | 7,344 |  | 302 | 1.566408 |  | B | easy |
| $50 \mathrm{v}-10$ | 233 | 2,013 | 2,745 | 1,464 | 183 | 366 | 3311.179984123 | 2879.065687 |  | C | hard |
| a1c1s1 | 3,312 | 3,648 | 10,178 | 192 |  | 3,456 | 11503.444125 | 997.529583 |  | C | hard |
| acc-tight4 | 3,285 | 1,620 | 17,073 | 1,620 |  |  | 0 | 0 |  | RP | easy |
| acc-tight5 | 3,052 | 1,339 | 16,134 | 1,339 |  |  | 0 | 0 |  | BRP | easy |
| acc-tight6 | 3,047 | 1,335 | 16,108 | 1,335 |  |  | 0 | 0 | 0.001 | RP | easy |
| aflow40b | 1,442 | 2,728 | 6,783 | 1,364 |  | 1,364 | 1168 | 1005.664817 |  | B | easy |
| air04 | 823 | 8,904 | 72,965 | 8,904 |  |  | 56137 | 55535.436388 |  | B | easy |
| app1-2 | 53,467 | 26,871 | 199,175 | 13,300 |  | 13,571 | -41 | -264.601651 | 0.001 | B | easy |
| ash608gpia-3col | 24,748 | 3,651 | 74,244 | 3,651 |  |  | infeasible | 2 |  | BI | easy |
| atlanta-ip | 21,732 | 48,738 | 257,532 | 46,667 | 106 | 1,965 | 90.009878614 | 81.243199 |  | C | hard |
| atm20-100 | 4,380 | 6,480 | 58,878 | 2,220 |  | 4,260 | ? | 2141734.684878 | 0.006 | C | open |
| b2c1s1 | 3,904 | 3,872 | 11,408 | 288 |  | 3,584 | ? | 4034.218333 |  | C | open |
| bab1 | 60,680 | 61,152 | 854,392 | 61,152 |  |  | ? | -286923.824223 |  | C | open |
| bab3 | 23,069 | 393,800 | 3,301,838 | 393,800 |  |  | ? | -733091.180443 |  | C | open |
| bab5 | 4,964 | 21,600 | 155,520 | 21,600 |  |  | -106411.8401 | -124657.641413 |  | B | easy |
| beasleyC3 | 1,750 | 2,500 | 5,000 | 1,250 |  | 1,250 | 754 | 40.426829 |  | B | easy |
| berlin_5_8_0 | 1,532 | 1,083 | 4,507 | 794 |  | 289 | ? | 52 |  | C | open |
| bg512142 | 1,307 | 792 | 3,953 | 240 |  | 552 | ? | 144364.073815 |  | C | open |
| biella 1 | 1,203 | 7,328 | 71,489 | 6,110 |  | 1,218 | 3065005.78 | 3060037.430763 |  | B | easy |
| bienst2 | 576 | 505 | 2,184 | 35 |  | 470 | 54.6 | 11.724138 |  | B | easy |
| binkar10_1 | 1,026 | 2,298 | 4,496 | 170 |  | 2,128 | 6742.200024 | 6637.188027 |  | B | easy |
| bley_xl1 | 175,620 | 5,831 | 869,391 | 5,831 |  |  | 190 | 154.3902 |  | B | easy |
| blp-ar98 | 1,128 | 16,021 | 200,601 | 15,806 |  | 215 | 6205.2147104 | 5891.22658 |  | T | easy |
| blp-ic97 | 923 | 9,845 | 118,149 | 9,753 |  | 92 | ? | 3846.358667 |  | C | open |
| bnatt350 | 4,923 | 3,150 | 19,061 | 3,150 |  |  | 0 | 0 |  | BRP | easy |
| bnatt400 | 5,614 | 3,600 | 21,698 | 3,600 |  |  | 1 | 0 |  | CR | hard |
| buildingenergy | 277,594 | 154,978 | 788,969 |  | 26,287 | 128,691 | ? | 33246.2 |  | C | open |
| cdma | 9,095 | 7,891 | 168,227 | 4,235 |  | 3,656 | ? | $-6.38289 e+16$ | 0.194 | CU | open |
| circ10-3 | 42,620 | 2,700 | 307,320 | 2,700 |  |  | ? | 140 | 0.001 | CR | open |
| co-100 | 2,187 | 48,417 | 1,995,817 | 48,417 |  |  | 2639942.06 | 917102.214427 |  | C | hard |
| core2536-691 | 2,539 | 15,293 | 177,739 | 15,284 |  | 9 | 689 | 688.476034 |  | B | easy |
| core4872-1529 | 4,875 | 24,656 | 218,762 | 24,645 |  | 11 | ? | 1509.718561 |  | C | open |
| cov1075 | 637 | 120 | 14,280 | 120 |  |  | 20 | 17.142857 |  | B | easy |
| csched007 | 351 | 1,758 | 6,379 | 1,457 |  | 301 | 351 | 269.251587 |  | T | easy |
| csched008 | 351 | 1,536 | 5,687 | 1,284 |  | 252 | 173 | 171 |  | RT | easy |
| csched010 | 351 | 1,758 | 6,376 | 1,457 |  | 301 | 408 | 332.422727 |  | B | easy |
| d10200 | 947 | 2,000 | 57,637 | 733 | 1,267 |  | ? | 12425.583005 |  | C | open |
| d20200 | 1,502 | 4,000 | 189,389 | 3,181 | 819 |  | ? | 12229.625788 |  | C | open |
| dano3mip | 3,202 | 13,873 | 79,655 | 552 |  | 13,321 | ? | 576.23162 | 0.005 | CR | open |
| danoint | 664 | 521 | 3,232 | 56 |  | 465 | 65.666666667 | 62.63728 |  | B | easy |
| datt256 | 11,077 | 262,144 | 1,503,732 | 262,144 |  |  | ? | 256 | - | C | open |
| dc1c | 1,649 | 10,039 | 121,158 | 8,380 |  | 1,659 | ? | 1754946.863638 |  | C | open |
| dc1l | 1,653 | 37,297 | 448,754 | 35,638 |  | 1,659 | ? | 1744591.692942 |  | C | open |
| dfn-gwin-UUM | 158 | 938 | 2,632 |  | 90 | 848 | 38752 | 27467.257235 |  | B | easy |

[^4]| Name | Rows | Columns | Non-Zeros | Binary | Integer | Continuous | mIP Solution | LP Solution | Att.-level | Sets | Status |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| dg012142 | 6,310 | 2,080 | 14,795 | 640 |  | 1,440 | ? | 757818.480114 |  | C | open |
| dolom1 | 1,803 | 11,612 | 190,413 | 9,720 |  | 1,892 | ? | 6556066.068315 |  | C | open |
| ds-big | 1,042 | 174,997 | 4,623,442 | 174,997 |  |  | ? | 86.820068 |  | CR | open |
| eil33-2 | 32 | 4,516 | 44,243 | 4,516 |  |  | 934.007916 | 811.278996 |  | B | easy |
| eilA101-2 | 100 | 65,832 | 959,373 | 65,832 |  |  | 880.920108 | 803.373888 |  | C | hard |
| eilB101 | 100 | 2,818 | 24,120 | 2,818 |  |  | 1216.920174 | 1075.247691 |  | B | easy |
| enlight13 | 169 | 338 | 962 | 169 | 169 |  | 71 | 0 |  | B | easy |
| enlight14 | 196 | 392 | 1,120 | 196 | 196 |  | infeasible | 0 |  | BI | easy |
| enlight15 | 225 | 450 | 1,290 | 225 | 225 |  | 69 | 0 |  | T | easy |
| enlight16 | 256 | 512 | 1,472 | 256 | 256 |  | infeasible | 0 |  | IT | easy |
| enlight9 | 81 | 162 | 450 | 81 | 81 |  | infeasible | 0 |  | 1 | easy |
| ex1010-pi | 1,468 | 25,200 | 102,114 | 25,200 |  |  | ? | 220.670087 |  | C | open |
| ex10 | 69,608 | 17,680 | 1,162,000 | 17,680 |  |  | 100 | 100 | 0.001 | P | easy |
| ex9 | 40,962 | 10,404 | 517,112 | 10,404 |  |  | 81 | 81 |  | BP | easy |
| f2000 | 10,500 | 4,000 | 29,500 | 4,000 |  |  | ? | 1331 |  | CR | open |
| g200x 740 i | 940 | 1,480 | 2,960 | 740 |  | 740 | ? | 2292.465 |  | C | open |
| ger50_17_trans | 499 | 22,414 | 172,035 |  | 18,062 | 4,352 | ? | 6850.628623 | 0.01 | CU | open |
| germanrr | 10,779 | 10,813 | 175,547 | 5,288 | 5,286 | 239 | ? | 45980135.416399 |  | C | open |
| germany50-DBM | 2,526 | 8,189 | 24,479 |  | 88 | 8,101 | ? | 438028 |  | C | open |
| glass4 | 396 | 322 | 1,815 | 302 |  | 20 | 1200012600 | 800002400 |  | BT | easy |
| gmu-35-40 | 424 | 1,205 | 4,843 | 1,200 |  | 5 | -2406733.3688 | -2406943.556343 |  | BT | easy |
| gmu-35-50 | 435 | 1,919 | 8,643 | 1,914 |  | 5 | -2607958.33 | -2608070.315743 |  | T | easy |
| gmut-75-50 | 2,565 | 68,865 | 571,475 | 68,859 |  | 6 | ? | -14182312.661731 | 0.001 | C | open |
| gmut-77-40 | 2,554 | 24,338 | 159,902 | 24,332 |  | 6 | ? | -14173396.636852 | 0.002 | C | open |
| go19 | 441 | 441 | 1,885 | 441 |  |  | 84 | 76.530222 |  | CT | hard |
| hanoi5 | 16,399 | 3,862 | 39,718 | 3,862 |  |  | $?$ | 1467 |  | CR | open |
| harp2 | 112 | 2,993 | 5,840 | 2,993 |  |  | -73899798 | -74353341.5023 |  | U | easy |
| hawaiiv10-130 | 1,388,052 | 685,130 | 183,263,061 | 578,444 |  | 106,686 | ? | 52281537.594958 | 0.24 | CXU | open |
| ic97_potential | 1,046 | 728 | 3,138 | 450 | 73 | 205 | 3942 | 3868 |  | C | hard |
| iis-100-0-cov | 3,831 | 100 | 22,986 | 100 |  |  | 29 | 16.666667 |  | B | easy |
| iis-bupa-cov | 4,803 | 345 | 38,392 | 345 |  |  | 36 | 26.497217 |  | B | easy |
| iis-pima-cov | 7,201 | 768 | 71,941 | 768 |  |  | 33 | 26.620389 |  | B | easy |
| in | 1,526,202 | 1,449,074 | 6,811,639 | 1,489 |  | 1,447,585 | ? | ? | - | CRX | open |
| ivu06-big | 1,177 | 2,277,736 | 23,125,770 | 2,277,736 |  |  | ? | 135.428 |  | CRX | open |
| ivu52 | 2,116 | 157,591 | 2,179,476 | 157,591 |  |  | ? | 480.250438 | 0.001 | CR | open |
| janos-us-DDM | 760 | 2,184 | 6,384 |  | 84 | 2,100 | ? | 1488134.75 |  | C | open |
| k16x240 | 256 | 480 | 960 | 240 |  | 240 | 10674 | 2769.838 |  | T | easy |
| lectsched-1 | 50,108 | 28,718 | 310,792 | 28,236 | 482 |  | 0 | 0 |  | P | easy |
| lectsched-1-obj | 50,108 | 28,718 | 310,792 | 28,236 | 482 |  | ? | 0 |  | C | open |
| lectsched-2 | 30,738 | 17,656 | 186,520 | 17,287 | 369 |  | 0 | 0 |  | P | easy |
| lectsched-3 | 45,262 | 25,776 | 279,967 | 25,319 | 457 |  | 0 | 0 |  | P | easy |
| lectsched-4-obj | 14,163 | 7,901 | 82,428 | 7,665 | 236 |  | 4 | 0 |  | B | easy |
| leol | 593 | 6,731 | 131,218 | 6,730 |  | 1 | 404227536.16 | 388573315.509608 |  | T | easy |
| leo2 | 593 | 11,100 | 219,959 | 11,099 |  | 1 | 404077441.12 | 386421293.208919 |  | C | hard |
| liu | 2,178 | 1,156 | 10,626 | 1,089 |  | 67 | ? | 346 |  | C | open |
| lotsize | 1,920 | 2,985 | 6,565 | 1,195 |  | 1,790 | 1480195 | 348385.346551 | 0.009 | C | hard |
| Irsa120 | 14,521 | 3,839 | 39,956 | 120 | 119 | 3,600 | ? | 29 |  | C | open |
| m100n500k4r1 | 100 | 500 | 2,000 | 500 |  |  | -25 | -25 |  | BP | hard |
| macrophage | 3,164 | 2,260 | 9,492 | 2,260 |  |  | 374 | 0 |  | B | easy |


| Name | Rows | Columns | Non-Zeros | Binary | Integer | Continuous | miP Solution | LP Solution | Att.-level | Sets | Status |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| map06 | 328,818 | 164,547 | 549,920 | 146 |  | 164,401 | -289 | -406.181173 |  | R | easy |
| map10 | 328,818 | 164,547 | 549,920 | 146 |  | 164,401 | -495 | -602.176181 |  | R | easy |
| map14 | 328,818 | 164,547 | 549,920 | 146 |  | 164,401 | -674 | -778.549324 |  | R | easy |
| map18 | 328,818 | 164,547 | 549,920 | 146 |  | 164,401 | -847 | -932.782685 |  | BR | easy |
| map20 | 328,818 | 164,547 | 549,920 | 146 |  | 164,401 | -922 | -998.836419 |  | B | easy |
| markshare_5_0 | 5 | 45 | 203 | 40 |  | 5 | 1 | 0 |  | T | easy |
| maxgasflow | 7,160 | 7,437 | 19,717 | 2,456 |  | 4,981 | ? | -70929535.9 | 0.01 | CT | open |
| mc11 | 1,920 | 3,040 | 6,080 | 1,520 |  | 1,520 | 11689 | 608.84434 |  | T | easy |
| mcsched | 2,107 | 1,747 | 8,088 | 1,731 | 14 | 2 | 211913 | 193774.753707 |  | B | easy |
| methanosarcina | 14,604 | 7,930 | 43,812 | 7,930 |  |  | ? | 0 |  | C | open |
| mik-250-1-100-1 | 151 | 251 | 5,351 | 100 | 150 | 1 | -66729 | -79842.423635 |  | B | easy |
| mine-166-5 | 8,429 | 830 | 19,412 | 830 |  |  | -566395707.87083 | -821763677.673139 |  | B | easy |
| mine-90-10 | 6,270 | 900 | 15,407 | 900 |  |  | -784302337.633173 | -887165318.510226 |  | B | easy |
| mining | 661,133 | 348,921 | 3,844,879 | 348,920 |  | 1 | ? | -949724584.696851 | - | C | open |
| mkc | 3,411 | 5,325 | 17,038 | 5,323 |  | 2 | -563.846 | -611.85 |  | C | hard |
| momentum1 | 42,680 | 5,174 | 103,198 | 2,349 |  | 2,825 | 109143 | 72793.345255 | 0.017 | CT | hard |
| momentum 2 | 24,237 | 3,732 | 349,695 | 1,808 | 1 | 1,923 | 12314.1 | 7225.44067 | 0.069 | U | easy |
| momentum 3 | 56,822 | 13,532 | 949,495 | 6,598 | 1 | 6,933 | ? | 91952.392314 | 0.014 | CR | open |
| msc98-ip | 15,850 | 21,143 | 92,918 | 20,237 | 53 | 853 | 19839497.005874302 | 19520966.151661 |  | BR | easy |
| mspp16 | 561,657 | 29,280 | 27,678,735 | 29,280 |  |  | 363 | 341 |  | BX | easy |
| mzzv11 | 9,499 | 10,240 | 134,603 | 9,989 | 251 |  | -21718 | -22945.239631 | 0.001 | B | easy |
| n15-3 | 29,494 | 153,140 | 611,000 |  | 780 | 152,360 | ? | 23703.941176 | 0.007 | CR | open |
| n3-3 | 2,425 | 9,028 | 35,380 |  | 366 | 8,662 | $?$ | 7465.294118 |  | C | open |
| n3700 | 5,150 | 10,000 | 20,000 | 5,000 |  | 5,000 | $?$ | 972305.748043 | 0.008 | C | open |
| n3705 | 5,150 | 10,000 | 20,000 | 5,000 |  | 5,000 | ? | 973361.017012 | 0.008 | C | open |
| n370a | 5,150 | 10,000 | 20,000 | 5,000 |  | 5,000 | ? | 979219.544813 | 0.007 | C | open |
| n3div36 | 4,484 | 22,120 | 340,740 | 22,120 |  |  | 130800 | 114333.374741 |  | B | hard |
| n3seq24 | 6,044 | 119,856 | 3,232,340 | 119,856 |  |  | 52200 | 52000 |  | B | easy |
| n4-3 | 1,236 | 3,596 | 14,036 |  | 174 | 3,422 | 8993 | 4080.882353 |  | B | easy |
| n9-3 | 2,364 | 7,644 | 30,072 |  | 252 | 7,392 | 14409 | 7889.705882 |  | C | hard |
| nag | 5,840 | 2,884 | 26,499 | 1,350 | 35 | 1,499 | ? | 465 |  | C | open |
| nb10tb | 150,495 | 73,340 | 1,172,289 | 14,124 | 2,756 | 56,460 | ? | 12986061164.423624 | 0.34 | CU | open |
| neos-1109824 | 28,979 | 1,520 | 89,528 | 1,520 |  |  | 378 | 278 |  | B | easy |
| neos-1112782 | 2,115 | 4,140 | 8,145 | 2,070 |  | 2,070 | $5.72103 e+11$ | 499999999923.7446 | 0.246 | U | easy |
| neos-1112787 | 1,680 | 3,280 | 6,440 | 1,640 |  | 1,640 | $5.65032 e+11$ | 499999999913.1923 | 0.066 | U | easy |
| neos-1140050 | 3,795 | 40,320 | 808,080 | 38,640 |  | 1,680 | ? | 5071593.661704 | 0.299 | CU | open |
| neos-1171692 | 4,239 | 1,638 | 42,945 | 819 |  | 819 | -273 | -273 |  | P | easy |
| neos-1171737 | 4,179 | 2,340 | 58,620 | 1,170 |  | 1,170 | -195 | -195 |  | P | easy |
| neos-1224597 | 3,276 | 3,395 | 25,090 | 3,150 | 245 |  | -428 | -428 |  | P | easy |
| neos-1225589 | 675 | 1,300 | 2,525 | 650 |  | 650 | 1231065191.85 | 200000000 | 0.186 | U | easy |
| neos-1311124 | 1,643 | 1,092 | 7,140 | 546 |  | 546 | ? | -182 |  | C | open |
| neos-1337307 | 5,687 | 2,840 | 30,799 | 2,840 |  |  | -202319 | -203123.973856 |  | B | easy |
| neos-1396125 | 1,494 | 1,161 | 5,511 | 129 |  | 1,032 | 3000.045337302 | 388.5524 |  | B | easy |
| neos13 | 20,852 | 1,827 | 253,842 | 1,815 |  | 12 | -95.474806559 | -126.178378 |  | B | easy |
| neos-1426635 | 796 | 520 | 3,400 | 260 |  | 260 | -176 | -178 |  | T | easy |
| neos-1426662 | 1,914 | 832 | 8,048 | 416 |  | 416 | -44 | -52 |  | T | easy |
| neos-1429212 | 58,726 | 416,040 | 1,855,220 | 54,756 |  | 361,284 | ? | 30 |  | C | open |
| neos-1436709 | 1,417 | 676 | 6,214 | 338 |  | 338 | -128 | -129 |  | T | easy |
| neos-1440225 | 330 | 1,285 | 14,168 | 1,285 |  |  | 36 | 36 | 0.003 | P | easy |


| Name | Rows | Columns | Non-Zeros | Binary | Integer | Continuous | MIP Solution | LP Solution | Att.-level | Sets | Status |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| neos-1440460 | 989 | 468 | 4,302 | 234 |  | 234 | -179.25 | -180 |  | T | easy |
| neos-1442119 | 1,524 | 728 | 6,692 | 364 |  | 364 | -181 | -182 |  | T | easy |
| neos-1442657 | 1,310 | 624 | 5,736 | 312 |  | 312 | -154.5 | -156 |  | T | easy |
| neos15 | 552 | 792 | 1,766 | 160 |  | 632 | 80598.430096861 | 29624.693694 |  | T | easy |
| neos-1601936 | 3,131 | 4,446 | 72,500 | 3,906 |  | 540 | 3 | 1 |  | BR | easy |
| neos-1605061 | 3,474 | 4,111 | 93,483 | 3,570 |  | 541 | 12 | 6.150735 |  | R | easy |
| neos-1605075 | 3,467 | 4,173 | 91,377 | 3,633 |  | 540 | 9 | 3.214461 |  | R | easy |
| neos-1616732 | 1,999 | 200 | 3,998 | 200 |  |  | 159 | 100 |  | T | easy |
| neos-1620770 | 9,296 | 792 | 19,292 | 792 |  |  | 9 | 1 |  | T | hard |
| neos16 | 1,018 | 377 | 2,801 | 336 | 41 |  | 446 | 429 |  | T | easy |
| neos18 | 11,402 | 3,312 | 24,614 | 3,312 |  |  | 16 | 7 |  | B | easy |
| neos-476283 | 10,015 | 11,915 | 3,945,693 | 5,588 |  | 6,327 | 406.363206984 | 406.244708 |  | B | easy |
| neos-506422 | 6,811 | 2,527 | 31,815 | 63 |  | 2,464 | 0 | 0 |  | P | easy |
| neos-506428 | 129,925 | 42,981 | 343,466 | 42,981 |  |  | 583780 | 145945 |  | R | easy |
| neos-520729 | 31,178 | 91,149 | 322,203 | 30,708 |  | 60,441 | -1385000 | -1391291.666667 | 0.185 | U | easy |
| neos-555424 | 2,676 | 3,815 | 15,667 | 3,800 | 15 |  | 1286800 | 1196312.54944 |  | P | easy |
| neos-631710 | 169,576 | 167,056 | 834,166 | 167,056 |  |  | ? | 188.25 |  | CR | open |
| neos-686190 | 3,664 | 3,660 | 18,085 | 3,600 | 60 |  | 6730 | 5134.81383 |  | B | easy |
| neos-693347 | 3,192 | 1,576 | 113,472 | 1,405 |  | 171 | 234 | 234 |  | P | easy |
| neos6 | 1,036 | 8,786 | 251,946 | 8,340 |  | 446 | 83 | 83 |  | P | easy |
| neos-738098 | 25,849 | 9,093 | 101,360 | 8,946 |  | 147 | -1099 | -1099 |  | P | easy |
| neos-777800 | 479 | 6,400 | 32,000 | 6,400 |  |  | -80 | -80 |  | P | easy |
| neos-785912 | 1,714 | 1,380 | 16,610 | 1,380 |  |  | infeasible | 42 |  | 1 | easy |
| neos788725 | 433 | 352 | 4,912 | 352 |  |  | infeasible | -44.65 |  | 1 | easy |
| neos-799711 | 59,218 | 41,998 | 147,164 | 910 |  | 41,088 | -11170211.73363777 | -11228065.153797 | 0.056 | U | easy |
| neos-807456 | 840 | 1,635 | 4,905 | 1,635 |  |  | ? | 280 | 0.005 | C | open |
| neos808444 | 18,329 | 19,846 | 120,512 | 19,846 |  |  | 0 | 0 |  | P | easy |
| neos-820146 | 830 | 600 | 3,225 | 600 |  |  | infeasible | 0 |  | IT | easy |
| neos-820157 | 1,015 | 1,200 | 4,875 | 1,200 |  |  | infeasible | 0 |  | IT | easy |
| neos-824661 | 18,804 | 45,390 | 138,890 | 15,640 |  | 29,750 | 33 | 33 |  | P | easy |
| neos-824695 | 9,576 | 23,970 | 72,590 | 8,500 |  | 15,470 | 31 | 31 |  | P | easy |
| neos-826650 | 2,414 | 5,912 | 20,440 | 5,792 |  | 120 | 29 | 28 |  | T | easy |
| neos-826694 | 6,904 | 16,410 | 59,268 | 16,290 |  | 120 | 58 | 58 |  | P | easy |
| neos-826812 | 6,844 | 15,864 | 53,808 | 10,350 |  | 5,514 | 58.011 | 58.011 |  | P | easy |
| neos-826841 | 2,354 | 5,516 | 18,460 | 3,488 |  | 2,028 | 29.0082 | 28.0082 |  | T | easy |
| neos-847302 | 609 | 737 | 9,566 | 729 |  | 8 | 4 | 0 |  | T | hard |
| neos-849702 | 1,041 | 1,737 | 19,308 | 1,737 |  |  | 0 | 0 | 0.001 | BP | easy |
| neos858960 | 132 | 160 | 2,770 | 160 |  |  | infeasible | 1 |  | IT | easy |
| neos-859770 | 2,065 | 2,504 | 880,736 | 2,504 |  |  | infeasible | 4500 |  | 1 | easy |
| neos-885086 | 11,574 | 4,860 | 248,310 | 2,430 |  | 2,430 | -243 | -243 |  | P | easy |
| neos-885524 | 65 | 91,670 | 258,309 | 91,670 |  |  | 12320.092 | 11754.885 |  | P | easy |
| neos-911880 | 83 | 888 | 2,568 | 840 |  | 48 | 54.76 | 23.26 |  | T | easy |
| neos-916792 | 1,909 | 1,474 | 134,442 | 717 |  | 757 | 31.870398371 | 26.203596 | 0.001 | B | easy |
| neos-932816 | 30,823 | 21,007 | 484,926 | 20,566 |  | 441 | 15376 | 2285.5 |  | P | easy |
| neos-933638 | 13,658 | 32,417 | 187,173 | 28,637 |  | 3,780 | 276 | 276 |  | P | easy |
| neos-933966 | 12,047 | 31,762 | 180,618 | 27,982 |  | 3,780 | 318 | 318 |  | P | easy |
| neos-934278 | 11,495 | 23,123 | 125,577 | 19,955 |  | 3,168 | 260 | 259.5 |  | B | easy |
| neos-935627 | 7,859 | 10,301 | 40,476 | 7,522 |  | 2,779 | 2598 | 2598 |  | RP | easy |
| neos-935769 | 6,741 | 9,799 | 36,447 | 7,020 |  | 2,779 | 3010 | 3010 |  | P | easy |


| Name | Rows | Columns | Non-Zeros | Binary | Integer | Continuous | MIP Solution | LP Solution | Att.-level | Sets | Status |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| neos-937511 | 8,158 | 11,332 | 44,237 | 8,562 |  | 2,770 | 3510 | 3510 |  | P | easy |
| neos-937815 | 9,251 | 11,646 | 48,013 | 8,876 |  | 2,770 | ? | 2837 |  | CR | open |
| neos-941262 | 6,703 | 9,480 | 35,659 | 6,710 |  | 2,770 | 2791 | 2790.5 |  | R | easy |
| neos-941313 | 13,189 | 167,910 | 484,080 | 167,910 |  |  | 9361 | 9361 |  | P | easy |
| neos-942830 | 803 | 882 | 13,290 | 834 |  | 48 | 16 | 12 |  | T | easy |
| neos-948126 | 7,271 | 9,551 | 38,219 | 6,965 |  | 2,586 | 2607 | 2602 |  | R | hard |
| neos-952987 | 354 | 31,329 | 90,384 | 31,329 |  |  | ? | 1327.33714 |  | C | open |
| neos-957389 | 5,115 | 6,036 | 355,372 | 6,036 |  |  | 1.5 | 1.5 |  | P | easy |
| neos-984165 | 6,962 | 8,883 | 36,742 | 6,478 |  | 2,405 | ? | 2186 |  | CR | open |
| net12 | 14,021 | 14,115 | 80,384 | 1,603 |  | 12,512 | 214 | 17.249479 |  | BR | easy |
| netdiversion | 119,589 | 129,180 | 615,282 | 129,180 |  |  | 242 | 230.8 |  | B | easy |
| newdano | 576 | 505 | 2,184 | 56 |  | 449 | 65.666666667 | 11.724138 |  | B | easy |
| nobel-eu-DBE | 879 | 3,771 | 11,313 | 1,639 |  | 2,132 | 608910 | 570687.5 |  | T | hard |
| noswot | 182 | 128 | 735 | 75 | 25 | 28 | -41 | -43 |  | BT | easy |
| npmv07 | 76,342 | 220,686 | 859,614 | 1,880 |  | 218,806 | $1.0481 e+11$ | 104809667051.7079 | 0.007 | U | hard |
| ns1111636 | 13,895 | 360,822 | 568,444 | 13,200 |  | 347,622 | ? | 96.25 | 0.015 | CR | open |
| ns1116954 | 131,991 | 12,648 | 410,582 | 7,482 |  | 5,166 | 0 | 0 |  | P | easy |
| ns1158817 | 68,455 | 1,804,022 | 2,842,044 | 66,022 |  | 1,738,000 | infeasible | infeasible | 0.01 | 1 | easy |
| ns1208400 | 4,289 | 2,883 | 81,746 | 2,880 |  | 3 | 2 | 0 |  | B | easy |
| ns1456591 | 1,997 | 8,399 | 199,862 | 8,000 | 19 | 380 | ? | 361.939022 | 0.001 | CT | open |
| ns1606230 | 3,503 | 4,173 | 92,133 | 3,633 |  | 540 | 21 | 13.225 |  | R | easy |
| ns1631475 | 24,496 | 22,696 | 116,733 | 22,470 | 211 | 15 | ? | 817.193748 |  | CR | open |
| ns1644855 | 40,698 | 30,200 | 2,110,696 | 10,000 |  | 20,200 | -1524.333333333 | -1524.333333 | 0.039 | R | hard |
| ns1663818 | 172,017 | 124,626 | 20,433,649 | 124,626 |  |  | ? | 1 |  | CX | open |
| ns1685374 | 44,121 | 10,000 | 220,859 | 10,000 |  |  | -13 | -51.800913 |  | R | hard |
| ns1686196 | 4,055 | 2,738 | 68,529 | 2,738 |  |  | infeasible | 2 |  | 1 | easy |
| ns1688347 | 4,191 | 2,685 | 66,908 | 2,685 |  |  | 27 | 2 |  | B | easy |
| ns1696083 | 11,063 | 7,982 | 384,129 | 7,982 |  |  | ? | 2 | 0.003 | CR | open |
| ns1702808 | 1,474 | 804 | 5,856 | 666 |  | 138 | infeasible | 1700 |  | 1 | easy |
| ns1745726 | 4,687 | 3,208 | 90,278 | 3,208 |  |  | infeasible | 3 |  | 1 | easy |
| ns1758913 | 624,166 | 17,956 | 1,283,444 | 17,822 |  | 134 | -1454.671755 | -1501.183256 |  | B | easy |
| ns1766074 | 182 | 100 | 666 |  | 90 | 10 | infeasible | 5833.8 |  | BIT | easy |
| ns1769397 | 5,527 | 3,772 | 117,383 | 3,772 |  |  | infeasible | 3 | 0.001 | 1 | easy |
| ns1778858 | 10,666 | 4,720 | 32,673 | 4,720 |  |  | ? | -28931833.446612 |  | C | open |
| ns1830653 | 2,932 | 1,629 | 100,933 | 1,458 |  | 171 | 20622 | 6153 |  | B | easy |
| ns1853823 | 224,526 | 213,440 | 1,489,480 | 213,440 |  |  | ? | 60182.9 | 0.008 | C | open |
| ns1854840 | 143,616 | 135,754 | 856,994 | 135,280 | 474 |  | ? | 122000 |  | C | open |
| ns1856153 | 35,407 | 11,998 | 105,882 | 11,956 |  | 42 | ? | 0 |  | CR | open |
| ns1904248 | 149,437 | 38,458 | 378,770 | 38,416 |  | 42 | ? | 0 | 0.007 | C | open |
| ns1905797 | 51,884 | 18,192 | 239,700 | 17,676 | 4 | 512 | ? | 11.75098 |  | C | open |
| ns1905800 | 8,289 | 3,228 | 38,100 | 3,030 | 3 | 195 | ? | 6.4366 |  | C | open |
| ns1952667 | 41 | 13,264 | 335,643 |  | 13,264 |  | 0 | 0 |  | P | easy |
| ns2017839 | 54,510 | 55,224 | 317,840 | 12 |  | 55,212 | 7.70305e+13 | 77025639567520.05 | 0.01 | U | easy |
| ns2081729 | 1,190 | 661 | 5,680 | 600 |  | 61 | 9 | 4.6 |  | T | easy |
| ns2118727 | 163,354 | 167,440 | 646,864 | 159,514 |  | 7,926 | infeasible | 260.751793 | 0.002 | IR | easy |
| ns2122603 | 24,754 | 19,300 | 77,044 | 7,588 |  | 11,712 | infeasible | 0 | 1 | IU | hard |
| ns2124243 | 139,280 | 156,083 | 429,032 | 16,447 |  | 139,636 | ? | 53998.333333 |  | C | open |
| ns2137859 | 206,726 | 103,361 | 923,682 | 103,041 |  | 320 | ? | 24629 |  | C | open |
| ns4-pr3 | 2,210 | 8,601 | 25,986 |  | 61 | 8,540 | ? | 36073 |  | C | open |


| Name | Rows | Columns | Non-Zeros | Binary | Integer | Continuous | MIP Solution | LP Solution | Att.-level | Sets | Status |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| ns4-pr9 | 2,220 | 7,350 | 22,176 |  | 42 | 7,308 | ? | 35175 |  | C | open |
| ns894236 | 8,218 | 9,666 | 41,067 | 9,666 |  |  | ? | 12.305229 |  | CR | open |
| ns894244 | 12,129 | 21,856 | 90,864 | 21,856 |  |  | 15 | 12.326616 | 0.006 | R | easy |
| ns894786 | 16,794 | 27,278 | 113,575 | 27,278 |  |  | ? | 6.080533 | 0.001 | CR | open |
| ns894788 | 2,279 | 3,463 | 14,381 | 3,463 |  |  | 7 | 6.304802 |  | T | easy |
| ns903616 | 18,052 | 21,582 | 91,641 | 21,582 |  |  | ? | 14.750147 | 0.001 | CR | open |
| ns930473 | 23,240 | 11,328 | 121,764 | 11,176 |  | 152 | ? | 0 | 0.001 | CR | open |
| nsr8k | 6,284 | 38,356 | 371,608 | 32,040 |  | 6,316 | ? | 17500809.511815 | 0.001 | CR | open |
| nu120-pr3 | 2,210 | 8,601 | 25,986 | 8,540 | 61 |  | 28130 | 21306.442308 |  | C | hard |
| nu60-pr9 | 2,220 | 7,350 | 22,176 | 7,308 | 42 |  | 24940 | 22850 |  | C | hard |
| ofi | 422,587 | 420,434 | 1,778,754 | 18,632 | 11,073 | 390,729 | $6.15538 e+09$ | 6131846109.623997 | 0.168 | U | hard |
| opm2-z10-s2 | 160,633 | 6,250 | 371,243 | 6,250 |  |  | ? | -49308.278601 | 0.001 | C | open |
| opm2-z11-s8 | 223,082 | 8,019 | 510,283 | 8,019 |  |  | ? | -62971.930395 |  | CR | open |
| opm2-z12-s14 | 319,508 | 10,800 | 725,376 | 10,800 |  |  | ? | -91524.54224 | 0.001 | CR | open |
| opm2-z12-s7 | 319,508 | 10,800 | 725,385 | 10,800 |  |  | ? | -90514.285842 | 0.001 | CR | open |
| opm2-z7-s2 | 31,798 | 2,023 | 79,762 | 2,023 |  |  | -10280 | -12879.686897 |  | B | easy |
| p100x588b | 688 | 1,176 | 2,352 | 588 |  | 588 | ? | 5554.011111 |  | C | open |
| p2m2p1m1p0n100 | 1 | 100 | 100 | 100 |  |  | infeasible | 80424 |  | IT | easy |
| p6b | 5,852 | 462 | 11,704 | 462 |  |  | $?$ | -231 |  | C | open |
| p80x400b | 480 | 800 | 1,600 | 400 |  | 400 | 39667 | 6418.8 |  | T | easy |
| pb-simp-nonunif | 1,451,912 | 23,848 | 4,366,648 | 23,848 |  |  | ? | 6 | 0.001 | CX | open |
| pg5-34 | 225 | 2,600 | 7,700 | 100 |  | 2,500 | -14339.353446926 | -16646.586017 |  | B | easy |
| pg | 125 | 2,700 | 5,200 | 100 |  | 2,600 | -8674.342607117 | -11824.657382 |  | T | easy |
| pigeon-10 | 931 | 490 | 8,150 | 400 |  | 90 | -9000 | -10000 |  | BT | easy |
| pigeon-11 | 1,123 | 572 | 9,889 | 473 |  | 99 | -10000 | -11000 |  | T | easy |
| pigeon-12 | 1,333 | 660 | 11,796 | 552 |  | 108 | -11000 | -12000 |  | CT | hard |
| pigeon-13 | 1,561 | 754 | 13,871 | 637 |  | 117 | ? | -13000 |  | C | open |
| pigeon-19 | 3,307 | 1,444 | 29,849 | 1,273 |  | 171 | ? | -19000 |  | C | open |
| probportfolio | 302 | 320 | 6,620 | 300 |  | 20 | 16.734246764 | 5 |  | C | hard |
| protfold | 2,112 | 1,835 | 23,491 | 1,835 |  |  | -31 | -41.957447 | 0.01 | R | hard |
| pw-myciel4 | 8,164 | 1,059 | 17,779 | 1,058 | 1 |  | 10 | 0 |  | B | easy |
| qiu | 1,192 | 840 | 3,432 | 48 |  | 792 | -132.873136947 | -931.638845 |  | B | easy |
| queens-30 | 960 | 900 | 93,440 | 900 |  |  | ? | -70.912689 |  | C | open |
| r80x800 | 880 | 1,600 | 3,200 | 800 |  | 800 | ? | 3651.48 |  | C | open |
| rail01 | 46,843 | 117,527 | 392,086 | 117,527 |  |  | -70.5699643 | -92.0873 | 0.002 | R | easy |
| rail02 | 95,791 | 270,869 | 756,228 | 270,869 |  |  | -200.449907667 | -206.6102 | 0.01 | CR | hard |
| rail03 | 253,905 | 758,775 | 1,728,451 | 758,775 |  |  | ? | -920.274 | 0.025 | CR | open |
| rail507 | 509 | 63,019 | 468,878 | 63,009 |  | 10 | 174 | 172.145567 |  | B | easy |
| ramos3 | 2,187 | 2,187 | 32,805 | 2,187 |  |  | ? | 145.8 |  | CR | open |
| ran14x18-disj-8 | 447 | 504 | 10,277 | 252 |  | 252 | 3735 | 3444.421066 |  | T | easy |
| ran14x18 | 284 | 504 | 1,008 | 252 |  | 252 | 3712 | 3016.944354 |  | T | easy |
| ran16x16 | 288 | 512 | 1,024 | 256 |  | 256 | 3823 | 3116.429512 |  | B | easy |
| reblock166 | 17,024 | 1,660 | 39,442 | 1,660 |  |  | $-6.00052 e+08$ | -886882876.965829 |  | T | easy |
| reblock354 | 19,906 | 3,540 | 52,901 | 3,540 |  |  | -39280521.2281657 | -39641692.452292 |  | C | hard |
| reblock420 | 62,800 | 4,200 | 138,670 | 4,200 |  |  | $-5.17793 e+08$ | -886535897.522137 |  | C | hard |
| reblock67 | 2,523 | 670 | 7,495 | 670 |  |  | -34630648.43833169 | -39339910.923037 |  | B | easy |
| rmatr100-p10 | 7,260 | 7,359 | 21,877 | 100 |  | 7,259 | 423 | 360.593308 |  | B | easy |
| rmatr100-p5 | 8,685 | 8,784 | 26,152 | 100 |  | 8,684 | 976 | 762.040054 |  | B | easy |
| rmatr200-p10 | 35,055 | 35,254 | 105,362 | 200 |  | 35,054 | ? | 1550.620783 |  | C | open |


| Name | Rows | Columns | Non-Zeros | Binary | Integer | Continuous | mIP Solution | LP Solution | Att.-level | Sets | Status |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| rmatr200-p20 | 29,406 | 29,605 | 88,415 | 200 |  | 29,405 | 837 | 688.357943 |  | C | hard |
| rmatr200-p5 | 37,617 | 37,816 | 113,048 | 200 |  | 37,616 | 4521 | 3283.653831 |  | C | hard |
| rmine10 | 65,274 | 8,439 | 162,264 | 8,439 |  |  | ? | -1926.86382 |  | C | open |
| rmine14 | 268,535 | 32,205 | 660,346 | 32,205 |  |  | ? | -4310.694704 | 0.002 | C | open |
| rmine21 | 1,441,651 | 162,547 | 3,514,884 | 162,547 |  |  | ? | -10679.2 | 0.01 | CX | open |
| rmine25 | 2,953,849 | 326,599 | 7,182,744 | 326,599 |  |  | ? | -15667.9 | - | CX | open |
| rmine6 | 7,078 | 1,096 | 18,084 | 1,096 |  |  | -457.18614 | -462.305727 |  | B | easy |
| rocll-4-11 | 21,738 | 9,234 | 243,106 | 9,086 |  | 148 | -6.652756 | -11.937162 |  | B | easy |
| rocll-7-11 | 37,215 | 16,101 | 423,661 | 15,851 |  | 250 | ? | -11.964093 |  | C | open |
| rocll-9-11 | 47,533 | 20,679 | 544,031 | 20,361 |  | 318 | ? | -11.972072 |  | C | open |
| rococoB10-011000 | 1,667 | 4,456 | 16,517 | 4,320 | 136 |  | 19449 | 8350.199468 |  | C | hard |
| rococoC10-001000 | 1,293 | 3,117 | 11,751 | 2,993 | 124 |  | 11460 | 7515.271029 |  | B | easy |
| rococoC11-011100 | 2,367 | 6,491 | 30,472 | 6,325 | 166 |  | ? | 9024.205406 |  | CR | open |
| rococoC12-111000 | 10,776 | 8,619 | 48,920 | 8,432 | 187 |  | ? | 27337.357381 |  | C | open |
| roll3000 | 2,295 | 1,166 | 29,386 | 246 | 492 | 428 | 12890 | 11097.127677 |  | B | easy |
| rvb-sub | 225 | 33,765 | 984,143 | 33,763 |  | 2 | ? | 11.206514 |  | C | open |
| satellites1-25 | 5,996 | 9,013 | 59,023 | 8,509 |  | 504 | -5 | -20 | 0.016 | B | easy |
| satellites2-60-fs | 16,516 | 35,378 | 125,048 | 34,324 |  | 1,054 | -19 | -30 | 0.051 | R | easy |
| satellites2-60 | 20,916 | 35,378 | 283,668 | 34,324 |  | 1,054 | -19 | -30 | 0.143 | CRU | hard |
| satellites3-40-fs | 35,553 | 81,681 | 291,161 | 79,961 |  | 1,720 | ? | -39 | 0.292 | CRU | open |
| satellites3-40 | 44,804 | 81,681 | 698,176 | 79,961 |  | 1,720 | ? | -39 | 0.3 | CRU | open |
| sct1 | 12,154 | 22,886 | 105,571 | 9,044 | 1,268 | 12,574 | ? | -218.139003 |  | C | open |
| sct32 | 5,440 | 9,767 | 109,654 | 6,396 | 1,332 | 2,039 | ? | -62.990833 |  | C | open |
| sct5 | 13,304 | 37,265 | 147,037 | 20,702 | 2,302 | 14,261 | ? | -228.176552 |  | CR | open |
| set3-10 | 3,747 | 4,019 | 13,747 | 1,424 |  | 2,595 | ? | 788.890655 |  | C | open |
| set3-15 | 3,747 | 4,019 | 13,747 | 1,424 |  | 2,595 | ? | 8364.040745 |  | C | open |
| set3-20 | 3,747 | 4,019 | 13,747 | 1,424 |  | 2,595 | ? | 10347.381087 |  | C | open |
| seymour | 4,944 | 1,372 | 33,549 | 1,372 |  |  | 423 | 403.846474 |  | C | hard |
| seymour-disj-10 | 5,108 | 1,209 | 64,704 | 1,209 |  |  | ? | 280.817818 |  | C | open |
| shipsched | 45,554 | 13,594 | 121,571 | 10,549 |  | 3,045 | ? | 0 |  | C | open |
| shs1023 | 133,944 | 444,625 | 1,044,725 | 1,296 | 440,899 | 2,430 | ? | 12121.358113 | 0.001 | C | open |
| siena1 | 2,220 | 13,741 | 258,915 | 11,775 |  | 1,966 | ? | 10163179.229002 |  | C | open |
| sing161 | 455,631 | 770,102 | 2,072,500 | 733,244 |  | 36,858 | ? | 19071259.113927 |  | C | open |
| sing245 | 143,161 | 235,146 | 652,817 | 220,692 |  | 14,454 | ? | 25024015.754083 | 0.001 | CR | open |
| sing2 | 28,891 | 31,630 | 149,712 | 23,377 |  | 8,253 | ? | 17150914.71694 |  | C | open |
| sing359 | 437,116 | 713,762 | 1,975,605 | 674,643 |  | 39,119 | ? | 22534478.962498 | 0.001 | CR | open |
| sp97ar | 1,761 | 14,101 | 290,968 | 14,101 |  |  | 660705645.76 | 652560391.247564 |  | C | hard |
| sp98ic | 825 | 10,894 | 316,317 | 10,894 |  |  | 449144758.4 | 444277568.934152 |  | B | easy |
| sp98ir | 1,531 | 1,680 | 71,704 | 871 | 809 |  | 219676790.4 | 216663444.589936 |  | B | easy |
| splan1 | 572,800 | 1,317,382 | 5,233,840 | 90,810 | 1,978 | 1,224,594 | ? | -201899 | - | CXU | open |
| stockholm | 57,346 | 20,644 | 171,076 | 962 |  | 19,682 | ? | 0.755613 | 0.001 | C | open |
| stp3d | 159,488 | 204,880 | 662,128 | 204,880 |  |  | 493.71965 | 481.877786 | 0.006 | CR | hard |
| sts405 | 27,270 | 405 | 81,810 | 405 |  |  | ? | 135 |  | C | open |
| sts729 | 88,452 | 729 | 265,356 | 729 |  |  | ? | 243 | 0.001 | CR | open |
| swath | 884 | 6,805 | 34,965 | 6,724 |  | 81 | 467.407491 | 334.496858 |  | C | hard |
| t1717 | 551 | 73,885 | 325,689 | 73,885 |  |  | ? | 134531.021428 |  | C | open |
| t1722 | 338 | 36,630 | 133,096 | 36,630 |  |  | ? | 98815.407611 |  | C | open |
| tanglegram1 | 68,342 | 34,759 | 205,026 | 34,759 |  |  | 5182 | 0 |  | B | easy |
| tanglegram 2 | 8,980 | 4,714 | 26,940 | 4,714 |  |  | 443 | 0 |  | B | easy |


| Name | Rows | Columns | Non-Zeros | Binary | Integer | Continuous | MIP Solution | LP Solution | Att.-level | Sets | Status |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| timtab1 | 171 | 397 | 829 | 64 | 107 | 226 | 764772 | 28694 |  | BT | easy |
| toll-like | 4,408 | 2,883 | 13,224 | 2,883 |  |  | ? | 0 |  | C | open |
| transportmoment | 9,616 | 9,685 | 29,541 | 2,456 |  | 7,229 | ? | -70929535815.37999 | 0.325 | CU | open |
| triptim1 | 15,706 | 30,055 | 515,436 | 20,451 | 9,597 | 7 | 22.8681 | 22.868088 | 0.01 | BP | easy |
| triptim2 | 14,427 | 27,326 | 521,898 | 20,771 | 6,548 | 7 | ? | 10.866359 | 0.01 | CR | open |
| triptim3 | 14,939 | 28,440 | 524,124 | 21,621 | 6,812 | 7 | ? | 13.511741 | 0.011 | CR | open |
| tw-myciel4 | 8,146 | 760 | 27,961 | 759 | 1 |  | ? | 3.838028 |  | C | open |
| uc-case11 | 51,438 | 34,134 | 202,042 | 3,898 | 302 | 29,934 | ? | 611267.013004 | 0.001 | C | open |
| uc-case3 | 52,003 | 37,749 | 273,618 | 11,256 |  | 26,493 | ? | 7181.264177 |  | C | open |
| uct-subprob | 1,973 | 2,256 | 10,147 | 379 |  | 1,877 | 314 | 242 |  | c | hard |
| umts | 4,465 | 2,947 | 23,016 | 2,802 | 72 | 73 | 30090328 | 29129565.161344 |  | T | easy |
| unitcal_7 | 48,939 | 25,755 | 127,595 | 2,856 |  | 22,899 | 19635558.2440195 | 19387553.381271 | 0.002 | B | easy |
| usAbbrv-8-25_70 | 3,291 | 2,312 | 9,628 | 1,681 |  | 631 | ? | 95 |  | C | open |
| van | 27,331 | 12,481 | 487,296 | 192 |  | 12,289 | ? | 1.72352 |  | C | open |
| vpphard2 | 198,450 | 199,999 | 648,340 | 199,999 |  |  | ? | 0 |  | C | open |
| vpphard | 47,280 | 51,471 | 372,305 | 51,471 |  |  | 5 | 0 |  | B | easy |
| wachplan | 1,553 | 3,361 | 89,361 | 3,360 | 1 |  | -8 | -9 |  | T | easy |
| wnq-n100-mw99-14 | 656,900 | 10,000 | 1,333,400 | 10,000 |  |  | ? | 185.263158 |  | CT | open |
| zib01 | 5,887,041 | 12,471,400 | 49,877,768 | 12,471,400 |  |  | ? | 64697 | - | CX | open |
| zib02 | 9,049,868 | 37,709,944 | 146,280,582 | 37,709,944 |  |  | infeasible | infeasible | - | CIX | hard |
| zib54-UUE | 1,809 | 5,150 | 15,288 | 81 |  | 5,069 | 10334015.82 | 3875862.862589 |  | B | easy |

Table 7: Results for the Benchmark-Set using 1 thread, time limit 1 hour. Time is given in seconds, if the time limit was reached the optimality gap is given instead. Italic indicates that the solution did not pass the feasibility check. Best lists the minimum number of nodes and time over all solvers providing a feasible solution. Nodes and Time may have not been taken from the same solver. VS lists the variablility score of the instance as described in Section 5.2. Higher numbers indicate higher performance variability. The additional test sets containing each instance, other than benchmark, are listed in Sets

| Name | Sets | CPLEX |  | XPRESS |  | GUROBI |  | CBC |  | SCIP/SPX |  | Best |  | VS |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Nodes | Time | Nodes | Time | Nodes | Time | Nodes | Time | Nodes | Time | Nodes | Time |  |
| 30n20b8 |  | 96.7k | 20.3\% | 2.3M | 74.8\% | 87.7k | 804 | 213.1k | 60.2\% | 8.2 k | 332.5\% | 87654 | 804 |  |
| acc-tight5 | RP | 9 | 5 | 487 | 75 | 1.4k | 121 | 1.2 k | 303 | 497 | 137 | 9 | 5 | 0.72 |
| aflow40b |  | 98.3k | 376 | 134.8k | 399 | 166.7k | 738 | 367.9k | 5.3\% | 278.7k | 2400 | 98349 | 376 | 0.39 |
| air04 |  | 225 | 6 | 121 | 12 | 125 | 10 | 456 | 55 | 76 | 65 | 76 | 6 | 0.14 |
| app1-2 |  | 30.0k | 1420 | 33.6k | 125 | 64 | 65 | 2.7k | inf\% | 1 | inf\% | 64 | 65 |  |
| ash608gpia-3col | 1 | 9 | 53 | 15 | 180 | 5 | 221 | 1 | 567 | 7 | 47 | 1 | 47 | 0.20 |
| bab5 |  | 55.1k | 1722 | 27.3k | 0.7\% | 9.5k | 662 | 22.7k | inf\% | 7.5k | 1.4\% | 9470 | 662 |  |
| beasleyC3 |  | 544.9k | 1.1\% | 11.2 k | 89 | 729 | 13 | 170.1k | 21.6\% | 504.8k | 22.3\% | 729 | 13 |  |
| biella 1 |  | 11.2k | 899 | 5.5k | 424 | 1.2k | 238 | 16.0k | 0.0\% | 1.7 k | 682 | 1162 | 238 | 0.29 |
| bienst2 |  | 70.1k | 63 | 101.8k | 121 | 97.6k | 33 | 90.8k | 1312 | 89.6k | 290 | 70054 | 33 | 0.21 |
| binkar10_1 |  | 8.7 k | 15 | 5.5k | 14 | 51.5k | 35 | 59.0k | 481 | 199.4k | 406 | 5461 | 14 | 0.50 |
| bley_x11 |  | 43 | 17 | 1 | 8 | 1 | 17 | 50 | 891 | 38 | 305 | 1 | 8 | 0.26 |
| bnatt350 | RP | 16.5k | 3408 | 82.9k | inf\% | 36.1 k | inf\% | 7.4k | inf\% | 6.6 k | 1191 | 6567 | 1191 | 0.50 |
| core2536-691 |  | 748 | 57 | 183 | 81 | 771 | 194 | 869 | 275 | 308 | 377 | 183 | 57 | 0.67 |
| cov1075 |  | 4.7 k | 19 | 185.9k | 8.7\% | 342 | 6 | 138.6k | 8.9\% | 529.5k | 8.9\% | 342 | 6 | 0.06 |
| csched010 |  | 400.3k | 3.9\% | 136.3k | 1176 | 621.6k | 2.8\% | 549.1k | 18.9\% | 466.4k | 5.2\% | 136309 | 1176 | 0.26 |
| danoint |  | 528.9k | 2.4\% | 514.7k | 3398 | 819.9k | 3.0\% | 210.1k | 2.7\% | 507.6k | 3.1\% | 514711 | 3398 | 0.09 |
| dfn-gwin-UUM |  | 36.4 k | 72 | 150.9k | 264 | 242.3k | 225 | 332.5k | 1132 | 14.5k | 54 | 14491 | 54 | 0.23 |
| eil33-2 |  | 10.8k | 58 | 15.7k | 125 | 10.1k | 110 | 8.8k | 307 | 11.1 k | 180 | 8792 | 58 | 0.15 |
| eilB101 |  | 10.5k | 160 | 2.3k | 80 | 22.0k | 231 | 23.8k | 1570 | 3.0k | 680 | 2305 | 80 | 0.23 |
| enlight13 |  | 84.2k | 397 | 39.1k | 13 | 62.0k | 307 | 237.6k | inf\% | 622.6k | 413 | 39107 | 13 | 1.22 |
| enlight14 | 1 | 663.8k | inf\% | 142.0k | 42 | 571.5k | inf\% | 183.1k | inf\% | 738.2k | 665 | 142035 | 42 | 0.82 |
| ex9 | P | 1 | 2102 | 1 | 17 | 1 | 227 | 1 | inf\% | 1 | 85 | 1 | 17 | 0.11 |
| glass4 | T | 4.4 M | 1537 | 1.7M | 26.6\% | 496.3k | 280 | 221.8k | 47.5\% | 4.0M | 100.0\% | 496349 | 280 |  |
| gmu-35-40 | T | 1.6M | 893 | 3.6M | 0.0\% | 13.0M | 1898 | 1.8M | 0.0\% | 4.9 M | 0.0\% | 1578834 | 893 |  |
| iis-100-0-cov |  | 386.8k | 3233 | 83.4 k | 1882 | 144.0k | 1515 | 30.1k | 12.1\% | 103.9k | 1808 | 83425 | 1515 | 0.09 |
| iis-bupa-cov |  | 154.1k | 8.6\% | 54.1k | 7.5\% | 164.2k | 5.9\% | 25.2k | 11.3\% | 85.0k | 10.0\% | - | - | 0.06 |
| iis-pima-cov |  | 27.0k | 869 | 17.2k | 1014 | 7.9k | 318 | 15.9k | 10.2\% | 11.1k | 864 | 7917 | 318 | 0.21 |
| lectsched-4-obj |  | 1.5k | 9 | 1 | 1 | 108 | 5 | 8.4k | 1544 | 9.4 k | 265 | 1 | 1 | 1.04 |
| m100n500k4r1 | P | 1.8M | 4.2\% | 1.6M | 4.2\% | 4.3M | 4.2\% | 1.0M | 4.2\% | 3.9M | 4.2\% | - | - |  |
| macrophage |  | 8.6k | 131 | 641 | 43 | 418.2k | 1.4\% | 6.1k | 20.6\% | 308.1k | 27.1\% | 641 | 43 |  |
| map18 | R | 809 | 190 | 513 | 147 | 1.1k | 203 | 1.2 k | 1485 | 544 | 764 | 513 | 147 | 0.15 |
| map20 |  | 575 | 138 | 521 | 177 | 1.2k | 177 | 1.0k | 1339 | 550 | 580 | 521 | 138 | 0.20 |

Table 7 continued

| Name | Sets | CPLEX |  | XPRESS |  | GUROBI |  | CBC |  | SCIP/SPX |  | Best |  | VS |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Nodes | Time | Nodes | Time | Nodes | Time | Nodes | Time | Nodes | Time | Nodes | Time |  |
| mcsched |  | 111.8k | 479 | 427.7k | 2769 | 28.6k | 198 | 117.4k | 2.4\% | 23.1k | 337 | 23111 | 198 | 0.16 |
| mik-250-1-100-1 |  | 118.1k | 14 | 79.7k | 37 | 97.2k | 18 | 441.8k | 0.5\% | 415.1k | 176 | 79739 | 14 | 0.05 |
| mine-166-5 |  | 5.4 k | 24 | 249 | 7 | 6.7 k | 24 | 4.7k | 157 | 6.1 k | 76 | 249 | 7 | 0.24 |
| mine-90-10 |  | 345.9 k | 1350 | 142.5k | 216 | 1.1 M | 1144 | 130.8k | 1965 | 56.2 k | 264 | 56177 | 216 | 0.75 |
| msc98-ip | R | 2.4 k | 5.0\% | 21.0 k | 1.3\% | 4.7k | 700 | 294 | inf\% | 118 | inf\% | 4734 | 700 |  |
| mspp16 | X | 53 | 635 | 1 | 253 | 1 | 1840 |  |  |  |  | 1 | 253 |  |
| mzzv11 |  | 869 | 51 | 69 | 8 | 6 | 17 | 739 | 187 | 2.4 k | 591 | 6 | 8 | 0.21 |
| n3div36 |  | 286.3k | 6.0\% | 190.3k | 1.2\% | 501.7k | 3358 | 120.4k | 0.5\% | 84.7k | 11.2\% | 501686 | 3358 |  |
| n3seq24 |  | 491 | 61 | 1 | 181 | 40.8k | 677 | 268 | 1495 | 348 | 0.4\% | 1 | 61 |  |
| n4-3 |  | 8.5 k | 328 | 47.6k | 1979 | 120.6k | 2110 | 293.2k | 18.7\% | 81.5k | 1052 | 8467 | 328 | 0.34 |
| neos-1109824 |  | 8.7k | 30 | 2.1k | 14 | 10.5k | 109 | 22.0k | 428 | 10.8k | 119 | 2071 | 14 | 0.30 |
| neos-1337307 |  | 67.5k | 0.1\% | 439.5k | 0.0\% | 220.7k | 0.0\% | 12.4 k | 0.1\% | 167.4k | 0.0\% | - | - |  |
| neos-1396125 |  | 26.4k | 82 | 12.6k | 79 | 8.2k | 135 | 54.9k | 24.0\% | 49.8k | 3338 | 8175 | 79 | 0.25 |
| neos-1601936 | R | 6.3 k | 1759 | 695 | 31 | 333 | 56 | 8.9 k | 996 | 8.9 k | 66.7\% | 333 | 31 | 0.81 |
| neos-476283 |  | 1.0k | 243 | 777 | 149 | 515 | 142 | 710 | 1561 | 453 | 322 | 453 | 142 | 0.16 |
| neos-686190 |  | 4.3k | 29 | 6.7 k | 52 | 5.3k | 47 | 5.5k | 154 | 5.6k | 95 | 4298 | 29 | 0.27 |
| neos-849702 | P | 44.9k | inf\% | 43.9k | 409 | 104.6k | 1066 | 152.6k | inf\% | 244.3k | inf\% | 43941 | 409 | 1.59 |
| neos-916792 |  | 122.8k | 569 | 42.1k | 208 | 67.2k | 1525 | 106.0k | 4.3\% | 67.4k | 367 | 42060 | 208 | 2.23 |
| neos-934278 |  | 101 | 230 | 199 | 82 | 1 | 82 | 400 | 649 | 2.1k | 2.9\% | 1 | 82 |  |
| neos13 |  | 4.1k | 58 | 65 | 26 | 711 | 47 | 28.1k | 2.7\% | 283 | 657 | 65 | 26 | 1.72 |
| neos18 |  | 13.7k | 27 | 20.0k | 55 | 13.7k | 65 |  |  | 9.9 k | 68 | 9854 | 27 | 0.39 |
| net12 | R | 2.5 k | 22.1\% | 2.5 k | 92 | 1.3 k | 290 | 1.4 k | 35.3\% | 5.0k | 57.6\% | 1348 | 92 | 0.33 |
| netdiversion |  | 28 | 74 | 9 | 76 | 123 | 628 | 847 | 1.4\% | 51 | inf\% | 9 | 74 |  |
| newdano |  | 170.6k | 34.7\% | 372.4 k | 4.8\% | 683.3k | 11.0\% | 81.9k | 23.7\% | 1.5M | 31.0\% | - | - | 0.21 |
| noswot | T | 6.9 M | 950 | 1.7 M | 344 | 566.3k | 72 | 1.0M | 2194 | 605.0k | 210 | 566273 | 72 | 0.34 |
| ns1208400 |  | 2.9 k | 88 | 221.6k | inf\% | 623 | 81 | 57.8k | inf\% | 3.0 k | 526 | 623 | 81 | 0.70 |
| ns1688347 |  | 7.3k | 139 | 2.5 k | 25 | 868 | 31 | 3.6k | inf\% | 4.2 k | 1027 | 868 | 25 | 0.79 |
| ns1758913 |  | 24 | 158 | 1 | 37 | 1 | 44 | 1 | inf\% | 1 | inf\% | 1 | 37 |  |
| ns1766074 | IT | 870.3k | 133 | 520.8k | 141 | 1.1 M | 110 | 189.9k | 592 | 945.4k | 668 | 189900 | 110 | 0.12 |
| ns1830653 |  | 10.9k | 206 | 31.9 k | 394 | 26.9k | 427 | 20.7k | 95.0\% | 47.0k | 638 | 10915 | 206 | 0.42 |
| opm2-z7-s2 |  | 2.0k | 282 | 2.5 k | 501 | 639 | 67 | 3.5k | 1039 | 1.5k | 660 | 639 | 67 | 0.17 |
| pg5_34 |  | 107.8k | 244 | 88.6k | 376 | 187.0k | 439 | 97.3k | 1787 | 257.0k | 1247 | 88573 | 244 | 0.13 |
| pigeon-10 | T | 5.8M | 985 | 7.8M | 2561 | 4.0M | 558 | 685.7k | 11.1\% | 3.7M | 11.1\% | 3984370 | 558 |  |
| pw-myciel4 |  | 33.1 k | 159 | 108.6k | 1121 | 4.7M | 11.1\% | 35.5k | 66.7\% | 309.9k | 42.9\% | 33124 | 159 | 0.51 |
| qiu |  | 2.2 k | 11 | 8.3k | 55 | 3.4 k | 18 | 13.1k | 222 | 14.5k | 98 | 2157 | 11 | 0.19 |
| rail507 |  | 3.5k | 207 | 2.8k | 911 | 1.5k | 123 | 7.6k | 1458 | 1.3k | 1252 | 1259 | 123 |  |
| ran16×16 |  | 64.3k | 73 | 69.9k | 88 | 81.8k | 76 | 195.6k | 785 | 344.3k | 291 | 64322 | 73 | 0.20 |
| reblock67 |  | 588.1k | 766 | 234.5k | 342 | 636.6k | 651 | 305.1k | 3275 | 139.6k | 373 | 139635 | 342 | 0.32 |
| rmatr100-p10 |  | 2.0 k | 76 | 917 | 56 | 1.0k | 28 | 2.9k | 157 | 863 | 322 | 863 | 28 | 0.08 |
| rmatr100-p5 |  | 1.2 k | 94 | 681 | 107 | 1.2 k | 107 | 1.4k | 167 | 419 | 991 | 419 | 94 | 0.12 |
| rmine6 |  | 917.2k | 1979 | 416.7k | 1032 | 404.4k | 476 | 459.9k | 0.1\% | 546.9k | 0.1\% | 404406 | 476 | 0.19 |


| Name | Sets | CPLEX |  | XPRESS |  | GUROBI |  | CBC |  | SCIP/SPX |  | Best |  | VS |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Nodes | Time | Nodes | Time | Nodes | Time | Nodes | Time | Nodes | Time | Nodes | Time |  |
| rocll-4-11 |  | 175.6k | 271 | 47.3k | 318 | 33.8k | 205 | 19.2k | 0.3\% | 27.6k | 381 | 27610 | 205 | 0.32 |
| rococoC10-001000 |  | 45.5k | 597 | 35.9k | 420 | 1.7 M | 0.4\% | 36.3 k | 1345 | 462.5k | 2493 | 35937 | 420 | 0.42 |
| roll3000 |  | 31.3 k | 138 | 1.9k | 16 | 6.8 k | 68 | 34.5k | 2284 | 593.9k | 3399 | 1947 | 16 | 0.54 |
| satellites1-25 |  | 3.5k | 200 | 2.3k | 120 | 634 | 102 | 14.5k | $1582{ }^{2}$ | 8.6k | 197.0\% | 634 | 102 | 0.53 |
| sp98ic |  | 196.3k | 1166 | 23.3k | 563 | 32.8k | 289 | 86.5k | 0.3\% | 35.0k | 3.5\% | 23317 | 289 |  |
| sp98ir |  | 6.5k | 39 | 2.6k | 38 | 6.9 k | 126 | 6.9 k | 103 | 4.8 k | 78 | 2641 | 38 | 0.20 |
| tanglegram1 |  | 31 | 1791 | 35 | 157 | 23 | 287 | 203 | inf\% | 1 | 9954.4\% | 23 | 157 |  |
| tanglegram2 |  | 3 | 59 | 3 | 2 | 7 | 17 | 302 | 216 | 15 | 1306 | 3 | 2 | 0.41 |
| timtab1 | T | 855.6k | 797 | 307.8k | 373 | 3.4 M | 1568 | 233.4k | 24.8\% | 700.0k | 415 | 307773 | 373 | 0.43 |
| triptim1 | P | 1 | 39 | 33 | 60 | 1 | 59 | 1 | 123 | 118 | 0.1\% | 1 | 39 | 0.48 |
| unitcal_7 |  | 2.0 k | 108 | 39 | 18 | 3.1k | 189 | 3.3k | 1511 | 12.3k | 1479 | 39 | 18 | 1.05 |
| vpphard |  | 13.6k | 2481 | 149.3k | inf\% | 12.8k | inf\% | 6.4 k | inf\% | 4.3k | inf\% | 13580 | 2481 |  |
| zib54-UUE |  | 22.1k | 1818 | 164.0k | 1527 | 31.3k | 2397 | 79.3k | 6.5\% | 431.0k | 9.9\% | 22093 | 1527 | 0.28 |

[^5]Table 8: Results for the Benchmark-Set using 12 cores, time limit 1 hour. Time is given in seconds, if the time limit was reached the optimality gap is given instead. Italic indicates that the solution did not pass the feasibility check. Best lists the minimum number of nodes and time over all solvers providing a feasible solution. Nodes and Time may have not been taken from the same solver. $S U$ gives the speedup as the ratio between the best solution times for 1 thread and 12 threads. The additional test sets containing each instance, other than benchmark, are listed in Sets

| Name | Sets | CPLEX |  | XPRESS |  | GUROBI |  | CBC |  | $\mathrm{UG}[\mathrm{SCIP} / \mathrm{SPX}]$ |  | Best |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Nodes | Time | Nodes | Time | Nodes | Time | Nodes | Time | Nodes | Time | Nodes | Time | SU |
| 30n20b8 |  | 158.7k | 401 | 7.9M | 19.4\% | 61.2k | 173 | abort ${ }^{1}$ |  | 361 | 200.0\% | 61204 | 173 | 4.6 |
| acc-tight5 | RP | 53 | 6 | 743 | 13 | 235 | 13 | abort ${ }^{1}$ |  | 151 | 66 | 53 | 6 | 0.8 |
| aflow 40 b |  | 67.1 k | 45 | 218.8k | 139 | 535.9k | 159 |  |  | 28.9k | 233 | 28947 | 45 | 8.4 |
| air04 |  | 765 | 9 | 122 | 11 | 214 | 9 | 1.1 k | 34 | 35 | 70 | 35 | 9 | 0.7 |
| app1-2 |  | 378.0k | 1545 | 330.3k | 276 | 36 | 61 | 10.9k | 3443 | 282 | 490.3\% | 36 | 61 | 1.1 |
| ash608gpia-3col | 1 | 1 | 14 | 15 | 203 | 5 | 222 | 1 | 571 | 7 | 94 | 1 | 14 | 3.4 |
| bab5 |  | 230.5k | 1048 | 350.6k | 0.1\% | 25.1 k | 277 | 465.7 k | 8.6\% | 2.0 k | 0.9\% | 25086 | 277 | 2.4 |
| beasleyC3 |  | 1.6 M | 1088 | 31.7 k | 29 | 2.2 k | 11 | 1.5 M | 21.5\% | 557.4 k | 22.3\% | 2248 | 11 | 1.2 |
| biella1 |  | 10.8k | 101 | 17.0k | 128 | 2.8k | 178 | 22.0k | 371 | 1.5 k | 723 | 1496 | 101 | 2.4 |
| bienst2 |  | 72.0k | 9 | 99.5k | 14 | 102.6k | 5 | 104.7k | 104 | 115.5k | 128 | 71998 | 5 | 6.6 |
| binkar10_1 |  | 16.5k | 6 | 9.5k | 4 | 2.5 k | 1 | 36.6k | 67 | 28.3k | 35 | 2516 | 1 | 14.0 |
| bley_x11 |  | 18 | 12 | 1 | 6 | 1 | 17 | 21 | 563 | 1 | 178 | 1 | 6 | 1.3 |
| bnatt350 | RP | 12.5k | 357 | 256.0k | 1237 | 128.7k | 1650 | 108.3k | inf\% | 1.4 k | 344 | 1398 | 344 | 3.5 |
| core2536-691 |  | 1.1 k | 47 | 639 | 49 | 3.6k | 122 | 1.1 k | 125 | 54 | 359 | 54 | 47 | 1.2 |
| cov1075 |  | 8.7 k | 6 | 1.6M | 3415 | 342 | 3 | 748.2 k | 7.0\% | 1.6 M | 1601 | 342 | 3 | 2.0 |
| csched010 |  | 590.4k | 391 | 280.4k | 319 | 2.3 M | 1158 | 4.8M | 14.1\% | 1.0 M | 1307 | 280429 | 319 | 3.7 |
| danoint |  | 472.3k | 239 | 479.8k | 336 | 1.6M | 598 | abort ${ }^{1}$ |  | 754.8k | 599 | 472286 | 239 | 14.2 |
| dfn-gwin-UUM |  | 31.2 k | 12 | 181.2k | 65 | 245.7k | 23 | 91.1k | 73 | 12.2 k | 57 | 12202 | 12 | 4.5 |
| eil33-2 |  | 10.6k | 16 | 10.7k | 60 | 8.4 k | 38 | 9.5 k | 175 | 8.1 k | 163 | 8145 | 16 | 3.6 |
| eilB101 |  | 6.2 k | 18 | 2.8 k | 34 | 41.7k | 53 | 28.5k | 231 | 2.2 k | 445 | 2202 | 18 | 4.4 |
| enlight13 |  | 1.5M | 273 | 106.6k | 6 | 1.5M | 274 | abort ${ }^{1}$ |  | 3.1 M | 931 | 106585 | 6 | 2.2 |
| enlight14 | 1 | 7.3M | 2617 | 234.6k | 13 | 14.7M | inf\% | 2.3M | inf\% | 114.7k | 193 | 114658 | 13 | 3.2 |
| ex9 | P | 1 | 376 | 1 | 16 | 1 | 226 | 1 | inf\% | 1 | 87 | 1 | 16 | 1.1 |
| glass4 | T | 2.2 M | 20.8\% ${ }^{2}$ | 6.5 M | 718 | 1.6M | 45 | abort ${ }^{1}$ |  | 4.3M | 570 | 1622146 | 45 | 6.2 |
| gmu-35-40 | T | 1.2 M | 55 | 19.6M | 0.0\% | 103.2M | 3482 | abort ${ }^{1}$ |  | abort ${ }^{3}$ |  | 1240043 | 55 | 16.2 |
| iis-100-0-cov |  | 147.6k | 149 | 88.2k | 257 | 149.8k | 215 | 113.2 k | 7.5\% | 50.0k | 718 | 49991 | 149 | 10.2 |
| iis-bupa-cov |  | 770.5k | 1576 | 300.3k | 1246 | 224.1k | 612 | 355.3 k | 5.6\% | 126.8k | 1350 | 126850 | 612 | >5.9 |
| iis-pima-cov |  | 30.8k | 142 | 36.2k | 244 | 20.3 k | 149 | 32.3k | 695 | 7.3k | 889 | 7304 | 142 | 2.2 |
| lectsched-4-obj |  | 5.7 k | 8 | 393 | 2 | 547 | 4 | 12.7 k | 170 | 697 | 121 | 393 | 2 | 0.5 |
| m100n500k4r1 | P | 19.8M | 4.2\% | 12.3M | 4.2\% | 47.8M | 4.2\% | 3.8M | 4.2\% | 8.0M | 4.2\% | - | - | - |
| macrophage |  | 248.1k | 355 | 725 | 29 | 1.6M | 1102 | 159.6k | 15.8\% | 4.4 k | 27.0\% | 725 | 29 | 1.5 |
| map18 | R | 1.1 k | 124 | 2.0 k | 78 | 1.5k | 48 | 1.3 k | 733 | 375 | 1531 | 375 | 48 | 3.1 |
| map20 |  | 1.1k | 103 | 3.1k | 113 | 1.4k | 36 | 1.1k | 625 | 332 | 1292 | 332 | 36 | 3.8 |


| Name | Sets | CPLEX |  | XPRESS |  | GUROBI |  | CBC |  | UG[SCIP/SPX] |  | Best |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Nodes | Time | Nodes | Time | Nodes | Time | Nodes | Time | Nodes | Time | Nodes | Time | SU |
| mcsched |  | 117.8k | 58 | 324.0k | 263 | 26.7k | 50 | 76.2k | 389 | 15.5k | 269 | 15487 | 50 | 4.0 |
| mik-250-1-100-1 |  | 46.1k | 2 | 77.1k | 8 | 195.5k | 5 | 256.5k | 210 | 96.1k | 19 | 46052 | 2 | 7.0 |
| mine-166-5 |  | 6.2 k | 9 | 253 | 7 | 24.0k | 18 | 2.0k | 92 | 2.6k | 67 | 253 | 7 | 1.0 |
| mine-90-10 |  | 314.0k | 124 | 172.2k | 44 | 1.4 M | 270 | 120.0k | 320 | 63.2k | 154 | 63248 | 44 | 4.9 |
| msc98-ip | R | 4.7 k | 1342 | 169.9k | 0.7\% | 6.6k | 215 | 1.1k | inf\% | 29 | 57.0\% | 4737 | 215 | 3.3 |
| mspp16 | X | 22 | 659 | 1 | 254 | 1 | 1844 |  |  |  |  | 1 | 254 | 1.0 |
| mzzv11 |  | 828 | 25 | 141 | 8 | 1 | 13 | 621 | 98 | 2.1k | 850 | 1 | 8 | 1.0 |
| n3div36 |  | 2.1 M | 3.6\% | 578.5k | 3268 | 1.3M | 1342 | 155.4k | 1167 | 50.1 k | 11.0\% | 155362 | 1167 | 2.9 |
| n3seq24 |  | 539 | 69 | 1 | 183 | 3.1 k | 187 | 599 | 1243 | 11 | 20.0\% | 1 | 69 | 0.9 |
| n4-3 |  | 12.7k | 116 | 75.7k | 359 | 65.5k | 224 | 808.6k | 16.1\% | 20.1k | 441 | 12681 | 116 | 2.8 |
| neos-1109824 |  | 11.1k | 9 | 2.2 k | 6 | 3.0k | 3 | 19.7k | 72 | 4.4 k | 169 | 2167 | 3 | 4.7 |
| neos-1337307 |  | 252.2k | 1024 | 818.7k | 1094 | 638.9k | 1051 | 175.5k | 0.0\% | 1.2M | 0.1\% | 252150 | 1024 | >3.5 |
| neos-1396125 |  | 96.6k | 31 | 34.1 k | 50 | 28.2 k | 25 | 126.3k | 521 | 23.9k | 1278 | 23883 | 25 | 3.2 |
| neos-1601936 | R | 1.6k | 273 | 2.5 k | 19 | 4.8k | 213 | 537.4k | 200.0\% | 2.0k | 1223 | 1558 | 19 | 1.6 |
| neos-476283 |  | 832 | 143 | 537 | 104 | 905 | 106 | 408 | 1169 | 486 | 878 | 408 | 104 | 1.4 |
| neos-686190 |  | 6.3k | 11 | 17.2k | 24 | 10.0k | 20 | 4.6k | 43 | 2.5k | 81 | 2533 | 11 | 2.6 |
| neos-849702 | P | 241.0k | 1685 | 11.9k | 19 | 1.8M | 3160 | 107.2k | 187 | 25.6k | 412 | 11877 | 19 | 21.5 |
| neos-916792 |  | 98.9k | 83 | 205.5k | 210 | 69.8k | 183 | 467.9k | 7.1\% | 898.4k | 15.7\% | 69764 | 83 | 2.5 |
| neos-934278 |  | 606 | 151 | 4.5k | 119 | 1 | 82 |  |  | 58 | 4.0\% | 1 | 82 | 1.0 |
| neos13 |  | 3.9k | 33 | 23 | 14 | 2.1k | 55 | 8.5k | 563 | 510 | 655 | 23 | 14 | 1.9 |
| neos18 |  | 7.9k | 5 | 24.8 k | 10 | 14.3k | 20 | 28.4 k | 224 | 6.3k | 65 | 6293 | 5 | 5.4 |
| net12 | R | 3.5k | 562 | 909 | 11 | 4.1k | 229 | 2.2 k | 1010 | 1.7 k | 44.9\% | 909 | 11 | 8.4 |
| netdiversion |  | 27 | 96 | 17 | 67 | 54 | 550 | 229 | 1652 | 15 | inf\% | 17 | 67 | 1.1 |
| newdano |  | 938.0k | 1321 | 797.7k | 506 | 950.0k | 373 | 741.4k | 1197 | 3.4 M | 924 | 741404 | 373 | $>9.7$ |
| noswot | T | 1.6 M | 28 | 2.1 M | 94 | 382.4k | 7 | 788.5k | 182 | 1.5 M | 191 | 382411 | 7 | 10.3 |
| ns1208400 |  | 8.6k | 248 | 2.0 M | inf\% | 3.1k | 47 | 835.8k | inf\% | 141.3k | inf\% | 3142 | 47 | 1.7 |
| ns1688347 |  | 2.5k | 23 | 2.9k | 6 | 1.3 k | 20 | 29.2k | 34.7\% | 23.4k | 671 | 1271 | 6 | 4.2 |
| ns1758913 |  | 1 | 118 | 1 | 45 | 1 | 44 | 1 | inf\% | 1 | inf\% | 1 | 44 | 0.8 |
| ns1766074 | IT | 845.6k | 18 | 521.9k | 22 | 1.1 M | 14 | 191.0k | 75 | 925.5k | 2366 | 191024 | 14 | 7.9 |
| ns1830653 |  | 12.0k | 35 | 20.0k | 40 | 53.0k | 284 | 22.8k | 237 | 22.5k | 308 | 12003 | 35 | 5.9 |
| opm2-z7-s2 |  | 6.5k | 236 | 2.8k | 374 | 868 | 42 | 1.2 k | 459 | 1.2 k | 1572 | 868 | 42 | 1.6 |
| pg5_34 |  | 108.1k | 43 | 108.4k | 62 | 156.0k | 50 | 57.6k | 190 | 87.9k | 377 | 57638 | 43 | 5.7 |
| pigeon-10 | T | 5.8 M | 118 | 9.2 M | 399 | 3.4 M | 51 |  |  | 1.6M | 11.1\% | 3405798 | 51 | 10.9 |
| pw-myciel4 |  | 10.9k | 15 | 75.3k | 93 | 711.5k | 126 | 268.6k | 3351 | 434.3k | 1242 | 10893 | 15 | 10.6 |
| qiu |  | 5.6k | 3 | 13.6k | 11 | 4.1k | 5 | 12.2k | 36 | 10.0k | 70 | 4143 | 3 | 3.7 |
| rail507 |  | 3.0k | 39 | 20.2k | 685 | 4.2k | 26 |  |  | 1.2 k | 3054 | 1250 | 26 | 4.7 |
| ran16×16 |  | 56.4 k | 10 | 89.8k | 19 | 238.1k | 24 | 59.7k | 52 | 134.6k | 54 | 56408 | 10 | 7.3 |
| reblock67 |  | 572.2k | 84 | 485.1k | 95 | 817.8k | 160 | 114.3k | 369 | 115.7k | 86 | 114337 | 84 | 4.1 |
| rmatr100-p10 |  | 1.8 k | 15 | 791 | 12 | 1.8 k | 8 | 3.0k | 39 | 809 | 397 | 791 | 8 | 3.5 |
| rmatr100-p5 |  | 441 | 10 | 421 | 19 | 881 | 12 | 1.7k | 63 | 419 | 1535 | 419 | 10 | 9.4 |
| rmine6 |  | 944.8k | 278 | 584.9k | 220 | 487.9k | 137 | 262.2k | 585 | 474.8k | 354 | 262168 | 137 | 3.5 |


| Name | Sets | CPLEX |  | XPRESS |  | GUROBI |  | CBC |  | $\mathrm{UG}[\mathrm{SCIP} / \mathrm{SPX}]$ |  | Best |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Nodes | Time | Nodes | Time | Nodes | Time | Nodes | Time | Nodes | Time | Nodes | Time | SU |
| rocll-4-11 |  | 250.8k | 75 | 42.7k | 45 | 29.7k | 73 | 51.6k | 1266 | 27.3k | $374{ }^{4}$ | 27259 | 45 | 4.6 |
| rococoC10-001000 |  | 70.9k | 91 | 69.1k | 91 | 1.7M | 309 | 40.5k | 154 | 164.7k | 370 | 40502 | 91 | 4.6 |
| roll3000 |  | 32.0k | 19 | 2.1k | 5 | 69.4k | 52 | 22.7k | 233 | 672.0k | 1440 | 2117 | 5 | 3.2 |
| satellites1-25 |  | 4.2 k | 90 | 4.8 k | 45 | 2.5 k | 97 | 18.9k | $176{ }^{5}$ | 14.7k | 240.0\% | 2496 | 45 | 2.3 |
| sp98ic |  | 213.5k | 200 | 39.0k | 215 | 14.2k | 73 | 380.4k | 2292 | 1.2 M | 0.4\% | 14212 | 73 | 4.0 |
| sp98ir |  | 6.3 k | 12 | 5.0k | 18 | 9.9k | 39 | 6.8 k | 16 | 4.4k | 82 | 4376 | 12 | 3.2 |
| tanglegram1 |  | 31 | 514 | 23 | 65 | 54 | 196 | 549 | inf\% | 1 | 0.0\% | 23 | 65 | 2.4 |
| tanglegram2 |  | 1 | 3 | 3 | 2 | 15 | 16 | 519 | 46 | 47 | 2153 | 1 | 2 | 1.0 |
| timtab1 | T | 842.8k | 62 | 403.8k | 63 | 1.7 M | 106 |  |  | 1.5 M | 174 | 403805 | 62 | 6.0 |
| triptim1 | P | 1 | 159 | 119 | 57 | 1 | 60 | 1 | 125 | 2 | 3011 | 1 | 57 | 0.7 |
| unitcal_7 |  | 3.2 k | 97 | 45 | 16 | 3.7 k | 128 | 3.7k | 664 | 4.5k | 0.1\% | 45 | 16 | 1.1 |
| vpphard |  | 18.5k | 1340 | 511.8k | inf\% | 78.0k | 66.7\% |  |  | 409 | inf\% | 18514 | 1340 | 1.9 |
| zib54-UUE |  | 16.2k | 353 | 292.5k | 317 | 40.9k | 312 | 263.3k | 1148 | 360.7k | 811 | 16156 | 312 | 4.9 |

[^6]
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[^2]:    2 That is, given the same machine and the same settings the solver should perform identical runs. Especially in a multi-thread environment special care has to be taken to achieve this since all dependencies on the relative timing of the threads have to be removed.

[^3]:    3 While it can be expected that the same binary will run identically on similar CPUs in general, modern compilers, e. g., the Intel C/C++ compilers [116], can detect the precise type of the CPU and use different instructions depending on the particular CPU. Since the internal precision of x86 type CPUs can differ depending on the instruction set used, the rounding of the last digit can be different.

[^4]:    

[^5]:    ${ }^{1}$ out-of-memory; $\quad 2$ constraint violation, absolute error: 0.0003

[^6]:    ${ }^{1}$ segmentation fault; $\quad 2$ early termination after 90 s due to bug in CPLEX 12.2 .0 .2 , will be fixed in CPLEX 12.3 ;
    ${ }^{3}$ out-of-memory; ${ }^{4}$ objective function mismatch; ${ }^{5}$ constraint violation, absolute error: 0.0003

