

Originally published as:

Kaveh Mollazade ; Mahmoud Omid ; Fardin Akhlaghian Tab ; Yousef Rezaei Kalaj ;
Seyed Saeid Mohtasebi ; Manueal Zude : Analysis of texture based features for predicting me-
chanical properties of horticultural products by laser light backscattering imaging .
in: Computers and Electronics in Agriculture 98 (2013) 10 S. 34-45

DOI: 10.1016/j.compag.2013.07.011

1 Analysis of texture-based features for predicting
2 mechanical properties of horticultural products by
3 laser light backscattering imaging

4

5

6 Kaveh Mollazade ^{a*}, Mahmoud Omid ^a, Fardin Akhlaghian Tab ^b, Yousef Rezaei
7 Kalaj ^c, Sayed Saeid Mohtasebi ^a, Manuela Zude ^c

8

9 ^a Department of Agricultural Machinery Engineering, Faculty of Agricultural
10 Engineering and Technology, University of Tehran, P.O. Box 4111, Karaj 31587-
11 77871, Iran

12 ^b Department of Computer Engineering, Faculty of Engineering, University of
13 Kurdistan, Sanandaj, Iran

14 ^c Leibniz Institute for Agricultural Engineering Potsdam-Bornim (ATB), Max-Eyth-
15 Allee 100, 14469 Potsdam, Germany

16

17 * Corresponding author; Tel: +98 918 9720639; Fax: +98 261 2808138

18 E-mail address: mollazade@ut.ac.ir (K. Mollazade)

19

20

21

22 **Abstract**

23 Light backscattering imaging is an advanced technology applicable as a non-
24 destructive technique for monitoring quality of horticultural products. Because of
25 novelty of this technique, developed algorithms for processing this type of images are
26 in preliminary stage. Texture is one of the most important characteristics of images
27 and has been used widely in agro-food industry for assessing qualitative properties of
28 different types of products. The present study investigates the feasibility of texture-
29 based features to develop better models for predicting mechanical properties (fruit
30 flesh firmness or elastic modulus) of horticultural products. Images of apple, plum,
31 tomato, and mushroom were acquired using a backscattering imaging setup capturing
32 660 nm. After segmenting the backscattering regions of images by variable
33 thresholding technique, they were subjected to texture analyses and space domain
34 techniques in order to extract a number of features. Adaptive neuro-fuzzy inference
35 system models were developed for firmness or elasticity prediction using individual
36 types of feature sets and their combinations as input for prediction model applicable in
37 real-time applications. Results showed that fusion of the selected feature sets of image
38 texture analysis and space domain techniques provide an effective means for
39 improving the performance of backscattering imaging systems in predicting
40 mechanical properties of horticultural products. The maximum value of correlation
41 coefficient in the prediction stage was achieved as 0.887, 0.790, 0.919, and 0.896 for
42 apple, plum, tomato, and mushroom products, respectively.

43 **Keywords:** ANFIS, backscattering, feature fusion, quality evaluation, texture
44 analysis.

45

46 **1. Introduction**

47 Fruit flesh firmness and elastic modulus are two main mechanical parameters in
48 determining maturity and harvest time of horticultural products, and they are also key
49 parameters in evaluation and grading postharvest quality of fruit and some vegetables.
50 Mechanical properties of fresh produce change during growth and storage processes.
51 The conventional standard methods, like Magness-Taylor compression test and
52 Youngs' modulus of elasticity, are not suitable for real-time applications, such as
53 grading and sorting machines, because the samples should be per definition or
54 potentially damaged during the test. Technical advances over the last few decades
55 considering spectrophotometers, multi- and hyperspectral systems as well as computer
56 vision systems have led to the development of non-destructive devices capable of
57 measuring internal qualitative parameters of horticultural products. [Garcia-Ramos et](#)
58 [al. \(2005\)](#) reviewed the non-destructive techniques developed to measure mechanical
59 properties of agricultural products. They concluded that optical techniques have the
60 advantage over the others, since they can estimate several internal variables, such as
61 sugar content, acid content, firmness, and elasticity, with a single sensor. However, it
62 has been shown that the application of spectroscopic analyses is not capable to build
63 robust calibrations for predicting the mechanical properties of the produce, while the
64 composition considering pigments, soluble solids content, dry matter, and moisture
65 content as well as the detection of internal physiological disorders appeared feasible
66 in several products ([Zude, 2009](#)).

67 As an optical technique, computer vision-based quality evaluation systems are being
68 used increasingly in the agro-food industry because of their rapid, non-contact, and
69 non-destructive manner as well as availability of inexpensive camera systems. Driven

70 by considerable improvements in imaging hardware and rapid progression in image
71 processing techniques, computer vision has established its applications for the internal
72 surveillance of both fresh and processed agro-food materials. In combination with
73 multi- or hyperspectral imaging more specific variation of the produce, such as the
74 detection of distribution of water core and internal browning has been shown.

75 Horticultural products, as biological materials, are supposed to be turbid and transmit
76 the light through the tissue depending on the wavelengths (Mireei, 2010). When light
77 source impinges to a biological tissue, its internal contents reflect most of the passing
78 light as scattering photons towards the exterior tissue surface. Due to physiochemical
79 properties of the tissue, photons are scattered at different angles, leading to their
80 stochastic interaction with the internal components of biological tissue like joint
81 surfaces of the cell wall, chloroplasts, mitochondria, etc (Nicolai et al., 2007).
82 Because of this interaction, backscattering photons carry information related to the
83 morphology and structures of the tissue, such as mechanical properties additionally to
84 the information on absorbing molecules. Few work groups showed that it is possible
85 to record backscattered photons by a camera equipped with an imaging sensor
86 sensitive in the range of visible and short wave near infrared (SWNIR) of
87 electromagnetic spectrum. The technique focuses on the processing of these types of
88 images and extracting knowledge from them has been named as backscattering
89 imaging. Based on the light source and imaging unit used, the technique is divided
90 into three categories: hyperspectral backscattering imaging (HBI), mutispectral
91 backscattering imaging (MBI), and laser light (monochromatic) backscattering
92 imaging (LLBI). The acquired images by these categories are similar, when we speak
93 about a certain wavelength (Mollazade et al., 2012a).

94 In most researches done to date, light intensity-based features in the space domain
95 were used to establish calibration models between the backscattering images and
96 reference physical properties. [Qing et al. \(2007\)](#) used the simplest type of features, i.e.
97 the area of backscattering region that is equal to the total number of pixels in the
98 segmented backscattering image, to predict firmness of apple. Another simple
99 technique is to use the mean intensity value ([Qing et al., 2008](#)) or some statistical
100 characteristics of pixels remained after segmenting the backscattering region ([Noh
101 and Lu 2007](#)). [Lu \(2004\)](#) introduced a method, known as radial averaging, in which
102 scattering region of photons is divided into several circular rings and then average
103 value of all pixels within each ring is recorded as the features of image. Using the
104 radial averaging approach, researchers applied different semi-Gaussian mathematical
105 functions, like exponential, Lorentzian, and Gompertz, to fit one-dimensional (1D)
106 scattering profiles as a function of distance. The values of parameters of the fitted
107 functions were then used as the features of images ([Peng and Lu 2005, 2006, 2007](#)).
108 Extracting the absorption and reduced scattering coefficients of 1D profile from the
109 Farrell's diffusion theory model is another method used to predict firmness of apple
110 ([Qin and Lu, 2006](#)).

111 Although the above mentioned techniques have shown relatively fair utility in
112 describing the backscattering features, their relative performance in predicting
113 mechanical properties of horticultural products is not quite clear because they were
114 tested in separate studies, where the samples used were different and the experimental
115 setups were not the same. Hence, direct comparison of these feature extraction
116 techniques is required in order to investigate which method is the most suitable for
117 predicting mechanical properties of horticultural products. Furthermore, previous
118 techniques are based on some simple statistical features of pixel brightness or analysis

119 of 1D scattering profiles, and they did not investigate the pixel intensity pattern from
120 the overall two-dimensional (2D) scattering images acquired at a specific wavelength.
121 Use of 2D processing algorithms could present a chance to improve the performance
122 of backscattering imaging technique in predicting firmness and elasticity of
123 horticultural produce. Texture, as a 2D processing approach, is an important image
124 feature that corresponds to both brightness value and pixel locations. Many
125 researchers reported the feasibility of texture-based features in the food industry for
126 quality evaluation and inspection (Jackman and Sun, 2012). The distribution pattern
127 of backscattering photons is unique for each backscattering image, since the spatial
128 pattern in an image reflects the physiochemical properties of a product. Hence, by
129 utilizing the texture-based features, researchers may improve the accuracy
130 performance and take feasibility of backscattering systems in real-time applications.

131 Therefore, the overall objective of this research was to use LLBI technique for
132 predicting firmness and elastic modulus (elasticity) of a wide range of horticultural
133 products. The specific objectives were to:

- 134 • Analysis the capability of different texture processing techniques for
135 firmness/elasticity prediction.
- 136 • Compare the texture-based feature extraction techniques with those reported in
137 the previous researches (space domain techniques).
- 138 • Establish intelligent models for firmness/elasticity prediction by adaptive
139 neuro-fuzzy inference system (ANFIS).
- 140 • Suggesting the best feature set for real-time applications.

141

142 **2. Materials and methods**

143

144 2.1. Data set

145 Mechanical properties obtained from two stony fruits (apple and plum), a non-stony
146 fruit (tomato), and a vegetable (mushroom) were used as data set. Harvested manually
147 from the garden and greenhouse, samples were visually inspected for appearance and
148 surface defects. Only those samples free of visual defects (such as scars, cuts, shrivel,
149 etc.) were selected for the experiments. To generate samples with variations in their
150 properties, they were separated into several groups and stored at the standard
151 temperature and relative humidity conditions. Groups of samples were withdrawn
152 from the storage chamber two hours before the experiments at regular intervals of 15,
153 3, 7, and 3 days for apple, plum, tomato, and mushroom, respectively. After
154 acquisition of backscattering images, samples were subjected to compression test.
155 Firmness was measured as the mechanical signature of stony fruits, while for tomato
156 and mushroom samples, elasticity was calculated (Mohsenin, 1986). Table 1
157 summarizes some information related to the samples, measurement conditions, and
158 mechanical tests.

159 **Table 1.**

160 2.2. Backscattering image acquisition

161 Backscattering images were acquired using an in-house built LLBI system (Baranyai
162 and Zude, 2009). The system mainly consisted of a wide dynamic range monochrome
163 CCD camera (JAI A50IR CCIR, JAI, Denmark) with a zoom lens (model H6Z810,
164 PENTAX Europe GmbH, Germany), a solid-state laser diode emitting at 660 nm as
165 the light source (LPM series, Newport Corp., USA), a laser driver, a sample holder
166 unit, video converter (VRM AVC-1, Stemmer Imaging GmbH, Germany), and a

167 computer equipped with an in-house developed software to acquire the backscattering
168 images. The backscattering images with the spatial resolution of 720×576 pixels were
169 acquired in a dark room and laser diode spot of 1 mm diameter provided an acceptable
170 signal to noise ratio. The camera was placed perpendicular to the sample holder while
171 the incident angle of the laser beam was adjusted to 15°.

172

173 2.3. Image processing

174 Image processing was carried out using MATLAB R2009a and its image processing
175 toolbox (The Mathworks, Inc., Natick, MA, USA).

176

177 2.3.1. Segmentation

178 Segmentation plays a key role in processing of backscattering images. If it does not
179 perform well, useful information may be omitted. Segmentation operation consists of
180 segregating the region of interest (ROI), backscattering photons minus those saturate
181 the CCD of camera, from the background. This operation was carried out in two steps
182 as following:

183 *1. Removing saturated pixels:* Since saturated region in images consists of photons
184 that directly return to the camera's sensor, the light intensity of pixels in this region is
185 close to its maximum value, i.e. 255. By a trial and error procedure, it was found that
186 saturated regions are segmented successfully by the static threshold value of 252.

187 *2. Segmenting regions consists of backscattering photons from the background:*
188 Variable thresholding by local statistics is a powerful segmentation technique when
189 background illumination is uneven. At each pixel of image, the threshold value is
190 defined based on some statistical features extracted from the neighborhood pixels
191 (Gonzalez and Woods, 2004). In the current study, threshold values were selected

192 based on the standard deviation and the average of a 3×3 neighborhood for each pixel.
193 These features were very useful in setting local thresholds, because they are contrast
194 and average of local intensity.

195

196 2.3.2. Texture analysis

197 A wide variety of techniques have been proposed for describing image texture ([Zheng](#)
198 [et al., 2006](#)). Approaches to texture analysis are usually classified into four categories:
199 statistical, structural, transform-based, and model-based. Statistical techniques
200 represent the texture indirectly by non-deterministic properties that govern the
201 distribution and relationship between the grey levels of an image. Structural
202 approaches represent texture through some structural primitives constructed from grey
203 values of pixels. In the transform methods of texture analysis, an image is represented
204 in a space whose co-ordinate system has an interpretation that is closely related to the
205 characteristics of a texture (such as frequency or size). Model-based texture analysis
206 attempts to interpret an image texture by use of, respectively, generative image model
207 and stochastic model. The parameters of the model are calculated, based on the
208 relationship of the grey values between a pixel and its neighboring pixels, and then
209 these are used for image analysis.

210 To process backscattering images, texture-based features from four statistical
211 techniques (first order statistics of image histogram (FOSH), grey level co-occurrence
212 matrix(GLCM), grey level run length matrix (GLRLM), and local binary pattern
213 (LBP)), three transform-based techniques (wavelet transform, Gabor transform, and
214 Tamura), and two model-based techniques (fractal model and simultaneous
215 autoregressive model), were considered. Structural techniques were not considered in
216 this research since the structural primitives used in these methods can only describe

217 very regular textures (Bharati et al.,2004). Furthermore, structural techniques are
218 rarely used in the food industry to describe texture characteristics (Zheng et al., 2006).
219 A brief description of these techniques is provided in the following subsections.

220

221 2.3.2.1. First order statistics of image histogram

222 First order statistics of image histogram are considered as the most basic feature
223 extraction method of image texture. They act based on the probability of occurring
224 pixel intensity values in the image. They depend only on individual pixel values and
225 not on interaction of neighboring pixel values. First the histogram of grey level
226 backscattering images was extracted. The histograms were then normalized according
227 to the following formula:

$$228 \quad p(z_i) = \frac{H(z_i)}{N_I} \quad (1)$$

229 where $H(z_i)$ is the image histogram, $p(z_i)$ is the normalized histogram, and N_I is the
230 total number of arrays in the image matrix. Using the normalized histogram and
231 relations based on the occurrence of grey levels, eight statistical features were
232 extracted from each backscattering image (Bevk and Kononenko, 2002). The list of
233 features is presented in Table 2.

234

235 2.3.2.2. Grey level co-occurrence matrix

236 A GLCM is a matrix in which grey level pixels are considered in pairs with a relative
237 distance d and orientation θ among them. The entry $G_{d\theta}(i, j)$ of this matrix is the
238 number of occurrences of a pair of grey levels, i and j , for the specified displacement.
239 The scattering images were analyzed using the distance $d=1$ pixel with angles $\theta = 0,$
240 $45, 90,$ and 135° as suggested by Haralick (1979). After calculating GLCMs, they
241 were normalized so that sum of arrays in the normalized matrix is equal to 1. Ten

242 features were then extracted from each normalized GLCM according to [Table 2](#)
243 ([Haralick et al., 1973](#)). Thus, a total of 40 features (4 orientations \times 10 statistical
244 features) were extracted from each image.

245

246 2.3.2.3. Grey level run length matrix

247 Run length technique records the coarseness of a texture in specified directions by
248 encoding textural information based on the number each grey level appearing in the
249 image by itself. A run is defined as a string of consecutive pixels which have the
250 same grey level intensity along a specific linear orientation. Fine textures tend to
251 contain more short runs with similar grey level intensities, while coarse textures have
252 more long runs with significantly different grey level intensities. A GLRLM is a
253 matrix in which each element $r(i,j)$ determines the total number of occurrence of run
254 lengths j in the grey level i in specified direction θ . Run length matrices at four
255 directions $\theta = 0, 45, 90,$ and 135° were extracted for each backscattering image. Once
256 the GLRLMs were calculated along each direction, 11 texture descriptors, as
257 suggested by [Tang \(1998\)](#), were calculated to capture the texture properties and
258 differentiate among different textures ([Table 2](#)). For each image, a total of 44 features
259 (11 GLRLM texture descriptors \times 4 directions) were obtained.

260

261 2.3.2.4. Local binary pattern

262 The LBP texture analysis operator is defined as a grey-scale invariant texture
263 measure, derived from a general definition of texture in a local neighborhood. For
264 each pixel in an image, a neighborhood of the image (usually a 3×3 window) is
265 considered and the intensity value of neighboring pixels is compared with that of the
266 central pixel. If the intensity value of neighboring pixels is greater or equal to the

267 central pixel value, they are replaced with ones. Otherwise, their value is zero.
268 Finally, central pixel is replaced with the binary weighted sum of neighboring pixels
269 and the neighboring window is transferred to the next pixel. The output of LBP
270 operator is a P-bit binary number (P is the number of neighboring pixels), which can
271 take 2^P different values. Furthermore, LBP is completely dependent to indexing of
272 pixels contained in the neighborhood. Thus, in order to assign a unique value to each
273 private binary pattern, LBP matrices were robust to rotation by clockwise rotation of
274 the obtained binary number and selecting the maximum possible value (Ojala et al.,
275 2002). Finally, 8 statistical features were extracted from the normalized histogram of
276 GLRLM of each backscattering image.

277

278 2.3.2.5. Wavelet transform

279 Wavelet transform is a useful tool for analyzing the texture of agricultural materials.
280 A discrete wavelet transform (DWT) decomposes an image onto multiple wavelet
281 components using a filter bank as suggested by Mallat (1989). It provides four sets of
282 coefficient at each level of decomposition. Rows of the input image are first passed
283 through the low and high pass filters, followed by down-sampling along the rows by a
284 factor of 2. The columns of resulting images from both filters are sent through low
285 and high pass filters followed by down sampling along the columns to obtain four sets
286 of coefficients; namely, approximation, horizontal, vertical, and diagonal details
287 (Choudhary et al., 2008). Backscattering images were subjected to six levels of
288 wavelet decomposition using a fourth-order Daubechies mother wavelet (Db4), which
289 is the most popular mother wavelet family for image texture analysis. At each level of
290 decomposition, approximation coefficients and wavelet detail coefficients were
291 obtained for horizontal, vertical, and diagonal orientations. To determine optimum

292 level of decomposition, backscattering images at each level of decomposition were
293 compared to the original images. As is shown in the [Figure 1](#), an increase in the levels
294 of decomposition leads to increase the amount of down-sampling, resulting in lower
295 resolutions at successive levels. So, the wavelet coefficients from first to the fourth
296 level of decomposition were considered to be used in feature extraction stage. Four
297 statistical descriptors including mean, standard deviation, energy, and entropy were
298 extracted from each level of decomposition. A total of 64 features (4 statistical
299 descriptors \times 4 wavelet coefficients \times 4 decomposition levels) were obtained from the
300 DWT of each backscattering image.

301

302 2.3.2.6. Gabor transform

303 Gabor transform is one of the most effective and most popular filter-based approaches
304 to extract texture features of an image. Gabor filter is obtained by multiplying a
305 Gaussian function in a directional sine function. Therefore, this filter generates
306 powerful responses at locations with specific local direction and frequency ([Zhu et al.,
307 2007](#)). Gabor wavelet is a kind of wavelet transform function in which its mother
308 wavelet is a Gabor filter. After applying the Gabor wavelet on backscattering images,
309 a new matrix with $M \times N$ dimension was obtained. Each dimension represents a
310 frequency in a specific direction. Since each element of the final image, after applying
311 the Gabor transform, is a complex number with both real and imaginary parts, the
312 matrix magnitude was used for feature extraction ([Figure 2](#)). Mean, standard
313 deviation, energy, and entropy were used as statistical descriptors in order to build the
314 feature vector containing the texture descriptors of backscattering images by Gabor
315 filter. These statistical operators were then applied on the magnitude of matrices
316 found in the previous section for each backscattering image in four frequencies

317 (0.1768, 0.25, 0.3536, and 0.5 Hz) and four directions (0, $\pi/4$, $\pi/2$, and $3\pi/4$ radian).
 318 The size of feature vector based on the Gabor transform was 64 (4 statistical
 319 descriptors \times 4 frequencies \times 4 directions).

320

321 2.3.2.7. Tamura

322 Tamura features are designed based on psychological studies on human visual
 323 perception of objects texture (Tamura et al., 1978). These features include coarseness,
 324 contrast, directionality, line-likeness, regularity, and roughness. Since the last three
 325 features are derived from the first three ones, only coarseness, contrast, and
 326 directionality just were extracted from each backscattering image.

327

328 An image contains textures at several scales; coarseness aims to identify the largest
 329 size at which a texture exists, even though a smaller micro texture may exist. To
 330 compute the coarseness, using a $2^k \times 2^k$ ($k=0,1,\dots,5$) window, first a moving average
 331 filter $A_k(x,y)$ was applied on each pixel:

$$332 \quad A_k(x, y) = \frac{\sum_{i=x-2^{k-1}}^{x+2^{k+1}-1} \sum_{j=y-2^{k-1}}^{y+2^{k+1}-1} g(i,j)}{2^{2k}} \quad (2)$$

333 where $g(i,j)$ is the intensity value at pixel (i,j) .

334 Then at each pixel differences between pairs of $A_k(x,y)$ corresponding to non-
 335 overlapping neighborhoods on opposite sides of the point in both horizontal and
 336 vertical orientations were calculated:

$$337 \quad E_{k,h}(x, y) = |A_k(x + 2^{k-1}, y) - A_k(x - 2^{k-1}, y)| \quad (3)$$

$$338 \quad E_{k,v}(x, y) = |A_k(x, y + 2^{k-1}) - A_k(x, y - 2^{k-1})| \quad (4)$$

339 In order to determine the filter window size for each pixel which gives the highest
 340 output value, the value of k was taken in which E is maximized in either direction.

341 The coarseness was then computed by the following formula:

342
$$F_{crs} = \frac{1}{m \times n} \sum_{i=1}^m \sum_{j=1}^n 2^k(i, j) \quad (5)$$

343 Contrast aims to capture the dynamic range of grey levels in an image, together with
 344 the polarization of the distribution of black and white. The first is measured using the
 345 standard deviation of grey levels (σ) and the second from the kurtosis α_4 . The contrast
 346 measure was therefore defined as:

347
$$F_{con} = \frac{\sigma}{\alpha_4^{1/4}} \quad (6)$$

348 Directionality is a measure of the orientation of the image grey values. To compute
 349 the directionality, initially two simple masks were used first to detect edges in
 350 backscattering images. At each pixel the angle and magnitude were calculated. A
 351 histogram of edge probabilities was then built up by counting all points with
 352 magnitude greater than a threshold and quantizing by the edge angle. The histogram
 353 reflects the degree of directionality. Finally, the directionality was then computed
 354 from the sharpness of the peaks of histogram using their second moments.

355

356 2.3.2.8. Fractal model

357 In the image analysis of agro-food materials, fractal dimension can be used to
 358 estimate and quantify the complexity of the shape or texture of images. The fractal
 359 dimension gives a measure of the roughness of an image. Intuitively, the larger the
 360 fractal dimension, the rougher the texture is (Zheng et al., 2006). There are a number
 361 of methods proposed for defining the fractal dimensions, where the most common one
 362 is the Hausdorff's dimension (D_0):

363
$$D_0 = \lim_{\varepsilon \rightarrow 0} \frac{\log N(\varepsilon)}{\log \varepsilon^{-1}} \quad (7)$$

364 where $N(\varepsilon)$ is the number of hypercubes of Euclidean dimension E , and length ε that
 365 fill the object. In this research, a new developed algorithm known as segmentation-

366 based fractal texture analysis (SFTA) was used to extract the Hausdorff's fractal
367 dimension of backscattering images (Costa et al., 2012). The SFTA algorithm was
368 implemented in two steps. In the first step, a set of threshold values was computed
369 using multi-level Otsu algorithm and distribution of grey levels in the input images.
370 The number of optimum thresholds was set to 8, as suggested by Costa et al. (2012).
371 After that, the grey level backscattering images were disintegrated into a set of binary
372 images by selecting pairs of thresholds from the threshold set and applying the two-
373 threshold binary decomposition (TTBD) algorithm. The number of resulting binary
374 images was 16. Figure 3 illustrates the decomposition of a backscattering image taken
375 from a tomato sample at 660 nm using the TTBD algorithm. The threshold set for this
376 sample was as $T=[0, 0.0039, 0.0391, 0.1367, 0.2188, 0.3477, 0.4961, 0.6914]$. In the
377 second step of SFTA, Hausdorff's dimension was computed from the borders of each
378 binary image by applying the box counting algorithm (BCA). In the BCA, binary
379 images were divided into a grid composed of squares of size $\varepsilon \times \varepsilon$. The number ($N(\varepsilon)$)
380 of squares of size $\varepsilon \times \varepsilon$ that contains at least one pixel of ROI was counted. A $\log N(\varepsilon)$
381 versus $\log \varepsilon^{-1}$ curve was drawn for each binary image by varying the value ε . The
382 curve was approximated by a straight line using the least squares fitting approach.
383 Then, the slop of this line was recorded as the Hausdorff's dimension of each binary
384 image. The size of fractal feature vector for each backscattering image was 16 (Figure
385 3).

386

387 2.3.2.9. Autoregressive model

388 Simultaneous autoregressive (SAR), as a model-based texture analysis technique, has
389 found many applications in image segmentation (Sukissian, 1994, Sukissian et al.,
390 1997). This model acts based on the spatial relationship between the pixels of an

391 image. It assumes that intensity of pixels is the weighted sum of intensity from the
392 neighboring pixels. In fact a SAR models the relationship between a pixel and its
393 neighboring pixels using the following linear combination (Jain, 1989):

$$394 \quad f(s) = \mu + \sum_{q \in N} \theta(q) f(q) + \varepsilon(q) \quad (8)$$

395 where $f(s)$, $f(q)$, μ , $\varepsilon(q)$, N , and $\theta(q)$ are image intensity at position s , image intensity at
396 position q , bias value, noise value, number of neighboring pixels, and model
397 parameters, respectively. In the current research, the bias value was adjusted to the
398 average of light intensity of entire image, which was formerly normalized between 0
399 and 1. A Gaussian random variable with mean zero and variance σ^2 was used to adjust
400 the noise value. The number of neighboring pixels considered was equal to four
401 according to the pattern shown in Figure 4. For each backscattering image, a total of
402 five SAR model features, including values of θ in four neighboring pixels together
403 with the minimum prediction error variance, were extracted.

404 [Table 2](#)

405 [Figure 1](#)

406 [Figure 2](#)

407 [Figure 3](#)

408 [Figure 4](#)

409

410 2.3.3. Space domain analysis

411 In order to assess the effectiveness of texture analysis techniques, backscattering
412 images were subjected to several space domain techniques proposed by researchers in
413 literature. These techniques as described in the “Introduction” section, were:

414 1. Total number of pixels in the segmented backscattering region of image,

- 415 2. Statistical features of segmented backscattering region of image (mean, min,
416 max, sum, standard deviation, and variance),
- 417 3. Radial averaging technique (25 rings with thickness of five pixels),
- 418 4. Modified Lorentzian function parameters (four parameters: a , b , c , and d),
- 419 5. Modified Gompertz function parameters (four parameters: α , β , ε , and δ), and
- 420 6. Farrell's diffusion theory model parameters (two parameters: absorption (μ_a)
421 and reduced scattering coefficients (μ_s')).

422 Readers can refer to the references provided in the "Introduction" section to get more
423 information about these techniques.

424

425 2.4. Adaptive neuro-fuzzy inference system (ANFIS)

426 A neuro-fuzzy system integrates the advantages of artificial neural networks (ANNs)
427 with rule-based fuzzy inference systems (FIS). It covers the lacks of these techniques
428 when they are used individually. ANNs are efficient structures capable of learning
429 from examples, while fuzzy systems are suitable for uncertain knowledge
430 representation. These hybrid technique brings learning capability of ANN to FIS.
431 During the learning process, a number of desired input–output data pairs are used, and
432 then parameters associated with the membership functions and rules of a Takagi-
433 Sugeno type FIS are tuned by ANN so as to map the inputs to outputs. The
434 computation and adjustment of these parameters is facilitated by a gradient vector,
435 which provides a measure of how well the FIS is modeling the input/output data for a
436 given set of parameters. From the topology point of view, ANFIS is an
437 implementation of a representative FIS using a feed forward neural network-like
438 structure ([Jang, 1993](#)).

439 The fuzzy logic toolbox of MATLAB R2009a was used to create ANFIS models (The
440 Mathworks, Inc., Natick, MA, USA). The inputs to the models were the normalized
441 feature sets (in the range 0 to 1) extracted from backscattering images, while the
442 output was the firmness or elasticity of samples. ANFIS is susceptible to the curse of
443 dimensionality when number of inputs exceeds three. The training time increases
444 exponentially with respect to the number of fuzzy sets per input variable used. An
445 effective procedure to reduce the dimension of the input vector is to use principal
446 component analysis (PCA). The technique was outlined by authors previously (Omid
447 et al., 2009 and 2010). Hence, the inputs were subjected to the PCA and only the first
448 three principal components were fed to the ANFIS. The performance of ANFIS is
449 highly dependent to its structure. Therefore, four significant adjustments were made in
450 the structure of ANFIS models in order to find best one for predicting
451 firmness/elasticity of horticultural produce. Settings include the number of
452 membership functions (changed from 2 to 5 with step size of 1), types of input
453 membership functions (triangular, trapezoidal, bell-shaped, Gaussian, and sigmoid),
454 types of output membership function (constant and linear), and optimization methods
455 (hybrid and back-propagation). Each ANFIS model with its specific setting was run
456 20 times and the best was defined as the one with the best overall statistical accuracy
457 measures.

458

459 2.5. Statistical measures

460 To ensure the models were not over-fitted and the prediction results truly represent the
461 model performance, the samples were first divided into three separate parts randomly.
462 The first part (or 60% of all samples) was used for training, 15% of all samples were
463 used for cross-validation, and the remaining samples were used for independent test or

464 prediction. Calibration models for firmness and elasticity were developed using
 465 ANFIS from the training samples. Cross-validation was used to supervise the training
 466 process in order to prevent the over-training. Thereafter, the calibration models were
 467 used to predict the independent part of samples. The models were evaluated using root
 468 mean squares errors for cross validation (RMSECV) and prediction (RMSEP).

$$469 \quad RMSE = \sqrt{\frac{\sum_{i=1}^n (\hat{y}_i - y_i)^2}{n}} \quad (9)$$

470 where \hat{y}_i is the actual value, y_i is the predicted value, and n is the number of samples
 471 in prediction or calibration stages. In addition, correlation coefficients for calibration
 472 (R_c) and prediction (R_p) were also calculated. Processing time is an important factor
 473 when we want to use a backscattering imaging system in real-time applications. For
 474 each feature extraction technique, the processing time was recorded to be used as an
 475 evaluation criterion. MATLAB codes were implemented and run in a laptop computer
 476 with this configuration: Core 2Duo CPU, 2.53 GHz, 4 GB RAM, Windows 7 OC
 477 configuration.

478

479 **3. Results and discussion**

480 3.1. Individual feature set models

481 The statistical measures of individual texture-based feature models for predicting
 482 firmness/elasticity of apple, plum, tomato, and mushroom by ANFIS are presented in
 483 **Table 3**. The best firmness prediction of FOSH technique using ANFIS for apple was
 484 the highest ($R_p=0.861$) followed by the Tamura ($R_p=0.846$), fractal ($R_p=0.826$), and
 485 wavelet ($R_p=0.825$). The highest prediction accuracies for plum, tomato, and
 486 mushroom were obtained by the SAR ($R_p=0.757$), Gabor ($R_p=0.857$), and Tamura
 487 ($R_p=0.839$), respectively, whereas, for the same, the wavelet ($R_p=0.554$), GLRLM
 488 ($R_p=0.675$), and SAR ($R_p=0.717$) produced the lowest prediction performance.

489 Comparing to the other texture analysis techniques, Tamura and fractal provided good
490 results for all samples leading to select them as the best texture-based techniques for
491 analysis of backscattering images because of their consistency in firmness/elasticity
492 prediction performance. This reflects the fact that border of segmented regions along
493 with distribution pattern of light intensity in backscattering images are closely related
494 to the mechanical properties of horticultural products. On the other hand, LBP in all
495 cases was one of four techniques showed the lowest correlation with the
496 firmness/elasticity changes. The poor performance of LBP features can be attributed
497 to the small changes of run length values in backscattering images when mechanical
498 properties of products change. Comparing the results obtained for apple, plum,
499 tomato, and mushroom show that Tamura, fractal, FOSH, and GLCM are the best
500 texture analysis methods in overall for predicting firmness/elasticity of horticultural
501 produces when they are used as an individual feature set.

502 Regarding the space domain features (see [Table 4](#)), results showed that statistical,
503 radial averaging, and Farrell's features have the highest performance in predicting
504 firmness/elasticity of apple, plum, tomato, and mushroom compared to the other
505 techniques. However, for all products, the lowest prediction performance was
506 recorded for the total number of pixels technique. Lorentizan and Gompertz
507 techniques did not show the consistency in firmness/elasticity prediction so that they
508 presented acceptable performance for tomato fruit, while for the plum and mushroom
509 the accuracy of these techniques was considerably low. The reason for this is that the
510 area of backscattering region for tomato fruit was bigger than that of mushroom and
511 plum resulting in the better fitness of 1D backscattering profile by Lorentzian and
512 Gompertz functions. Comparing the results obtained in the [Tables 3 and 4](#)
513 demonstrates texture analysis techniques provide better performance than that of

514 space domain techniques when they are used individually. However, the differences
515 are very small.

516 **Table 3**

517 **Table 4**

518 3.2. Real-time feature set models

519 In real-time applications, such as grading/sorting machines, two factors are important:
520 prediction accuracy and processing time. To compare the capability of different
521 texture and space domain techniques for real-time applications, processing time
522 during implementation and feature extraction process for each technique was
523 recorded. **Figures 5 and 6** illustrate, respectively, the time achieved by various texture
524 and space domain methods on the study data set, respectively. Results show that the
525 type of sample has no significant impact on the processing time because the image
526 dimensions are the same. Obviously, Tamura, fractal, Gabor, and GLRLM are
527 unsuitable for real-time systems since they require considerable much time for
528 implementation. On the other hand, FOSH, GLCM, LBP, wavelet, and SAR were the
529 fastest techniques because their processing time was less than 0.5 second. Space
530 domain techniques, except radial averaging, recognized to be suitable for real-time
531 purposes since they need processing time lower than that of our threshold, i.e. 0.5
532 second.

533 Many researchers reported that the combined feature models perform better than
534 individual models. Hence, all of the real-time features were combined together to
535 make two data sets, one for texture analysis methods and the other for space domain
536 techniques. The combination process leads to produce data sets with large number of
537 inputs so that the size of new texture analysis and space domain feature vectors was
538 125 (8 FOSH + 40 GLCM + 8 LBP + 64 wavelet + 5 SAR) and 17 (2 Farrell + 4

539 Lorentzian + 4 Gompertz + 6 statistical features + 1 Total number of pixels),
540 respectively. The large number of model inputs may leads to increase the execution
541 time and reduce the predictive accuracy. Using feature selection approaches such as
542 PCA, sensitivity analysis, genetic algorithms (GA), etc., these problems go away by
543 eliminating redundant features. In this study, genetic algorithm technique (GA) was
544 used for feature reduction as many researchers reported its suitability for this aim
545 (Leardi, 2000; Mollazade et al., 2012b). Table 5 shows the list of top texture analysis
546 and space domain features obtained by GA for apple, plum, tomato and mushroom.
547 Feature selection process considerably reduced the size of feature vectors so that the
548 size of texture analysis and time domain feature vectors was 10 and 2 for apple, 7 and
549 3 for plum, 5 and 4 for tomato, and 5 and 2 for mushroom, respectively. The wavelet
550 and modified Lorentzian function are superior compared to others since most of the
551 top features have been selected from the features of these techniques.

552 The ANFIS model with the selected texture analysis features gave the prediction
553 correlation coefficient of 0.872, 0.776, 0.853, and 0.827 for apple, plum, tomato, and
554 mushroom, respectively, which are slightly higher than that obtained by the ANFIS
555 models with individual texture analysis techniques (Tables 3 and 6). Regarding the
556 selected real-time space domain features, the same behavior has been observed so that
557 prediction correlation coefficient for apple, plum, tomato, and mushroom showed an
558 increase from 0.823 to 0.847, 0.754 to 0.762, 0.796 to 0.864, and 0.744 to 0.764,
559 respectively (Tables 4 and 7).

560

561 3.3. Fusion of selected real-time feature sets model

562 The real-time features selected from texture analysis and space domain techniques
563 (Table 5) were combined together in order to make a single feature set having the

564 benefits of two feature sets. **Figure 7** presents the statistical measures of combined
565 feature set model by ANFIS. Using the combined feature set model, the prediction
566 accuracies of all the products were improved in comparison to the single real-time
567 selected feature set models (**Tables 6 and 7, and Figure 7**). The correlation coefficient
568 in prediction stage for tomato was highest ($R_p=0.919$) followed by mushroom
569 ($R_p=0.896$), apple ($R_p=0.887$), and plum ($R_p=0.790$). This indicates that the integration
570 of space domain and texture-based features considerably improved firmness/elasticity
571 prediction for tomato and mushroom products but with a lesser degree of accuracy for
572 apple and plum fruits. With the proposed features for laser induced backscattering
573 imaging, the system is suitable to be implemented as a non-destructive technique in
574 real-time machines to grade/sort horticultural products based on their mechanical
575 properties. More efforts are needed to improve the capabilities of this system to meet
576 the real-time requirements for monitoring different qualitative properties of
577 horticultural produce. Works in this direction is in progress by authors.

578 **Figure 5**

579 **Figure 6**

580 **Table 5**

581 **Table 6**

582 **Table 7**

583 **Figure 7**

584 **4. Conclusions**

585 In this research an experimental analysis of a number of different texture analysis
586 methods along with several space domain techniques was carried out for predicting
587 mechanical properties of apple, plum, tomato and mushroom. Calibration models
588 were developed by ANFIS that is an efficient artificial intelligent approach for

589 modeling. Texture analysis methods showed slightly better results than those of the
590 space domain techniques when feature set of each technique was fed independently to
591 the ANFIS. Results showed that combination of real-time features of texture analysis
592 techniques was more effective than when they were used individually for predicting
593 firmness/elasticity. Similar results were observed for the space domain techniques too.
594 Feature selection process showed that not only it leads to a considerable reduction in
595 the feature vectors but also improves the prediction accuracy of ANFIS models.
596 Among all of the techniques used for feature extraction, wavelet transform and
597 modified Lorentzian function are introduced as the best techniques for analysis of
598 backscattering images. For all horticultural products in this research, it was found that
599 integrating selected real-time features of both texture analysis and space domain
600 techniques provides the best prediction results. The statistical performance for apple,
601 tomato, and mushroom was in an acceptable range while real-time sensing of firmness
602 for plum fruit was still poor. Future works should focus on the improving the accuracy
603 and robustness of methods described in this research by applying the correction of
604 light scattering distortion algorithms and methods that lead to increase signal to noise
605 ratio.

606

607 **Acknowledgments**

608 The authors are grateful for the financial and technical support received from
609 University of Tehran, University of Kurdistan, and Leibniz Institute for Agricultural
610 Engineering Potsdam-Bornim (ATB) for this project.

611

612 **References**

613 Baranyai, L., Zude, M., 2009. Analysis of laser light propagation in kiwi fruit using
614 backscattering imaging and Monte Carlo simulation. *Comput. Electron. Agric.*
615 69, 33–39.

616 Bevk, M., Kononenko, I., 2002. A statistical approach to texture description of
617 medical images: A preliminary study. *Proceedings of the 15th IEEE Symposium*
618 *on Computer-Based Medical Systems (CBMS 2002)*, 239-244.

619 Bharati, M.H., Liu, J.J., MacGregor, J.F., 2004. Image texture analysis: methods and
620 comparisons. *Chemometr. Intell. Lab. 72*, 57–71.

621 Choudhary, R., Paliwal, J., Jayas, D. S., 2008. Classification of cereal grains using
622 wavelet, morphological, colour, and textural features of non-touching kernel
623 images. *Biosyst. eng. 99*, 330-337.

624 Costa, A.F., Humpire-Mamani, G.E., Traina, A.J.M., 2012. An efficient algorithm for
625 fractal analysis of textures. In *SIBGRAPI 2012: XXV Conference on Graphics,*
626 *Patterns, and Images*, 39-46.

627 Garcia-Ramos, F.J., Valero, C., Homer, I., Ortiz-Canavate, J., Ruiz-Altisent, M.,
628 2005. Non-destructive fruit firmness sensors: a review. *Span. J. Agric. Res. 3(1)*,
629 61-73.

630 Gonzalez, R.C., Woods, R.E., Eddins, S.L., 2004. *Digital Image Processing using*
631 *MATLAB*. Pearson Prentice Hall, New Jersey, USA.

632 Haralick, R.M., 1979. Statistical and structural approaches to texture. *P. IEEE. 67*,
633 786–804.

634 Haralick, R.M., Shanmugam, K., Dinstein, I., 1973. Textural features for image
635 classification. *IEEE. T. Syst. Man. Cyb. 6*, 610–621.

636 Jackman, P., Sun, D.W., 2012. Recent advances in image processing using image
637 texture features for food quality assessment. *Tr. Food. Sci. Tec. 29(1)*, 35-43.

638 Jain, A., 1989. *Fundamentals of Digital Image Processing*. Prentice Hall International,
639 Englewood Cliffs, USA.

640 Jang, J.S.R., 1993. ANFIS: adaptive-network-based fuzzy inference system. *IEEE. T.*
641 *Syst. Man. Cyb.* 23(3), 665-685.

642 Leardi, R., 2000. Application of genetic algorithm-PLS for feature selection in
643 spectral data set. *J. Chemometr.* 14, 643-655.

644 Lu, R., 2004. Multispectral imaging for predicting firmness and soluble solids content
645 of apple fruit. *Postharvest. Biol. Tec.* 31, 147–157.

646 Mallat, S.G., 1989. A theory for multiresolution signal decomposition: the wavelet
647 representation. *IEEE. T. Pattern. Anal.* 11(7), 674-693.

648 Mireei, S.A., 2010. *Nondestructive Determination of Effective Parameters on*
649 *Maturity of Mozafati and Shahani Date Fruits by NIR Spectroscopy Technique.*
650 *PhD Dissertation. Department of Mechanical Engineering of Agricultural*
651 *Machinery. University of Tehran. Iran. In Persian.*

652 Mohsenin, N.N., 1986. *Physical Properties of Plant and Animal Materials, Second*
653 *Edition Revised.* Gordon and Breach Science, NY, USA.

654 Mollazade, K., Omid, M., Akhlaghian Tab, F., Mohtasebi, S.S. 2012a. Principles and
655 applications of light backscattering imaging in quality evaluation of agro-food
656 products: a review. *Food. Bioprocess. Tech.* 5(5), 1465-1485.

657 Mollazade, K., Omid, M., Akhlaghian Tab, F., Mohtasebi, S. S., Zude, M., 2012b.
658 *Spatial mapping of moisture content in tomato fruits using hyperspectral imaging*
659 *and artificial neural networks. 4th International Workshop on Computer Image*
660 *Analysis in Agriculture, 09 - 11 July, Valencia, Spain.*

661 Nicolai, B.M., Beullens, K., Bobelyn, E., Peirs, A., Saeys, W., Theron, K.I.,
662 Lammertyn, J., 2007. Nondestructive measurement of fruit and vegetable quality
663 by means of NIR spectroscopy: a review. *Postharvest. Biol. Tec.* 46, 99-118.

664 Noh, H.K., Lu, R., 2007. Hyperspectral laser-induced fluorescence imaging for
665 assessing apple fruit quality. *Postharvest. Biol. Tec.* 43, 193–201.

666 Ojala, T., Pietikäinen, M., Mäenpää, T., 2002. Multiresolution grey-scale and rotation
667 invariant texture classification with local binary patterns. *IEEE. T. Pattern. Anal.*
668 24(7), 971-987.

669 Omid, M., Mahmoudi, A., Omid, M.H., 2009. An intelligent system for sorting
670 pistachio nut varieties. *Expert. Syst. Appl.* 36, 11528–11535.

671 Omid, M., Mahmoudi, A., Omid, M.H., 2010. Development of pistachio sorting
672 system using principal component analysis (PCA) assisted artificial neural
673 network (ANN) of impact acoustics. *Expert. Syst. Appl.* 37, 7205–7212.

674 Peng, Y., Lu, R., 2005. Modeling multispectral scattering profiles for prediction of
675 apple fruit firmness. *Trans. ASAE.* 48(1), 235–242.

676 Peng, Y., Lu, R., 2006. Improving apple fruit firmness predictions by effective
677 correction of multispectral scattering images. *Postharvest. Biol. Tec.* 41, 266–
678 274.

679 Peng, Y., Lu, R., 2007. Prediction of apple fruit firmness and soluble solids content
680 using characteristics of multispectral scattering images. *J. Food. Eng.* 82, 142–
681 152.

682 Qin, J., Lu, R., 2006. Measurement of the optical properties of apple using
683 hyperspectral diffuse reflectance imaging. *ASABE Paper No. 063037.* St. Joseph,
684 Mich.: ASABE.

685 Qing, Z., Ji, B., Zude, M. 2007., Predicting soluble solid content and firmness in apple
686 fruit by means of laser light backscattering image analysis. *J. Food. Eng.* 82, 58–
687 67.

688 Qing, Z., Ji, B., Zude, M., 2008. Non-destructive analysis of apple quality parameters
689 by means of laser-induced light backscattering imaging. *Postharvest. Biol. Tec.*
690 48, 215–222.

691 Sarkar, A., Sharma, K., Sonak, R., 1997. A new approach for subset 2-D AR model
692 identification for describing textures. *IEEE. T. Image. Process.* 6(3), 407-413.

693 Sukissian, L., Kollias, S., Boutalis, Y., 1994. Adaptive classification of textured
694 images using linear prediction and neural networks. *Signal. Process.* 36, 209-232.

695 Tamura, H., Mori, S., Yamawaki, T., 1978. Textural features corresponding to visual
696 perception. *IEEE Transactions on Systems, Man, and Cybernetics*, 8, 460–472.

697 Tang, X., 1998. Texture information in run-length matrices. *IEEE. T. Image. Process.*
698 (7), 1602-1609

699 Zheng, C., Sun, D.W., Zheng, L., 2006. Recent applications of image texture for
700 evaluation of food qualities—a review. *Tr. Food. Sci. Tec.* 17, 113–128.

701 Zhu, B., Jiang, L., Luo, Y., Tao, Y., 2007. Gabor feature-based apple quality
702 inspection using kernel principal component analysis. *J. Food. Eng.* 81, 741,749.

703 Zude, M., 2009. *Optical Monitoring of Fresh and Processed Agricultural Crops.* CRC
704 Press, Boca Raton, FL, USA, 450 (pp. 391).

705

706

Table 1. Data set specification

Sample	Number of samples	Storage condition	Storage time	Mechanical property	Mean	Min	Max	Standard deviation
Apple	59 Pinova 68 Elstar	T: 2 °C RH: 92±2 %	45 days	Firmness	59.85 (N/cm ²)	31.00 (N/cm ²)	84.50 (N/cm ²)	11.39 (N/cm ²)
Plum	180 Jojo 170 Tophit	T: 2 °C RH: 92±2 %	20 days	Firmness	3.86 (N/cm ²)	0.09 (N/cm ²)	11.40 (N/cm ²)	2.41 (N/cm ²)
Tomato	200 Pannovy	T: 15±1 °C RH: 92±2 %	30 days	Elasticity	0.43 (N/mm ²)	0.12 (N/mm ²)	1.75 (N/mm ²)	0.29 (N/mm ²)
Mushroom	200	T: 3±1 °C RH: 92±2 %	14 days	Elasticity	1.53 (N/mm ²)	0.21 (N/mm ²)	4.92 (N/mm ²)	1.06 (N/mm ²)

Table 2. Available texture features measured by statistical techniques for each backscattering image

1st order statistics of image histogram and local binary pattern		Grey level co-occurrence matrix		Grey level run length matrix	
Feature name	Formula*	Feature name	Formula**	Feature name	Formula***
Mean grey level	$\mu = \sum_{i=0}^{L-1} z_i p(z_i)$	Contrast	$\sum_{i,j} i-j ^2 p(i,j)$	Short run emphasis (SRE)	$\frac{\sum_{i=1}^{N_g} \sum_{j=1}^{N_r} \frac{r(i,j)}{j^2}}{\sum_{i=1}^{N_g} \sum_{j=1}^{N_r} r(i,j)}$
Standard deviation	$\sigma = \sqrt{\sum_{i=0}^{L-1} (z_i - \mu)^2 p(z_i)}$	Correlation	$\sum_{i,j} \frac{(i - \mu_i)(j - \mu_j) p(i,j)}{\sigma_i \sigma_j}$	Long run emphasis (LRE)	$\frac{\sum_{i=1}^{N_g} \sum_{j=1}^{N_r} j^2 r(i,j)}{\sum_{i=1}^{N_g} \sum_{j=1}^{N_r} r(i,j)}$
Smoothness	$1 - \frac{1}{1 + \sigma^2}$	Uniformity	$\sum_{i,j} p(i,j)^2$	Grey level non-uniformity (GLNU)	$\frac{\sum_{i=1}^{N_g} (\sum_{j=1}^{N_r} r(i,j))^2}{\sum_{i=1}^{N_g} \sum_{j=1}^{N_r} r(i,j)}$
Skewness	$\frac{1}{\sigma^3} \sum_{i=0}^{L-1} (z_i - \mu)^3 p(z_i)$	Homogeneity	$\sum_{i,j} \frac{p(i,j)}{1 + i-j }$	Run length non-uniformity (RLNU)	$\frac{\sum_{i=1}^{N_r} (\sum_{j=1}^{N_g} r(i,j))^2}{\sum_{i=1}^{N_g} \sum_{j=1}^{N_r} r(i,j)}$
Uniformity (energy)	$\sum_{i=0}^{L-1} P^2(z_i)$	Entropy	$-\sum_{i,j} p(i,j) \log p(i,j)$	Run percentage (RP)	$\frac{\sum_{i=1}^{N_g} \sum_{j=1}^{N_r} r(i,j)}{n_p}$
Entropy	$-\sum_{i=0}^{L-1} p(z_i) \log_2 p(z_i)$	Maximum of probability	$Max(p(i,j))$	Low grey level run emphasis (LGRE)	$\frac{\sum_{i=1}^{N_g} \sum_{j=1}^{N_r} \frac{r(i,j)}{i^2}}{\sum_{i=1}^{N_g} \sum_{j=1}^{N_r} r(i,j)}$
Kurtosis (4 th moment)	$\frac{1}{\sigma^4} \sum_{i=0}^{L-1} (z_i - \mu)^4 p(z_i)$	Dissimilarity	$\sum_{i,j} i-j p(i,j)$	High grey level run emphasis (HGRE)	$\frac{\sum_{i=1}^{N_g} \sum_{j=1}^{N_r} r(i,j) \cdot i^2}{\sum_{i=1}^{N_g} \sum_{j=1}^{N_r} r(i,j)}$
Coefficient of variation	$\frac{\sigma}{\mu}$	Cluster shade	$\sum_{i,j} ((i - \mu_i) + (j - \mu_j))^2 p(i,j)$	Short run low grey level emphasis (SRLGE)	$\frac{\sum_{i=1}^{N_g} \sum_{j=1}^{N_r} \frac{r(i,j)}{i^2 \cdot j^2}}{\sum_{i=1}^{N_g} \sum_{j=1}^{N_r} r(i,j)}$
		Cluster prominence	$\sum_{i,j} ((i - \mu_i) + (j - \mu_j))^4 p(i,j)$	Short run high grey level emphasis (SRHGE)	$\frac{\sum_{i=1}^{N_g} \sum_{j=1}^{N_r} \frac{r(i,j) \cdot i^2}{j^2}}{\sum_{i=1}^{N_g} \sum_{j=1}^{N_r} r(i,j)}$
		Variance	$\sum_{i,j} (i - \mu_i)^2 p(i,j)$	Long run low grey level emphasis (LRLGE)	$\frac{\sum_{i=1}^{N_g} \sum_{j=1}^{N_r} \frac{r(i,j) \cdot j^2}{i^2}}{\sum_{i=1}^{N_g} \sum_{j=1}^{N_r} r(i,j)}$
				Long run high grey level emphasis (LRHGE)	$\frac{\sum_{i=1}^{N_g} \sum_{j=1}^{N_r} r(i,j) \cdot i^2 \cdot j^2}{\sum_{i=1}^{N_g} \sum_{j=1}^{N_r} r(i,j)}$

* μ_n , z_i , $p(z_i)$, and L represent mean n^{th} moment, random variable related to intensity, normalized histogram of intensity levels, and number of possible intensity levels, respectively.

** σ is standard deviation, μ represents the mean, and $p(i, j)$ is grey level co-occurrence matrix.

*** $r(i, j)$, N_g , N_r , and n_p are run length matrix, number of grey levels in an image, number of run lengths, and sum of image pixels, respectively.

Table 3. The characteristics and statistical measures of the best models of ANFIS for predicting firmness/elasticity of some horticultural products by different texture analysis techniques

Product	Texture analysis technique	Type of mf		Number of Input mf	Optimization method	Calibration		Prediction	
		Input	Output			RMSECV	R _c	RMSEP	R _p
Apple	FOSH	Triangular	Linear	5	Hybrid	4.423	0.929	8.583	0.861
	GLCM	Trapezoidal	Linear	3	Hybrid	7.080	0.783	14.229	0.736
	GLRLM	Bell-shaped	Linear	4	Hybrid	2.357	0.979	12.119	0.701
	LBP	Triangular	Linear	4	Hybrid	3.129	0.962	14.825	0.512
	Wavelet	Trapezoidal	Linear	3	Hybrid	6.670	0.846	10.320	0.825
	Gabor	Gaussian	Constant	5	Hybrid	6.377	0.861	13.587	0.637
	Tamura	Trapezoidal	Linear	4	Hybrid	5.860	0.861	10.398	0.846
	Fractal	Sigmoid	Linear	3	Hybrid	5.954	0.869	8.998	0.826
	SAR	Bell-shaped	Constant	4	Hybrid	7.652	0.772	13.814	0.706
Plum	FOSH	Sigmoid	Linear	5	Hybrid	2.650	0.671	2.708	0.722
	GLCM	Triangular	Linear	5	Hybrid	2.091	0.623	3.325	0.659
	GLRLM	Sigmoid	Linear	5	Hybrid	1.862	0.686	2.044	0.697
	LBP	Trapezoidal	Constant	4	Hybrid	2.603	0.583	2.318	0.687
	Wavelet	Triangular	Linear	5	Hybrid	1.993	0.589	2.607	0.554
	Gabor	Trapezoidal	Linear	2	Hybrid	3.869	0.544	4.018	0.606
	Tamura	Sigmoid	Linear	5	Hybrid	1.809	0.692	2.444	0.712
	Fractal	Triangular	Linear	3	Hybrid	2.470	0.649	2.314	0.725
	SAR	Gaussian	Constant	4	Hybrid	1.968	0.645	1.722	0.757
Tomato	FOSH	Bell-shaped	Linear	3	Hybrid	0.325	0.648	0.356	0.678
	GLCM	Sigmoid	Linear	5	Hybrid	0.284	0.621	0.277	0.718
	GLRLM	Gaussian	Linear	4	Hybrid	0.268	0.621	0.344	0.675
	LBP	Gaussian	Linear	4	Hybrid	0.246	0.603	0.298	0.692
	Wavelet	Gaussian	Constant	4	Hybrid	0.258	0.677	0.237	0.795
	Gabor	Sigmoid	Linear	5	Hybrid	0.221	0.722	0.259	0.857
	Tamura	Gaussian	Linear	4	Hybrid	0.298	0.731	0.219	0.832
	Fractal	Triangular	Linear	4	Hybrid	0.295	0.685	0.339	0.791
	SAR	Sigmoid	Linear	3	Hybrid	0.256	0.740	0.425	0.706
Mushroom	FOSH	Gaussian	Constant	5	Hybrid	0.727	0.734	0.988	0.780
	GLCM	Sigmoid	Linear	4	Hybrid	0.789	0.721	1.331	0.780
	GLRLM	Sigmoid	Constant	4	Hybrid	0.791	0.699	0.782	0.779
	LBP	Bell-shaped	Linear	5	Hybrid	0.331	0.951	1.012	0.739
	Wavelet	Bell-shaped	Linear	3	Hybrid	0.832	0.724	1.477	0.746
	Gabor	Trapezoidal	Linear	4	Hybrid	0.695	0.742	0.994	0.788
	Tamura	Triangular	Linear	3	Hybrid	0.937	0.710	0.696	0.839
	Fractal	Triangular	Constant	5	Hybrid	0.643	0.803	1.005	0.780
	SAR	Bell-shaped	Constant	2	Hybrid	1.516	0.619	1.195	0.717

Table 4. The characteristics and statistical measures of the best models of ANFIS for predicting firmness/elasticity of some horticultural products by different space domain techniques

Product	Texture analysis technique	Type of mf		Number of Input mf	Optimization method	Calibration		Prediction	
		Input	Output			RMSECV	R _c	RMSEP	R _p
Apple	Total number of pixels	Trapezoidal	Linear	5	Hybrid	14.259	0.369	20.636	0.506
	Statistical features	Bell-shaped	Constant	4	Hybrid	7.961	0.720	11.883	0.761
	Radial averaging	Trapezoidal	Linear	4	Hybrid	7.621	0.861	11.254	0.789
	Lorentzian	Gaussian	Linear	5	Hybrid	8.209	0.755	14.536	0.753
	Gompertz	Sigmoid	Linear	3	Hybrid	11.512	0.497	15.831	0.562
	Farrel	Gaussian	Linear	4	Hybrid	8.671	0.672	10.332	0.823
Plum	Total number of pixels	Triangular	Constant	5	Hybrid	3.342	0.317	4.544	0.536
	Statistical features	Bell-shaped	Linear	4	Hybrid	1.682	0.723	2.195	0.754
	Radial averaging	Trapezoidal	Constant	4	Hybrid	2.031	0.593	2.408	0.630
	Lorentzian	Trapezoidal	Constant	4	Hybrid	2.568	0.252	4.496	0.411
	Gompertz	Triangular	Linear	2	Hybrid	2.544	0.457	3.056	0.450
	Farrel	Triangular	Constant	5	Hybrid	2.461	0.413	2.206	0.710
Tomato	Total number of pixels	Trapezoidal	Constant	2	Hybrid	0.471	0.689	0.374	0.668
	Statistical features	Bell-shaped	Linear	3	Hybrid	0.197	0.841	0.278	0.792
	Radial averaging	Gaussian	Linear	4	Hybrid	0.143	0.911	0.257	0.795
	Lorentzian	Triangular	Linear	4	Hybrid	0.186	0.811	0.360	0.789
	Gompertz	Triangular	Linear	2	Hybrid	0.197	0.755	0.289	0.773
	Farrel	Trapezoidal	Constant	2	Hybrid	0.254	0.834	0.345	0.796
Mushroom	Total number of pixels	Bell-shaped	Constant	4	Hybrid	1.123	0.284	1.584	0.499
	Statistical features	Triangular	Linear	4	Hybrid	0.861	0.772	0.968	0.744
	Radial averaging	Trapezoidal	Linear	3	Hybrid	0.587	0.843	0.841	0.827
	Lorentzian	Triangular	Linear	5	Hybrid	1.175	0.352	1.257	0.627
	Gompertz	Bell-shaped	Constant	3	Hybrid	1.219	0.381	0.999	0.642
	Farrel	Gaussian	Linear	4	Hybrid	0.837	0.637	1.062	0.701

Table 5. The list of top real-time features selected by GA for predicting mechanical properties of different type of horticultural products

Apple		Plum		Tomato		Mushroom	
Texture analysis	Space domain statistics	Texture analysis	Space domain statistics	Texture analysis	Space domain statistics	Texture analysis	Space domain statistics
FOSH (skewness)	Farrell (μ_s')	LBP (kurtosis)	Lorentzian (c)	Wavelet (mean-diagonal-2)	Lorentzian (b)	GLCM (Contrast-45°)	Farrell (μ_a)
FOSH (entropy)	Lorentzian (b)	Wavelet (mean-vertical-1)	Gompertz (α)	Wavelet (mean-vertical-3)	Lorentzian (d)	GLCM (Contrast-90°)	Lorentzian (c)
FOSH (coefficient of variation)		Wavelet (mean-horizontal-2)	Statistical features (mean)	Wavelet (mean-vertical-4)	Gompertz (β)	Wavelet (mean-vertical-2)	
Wavelet (standard deviation- horizontal-4)		Wavelet (mean-vertical-2)		SAR (θ_3)	Statistical features (min)	Wavelet (mean-diagonal-3)	
Wavelet (energy-horizontal-1)		Wavelet (mean-diagonal-2)		SAR (θ_4)		Wavelet (mean-vertical-4)	
Wavelet (energy-horizontal-4)		SAR (θ_1)					
Wavelet (entropy-horizontal-1)		SAR (θ_2)					
Wavelet (entropy-approximation-3)							
Wavelet (entropy-horizontal-4)							
Wavelet (entropy-vertical-1)							

FOSH: First order statistics of image histogram, LBP: Local Binary pattern, SAR: Simultaneous autoregressive model, GLCM: Grey level co-occurrence matrix

Table 6. The characteristics and statistical measures of the best models of ANFIS for predicting firmness/elasticity of some horticultural products by selected features from real-time texture analysis techniques

Product	Type of mf		Number of Input mf	Optimization method	Calibration		Prediction	
	Input	Output			RMSECV	R _c	RMSEP	R _p
Apple	Trapezoidal	Constant	4	Hybrid	6.288	0.907	12.474	0.872
Plum	Trapezoidal	Linear	4	Hybrid	1.948	0.724	3.287	0.776
Tomato	Triangular	Linear	2	Hybrid	0.242	0.767	0.203	0.853
Mushroom	Trapezoidal	Constant	4	Hybrid	0.783	0.722	0.896	0.872

Table 7. The characteristics and statistical measures of the best models of ANFIS for predicting firmness/elasticity of some horticultural products by selected features from real-time space domain techniques

Product	Type of mf		Number of Input mf	Optimization method	Calibration		Prediction	
	Input	Output			RMSECV	R _c	RMSEP	R _p
Apple	Trapezoidal	Linear	5	Hybrid	10.940	0.723	10.989	0.847
Plum	Triangular	Linear	3	Hybrid	2.249	0.668	1.687	0.762
Tomato	Sigmoid	Linear	5	Hybrid	0.179	0.863	0.260	0.864
Mushroom	Trapezoidal	Constant	2	Hybrid	0.870	0.603	1.278	0.764

Figure 1. Wavelet decomposition of backscattering image of a tomato sample at 660 nm using a fourth-order Daubechies mother wavelet (Db4)

Figure 2. Magnitude of Gabor wavelet transform obtained for backscattering image of a tomato sample at 660 nm in different directions and frequencies

Figure 3. The process of extracting the fractal features from backscattering image of a tomato sample at 660 nm by segmentation-based fractal texture analysis (SFTA) algorithm

Figure 4. The selection pattern of neighborhoods for a pixel at position s in the simultaneous autoregressive (SAR) model. The neighboring pixels are left, left-up, up, and right-up.

Figure 5. Processing time required to extract features from backscattering images of horticultural products by different texture analysis techniques

Figure 6. Processing time required to extract features from backscattering images of horticultural products by different space domain techniques

Figure 7. Results of predicting firmness/elasticity by fusion the selected features from real-time texture analysis and space domain feature sets for A. Apple, B. Plum, C. Tomato, and D. Mushroom. Red and blue dots represent the calibration and prediction data, respectively.

Figure 1
[Click here to download Figure: Figure 1.docx](#)

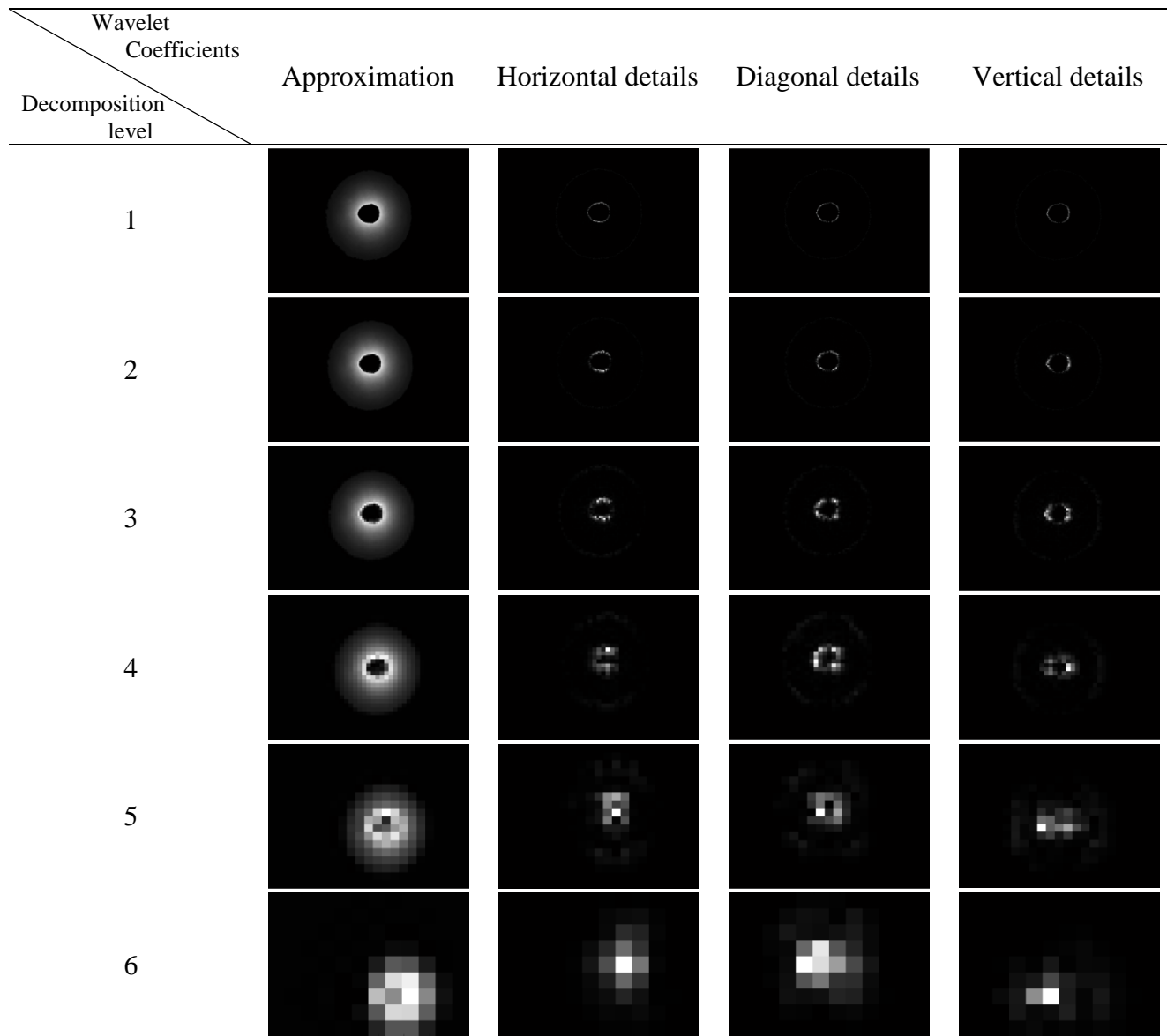
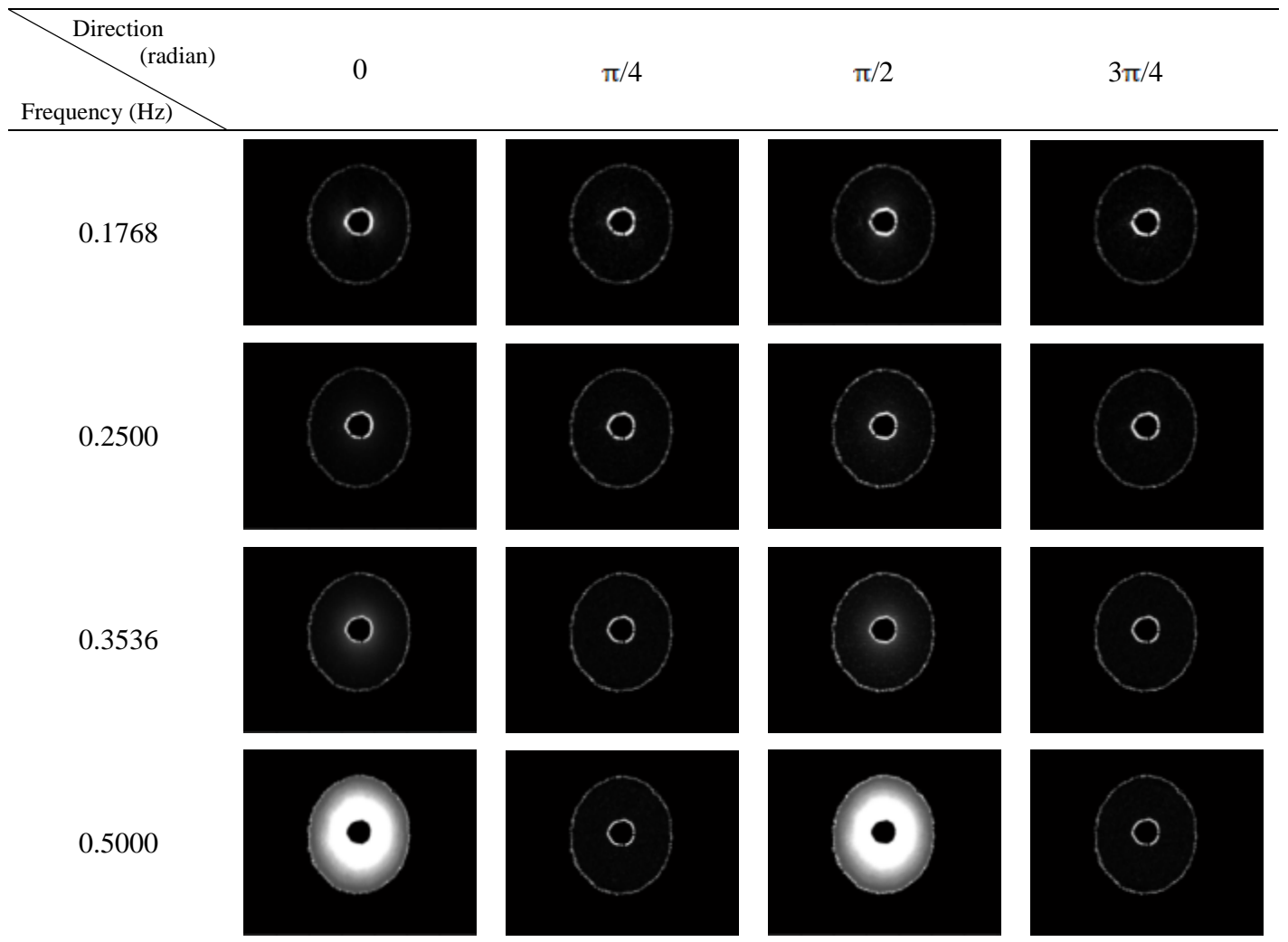


Figure 2
[Click here to download Figure: Figure 2.doc](#)



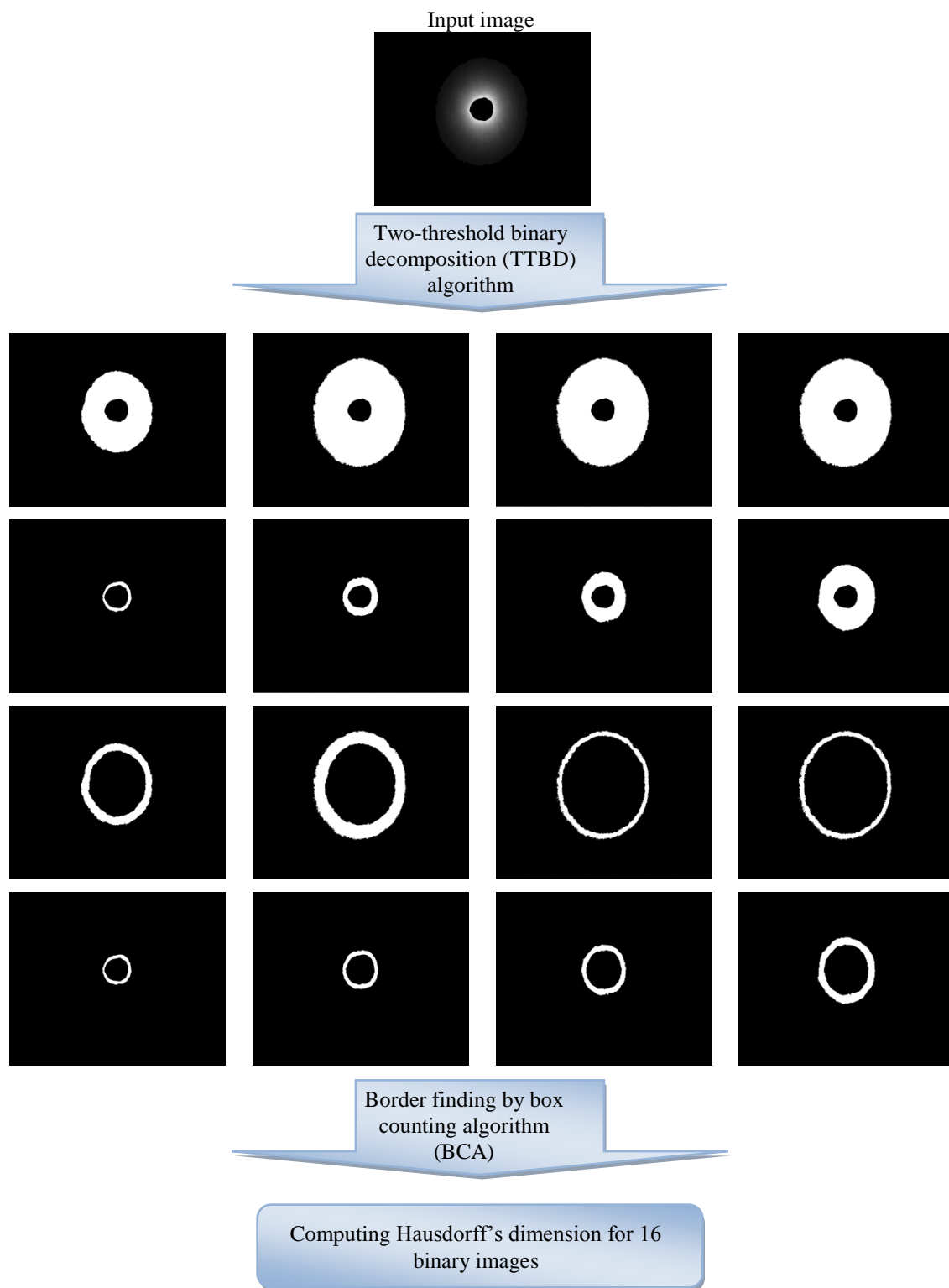


Figure 4

[Click here to download Figure: Figure 4.docx](#)

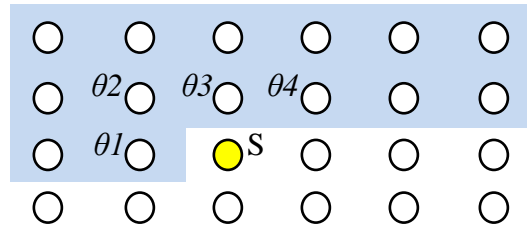


Figure 5
[Click here to download Figure: Figure 5.docx](#)

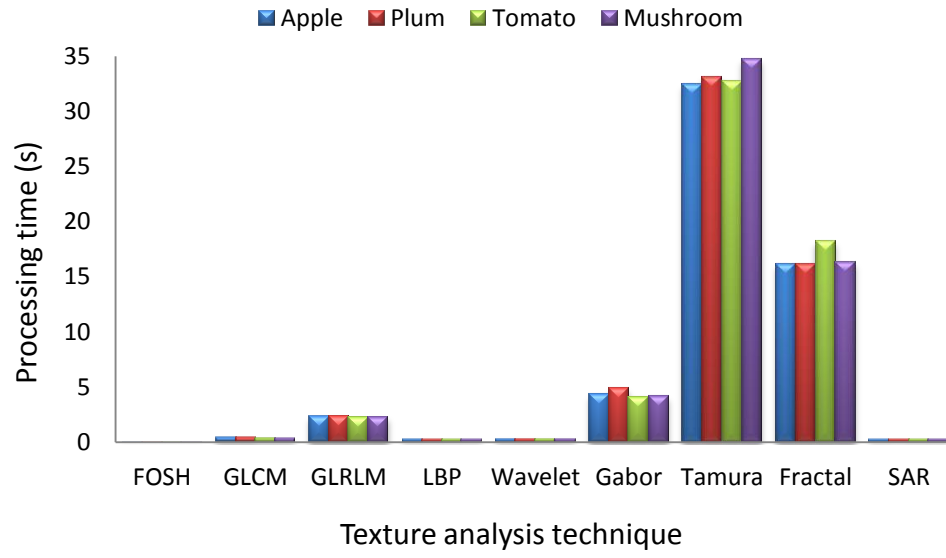


Figure 6
[Click here to download Figure: Figure 6.docx](#)

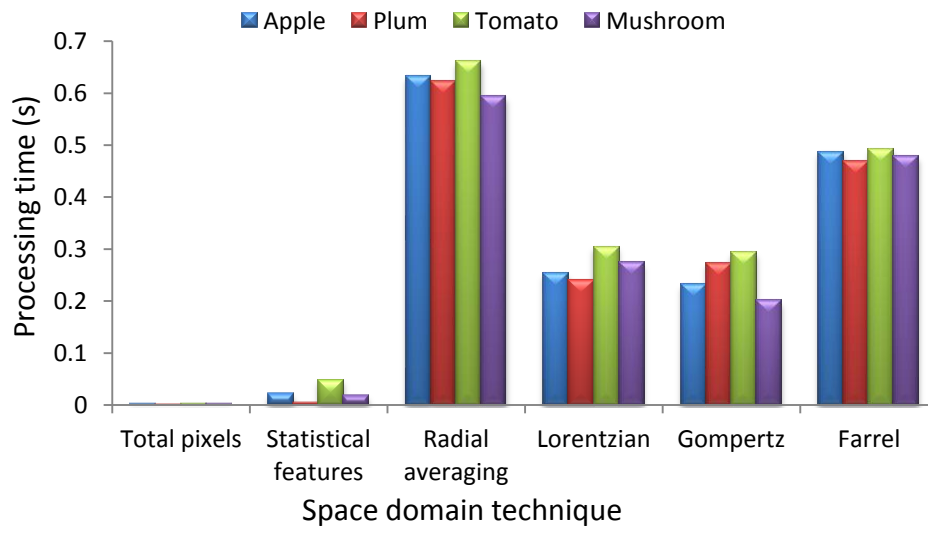


Figure 7

[Click here to download Figure: Figure 7.docx](#)

