Improving the Feasibility Pump

Tobias Achterberg*, Timo Berthold[†] September 23, 2005

Abstract

The Feasibility Pump described by Fischetti, Glover, and Lodi [8] and Bertacco, Fischetti, and Lodi [6] has proved to be a very successful heuristic for finding feasible solutions of mixed integer programs. The quality of the solutions in terms of the objective value, however, is sometimes quite poor. This paper proposes a slight modification of the algorithm in order to find better solutions. Extensive computational results show the success of this variant: for 89 out of 121 MIP instances the modified version produces improved solutions in comparison to the original Feasibility Pump.

Keywords: mixed integer programming, primal heuristics, feasibility pump

1 Introduction

A mixed integer program can be stated as

(MIP)
$$\min \{c^T x \mid Ax \leq b, \ l \leq x \leq u, \ x_j \in \mathbb{Z} \text{ for all } j \in I\}$$

with $A \in \mathbb{R}^{m \times n}$, $b \in \mathbb{R}^m$, $c, l, u \in \mathbb{R}^n$, and $I \subseteq N = \{1, \ldots, n\}$. Furthermore, let $B \subseteq I$ be the set of binary variables. For solving such problems it is important to quickly find feasible solutions of high quality: a good primal bound helps to cut off suboptimal branches in the search tree of a branch-and-bound based algorithm, and improvement heuristics like Local Branching [9], guided dives, and RINS [7] can only be applied after a feasible solution has been found.

Several heuristic methods to produce feasible solutions for (MIP) have been proposed in the literature, including Hillier [14], Balas and Martin [4], Saltzman and Hillier [19], Glover and Laguna [10, 11, 12], Løkketangen and Glover [16], Glover et al. [13], Nediak and Eckstein [18], and Balas et al. [3, 5].

The so-called Feasibility Pump was proposed by Fischetti, Glover, and Lodi [8] and improved by Bertacco, Fischetti, and Lodi [6]. This heuristic turned out to be very successful in finding feasible solutions even for very hard MIP instances. However, the quality of these solutions in terms of their objective value is sometimes poor, which was observed in [6] for MIPs with general integer variables and which we also confirm in the computational results of Section 3.

This paper suggests a slight modification of the Feasibility Pump. In contrast to the original version, the modified *Objective Feasibility Pump* takes the objective function c of the MIP into account during the course of the algorithm. Computational results show that the solution quality can indeed be improved by our approach without losing the ability to find feasible solutions in a reasonable amount of time.

^{*}Konrad-Zuse-Zentrum für Informationstechnik Berlin, achterberg@zib.de

[†]Konrad-Zuse-Zentrum für Informationstechnik Berlin, berthold@zib.de

The rest of the paper is organized as follows. The remainder of Section 1 reviews the original version of the Feasibility Pump as described by Bertacco, Fischetti, and Lodi [6]. Section 2 introduces the modifications included in the Objective Feasibility Pump. Finally, Section 3 gives computational results on a large test set of 121 MIP instances from the MIPLIB 2003 [2], the Mittelmann test set [17], and instances from Danna et al. [7].

1.1 The Feasibility Pump

The Feasibility Pump heuristic proceeds as follows: First the LP relaxation

(LP)
$$\min \{c^T x \mid Ax \leq b, \ l \leq x \leq u\}$$

of (MIP) is solved. Then, for S = B or S = I (see Section 1.2), the LP solution x^* is rounded to a vector $\tilde{x} = [x^*]^S$, with $[\cdot]^S$ defined by

$$[x]_j^S := \begin{cases} \lfloor x_j + 0.5 \rfloor & \text{if } j \in S \\ x_j & \text{if } j \notin S. \end{cases}$$
 (1)

If \tilde{x} is not feasible, an additional LP is solved in order to find a new point in the LP polyhedron

$$P := \{ x \in \mathbb{R}^n \mid Ax \le b, \ l \le x \le u \}$$

which is, w.r.t. the integer variables of S, closest to \tilde{x} , i.e., that minimizes

$$\Delta^{S}(x, \tilde{x}) := \sum_{j \in S} |x_j - \tilde{x}_j|.$$

The procedure is iterated using this point as new solution $x^* \in P$. Thereby, the algorithm creates two sequences of points: one with points x^* that fulfill the inequalities, and one with points \tilde{x} that fulfill the integrality requirements. The algorithm terminates if the two sequences converge or if a predefined iteration limit is reached.

In order to determine a point

$$x^* := \operatorname{argmin}\{\Delta^S(x, \tilde{x}) \mid x \in P\}$$
 (2)

in P, which is nearest to \tilde{x} , the following LP is solved:

$$\min \sum_{j \in S: \tilde{x}_{j} = l_{j}} (x_{j} - l_{j}) + \sum_{j \in S: \tilde{x}_{j} = u_{j}} (u_{j} - x_{j}) + \sum_{j \in S: l_{j} < \tilde{x}_{j} < u_{j}} d_{j}$$
s.t.
$$Ax \leq b$$

$$d \geq x - \tilde{x}$$

$$d \geq \tilde{x} - x$$

$$l \leq x \leq u.$$
(3)

The variables d_j are introduced to model the nonlinear function $d_j = |x_j - \tilde{x}_j|$ for integer variables x_j that are not equal to one of their bounds in the rounded solution \tilde{x} .

1.2 Implementational Issues

In the course of the algorithm, two main problems arise: First, the procedure can be caught in a cycle. That means, the same sequence of integer and LP-feasible points

is visited over and over again. Second, the progress in driving the integer points towards feasibility might be very slow. In [8] and [6] the first problem is handled by performing a so-called *restart* each time an integer point \tilde{x} is generated that was already visited in a prior iteration. In a restart a random perturbation step is executed, which shifts some of the variables randomly up or down and installs this perturbed vector as a new integer point \tilde{x} to continue the search.

To handle the second issue, the Feasibility Pump algorithm as described by Bertacco, Fischetti, and Lodi [6] is subdivided into three stages. At the first stage, a couple of iterations (so-called *pumping rounds*) are performed just on the binary variables S=B by relaxing the integrality conditions on the general integer variables. The first stage is stopped

- after an LP solution x^* was found with all binary variables being integral,
- the "fractionality" measure

$$f^S(x^\star) := \sum_{j \in S} f(x_j^\star) \quad \text{with} \quad f(x_j^\star) := \left| x_j^\star - \lfloor x_j^\star + 0.5 \rfloor \right| \text{ and } S = B$$

could not be decreased by at least p=10% in a certain number of iterations, or

• a pumping round limit is reached.

If the first stage does not yield a feasible solution, the second stage invokes pumping rounds taking all integer variables S=I into account. As initial integer point \tilde{x} one chooses a point visited in Stage 1 which was closest to the LP polyhedron. The second stage is aborted for analogous reasons as Stage 1 (using different parameter settings), or if 100 restarts have been performed in Stage 2.

If still no solution is found, a third stage is executed. Using a point \tilde{x} from Stage 2 closest to P, the MIP

$$\min \left\{ \Delta^{I}(x, \tilde{x}) \mid Ax \leq b, \ l \leq x \leq u, \ x_{j} \in \mathbb{Z} \text{ for all } j \in I \right\}$$
 (4)

is processed by a MIP solver which stops after the first feasible solution is found. One expects that the nearly feasible point \tilde{x} has integer feasible points in its vicinity. It is therefore likely that the MIP solver finds a feasible solution early in the search process if the objective function of (4) is used.

2 The Objective Feasibility Pump

Finding a high-quality solution of a MIP means to find a point $x \in \mathbb{R}^n$ satisfying three conditions: $x \in P$, $x_j \in \mathbb{Z}$ for all $j \in I$, and $c^T x$ is as small as possible. The Feasibility Pump generates sequences of points fulfilling the first and the second criteria, respectively, hopefully resulting in a point which satisfies both. However, despite the computation of the starting point, which is chosen to be the optimum of the LP relaxation, the third condition is disregarded. Therefore, the solution quality is usually rather poor, see Section 3.

For 0-1 MIPs Fischetti, Glover, and Lodi [8] address this issue by updating an objective limit each time a new solution has been found and calling the Feasibility Pump again on this restricted MIP. For MIPs with general integer variables Bertacco, Fischetti, and Lodi [6] propose to apply local search strategies like Local Branching [9] or RINS [7] to improve the solution.

We take a different approach. Instead of instantly discarding the original objective function of the MIP, we gradually reduce its influence and increase the weight of the artificial objective function $\Delta^S(\cdot,\tilde{x})$ of the Feasibility Pump. The hope is that we still converge to a feasible solution but concentrate the search on the region of high-quality points.

In the remainder of the paper we assume $c \neq 0$. Our modification of the Feasibility Pump replaces the distance function $\Delta^S(\,\cdot\,,\tilde{x})$ by a convex combination of $\Delta^S(\,\cdot\,,\tilde{x})$ and the original objective function vector c:

$$\Delta_{\alpha}^{S}(x,\tilde{x}) := (1 - \alpha)\Delta^{S}(x,\tilde{x}) + \alpha \frac{\sqrt{|S|}}{\|c\|} c^{T} x \quad \text{with } \alpha \in [0,1].$$
 (5)

Here, $\|\cdot\|$ is the Euclidean norm of a vector. Note that $\sqrt{|S|}$ is the Euclidean norm of the objective function vector of (3). We compute x^* using Δ_{α}^S instead of Δ^S in (2) by appropriately modifying the objective function of (3). In each pumping round α is geometrically decreased with a fixed factor $\varphi \in (0,1)$, i.e., $\alpha_{t+1} = \varphi \alpha_t$ and $\alpha_0 \in [0,1]$. With increasing iteration index t, this puts the emphasis more and more towards feasibility and decreases the influence of the original objective function. Note that you can obtain the original Feasibility Pump by choosing $\alpha_0 = 0$.

The introduction of Δ_{α}^{S} requires a modification of the cycle detection step in the Feasibility Pump algorithm. Especially during the first pumping rounds it might happen frequently that integer points are revisited, because of the higher resemblance of subsequent functions $\Delta_{\alpha}^{S}(\,\cdot\,,\tilde{x})$. Reaching the same point once again, however, does not automatically imply that the process runs into an infinite cycle like in the original heuristic. This is due to the fact that we are now using different directions $\Delta_{\alpha_t}^{S}$ in different iterations t in contrast to the old Δ^{S} , which only depends on the current integer point \tilde{x} . After α was decreased sufficiently, it is likely that the algorithm leaves the cycle. We therefore remember the visited points as pairs (\tilde{x}, α_t) and conduct a restart at iteration t only if the point \tilde{x} was already visited at iteration t' < t with $\alpha_{t'} - \alpha_t \le \delta_{\alpha}$ and $\delta_{\alpha} \in [0,1]$ being a fixed parameter value.

Instead of modifying the cycling detection as described above, one could also use different concepts like tabu lists (see, e.g., Glover and Laguna [12]). However, we tried to retain the proceeding of the original Feasibility Pump as close as possible in order to obtain good comparability between the two versions.

The pseudocode of the modified Feasibility Pump reads as follows.

Algorithm 2.1 (Objective Feasibility Pump) Stage 1:

- 1. Initialize $x^* := \operatorname{argmin}\{c^Tx \mid x \in P\}, \ S := B, \ \tilde{x} := [x^*]^S, \ t := 0, \ maxIter := maxIter_{ST1}, \ maxStalls := maxStalls_{ST1}, \ restarts := 0, \ L := \emptyset.$
- 2. If \tilde{x} did not change since the last iteration, round the T most fractional variables x_j^* , $j \in S$, to the other side compared to \tilde{x}_j (with T being a parameter).
- 3. While there exists $(\tilde{x}', \alpha_{t'}) \in L$ with $\tilde{x}' = \tilde{x}$ and $\alpha_{t'} \alpha_t \leq \delta_{\alpha}$, perform a random perturbation on \tilde{x} (see [6]) and set restarts := restarts + 1.
- 4. If \tilde{x} is feasible for (MIP) \rightarrow stop.
- 5. Set $L := L \cup \{(\tilde{x}, \alpha_t)\}$. Set t := t + 1, $\alpha_t := \varphi \alpha_{t-1}$.
- 6. If t > maxIter, goto next stage.

- 7. Solve $x^* := \operatorname{argmin} \{ \Delta_{\alpha_t}^S(x, \tilde{x}) \mid x \in P \}.$
- 8. If $x^* = \tilde{x}$, goto next stage.
- 9. If $f^S(x^*)$ did not decrease by at least a fraction $p \in (0,1)$ in the last maxStalls pumping rounds, goto next stage.
- 10. Set $\tilde{x} := [x^{\star}]^S$. Goto Step 2.

Stage 2:

- 1. Initialize \tilde{x} to be an integer point of Stage 1 with minimal $\Delta^B(x, \tilde{x}), x \in P$. Set t := 0, S := I, $maxIter := maxIter_{ST2}, maxStalls := maxStalls_{ST2}, restarts := 0, <math>L := \emptyset$.
- 2. Perform Steps 2 to 10 of Stage 1, but if restarts > maxRestarts in Step 3, goto Stage 3, and if $x^* = \tilde{x}$ in Step 8, stop.

Stage 3:

1. Solve MIP (4) with \tilde{x} being an integer point of Stage 2 with minimal $\Delta^{I}(x, \tilde{x})$, $x \in P$. Stop after the first feasible solution has been found.

3 Computational Results

This section compares the performances of the Feasibility Pump described in [6] and the Objective Feasibility Pump described in this paper. We thank Livio Bertacco, Matteo Fischetti, and Andrea Lodi for sending us the source code of their original version, in which we incorporated our ideas, thereby making a direct comparison possible. All computations were performed on a 3.4 GHz Pentium-4 with 512 KB cache and 3 GB RAM. CPLEX 9.03 [15] was used as underlying LP solver. We set a time limit of one hour in all runs.

3.1 Test Set and Settings

The computations were performed on a wide test set consisting of 121 instances taken from

- Miplib 2003 [2],
- the MIP collection of Mittelmann [17], and
- the instances used in [6], which are described in [7].

In all runs we used the parameter settings for the Feasibility Pump as suggested in [6], as follows. The maximum number of total iterations for Stages 1 and 2 were set to $maxIter_{ST1} = 10000$ and $maxIter_{ST2} = 2000$. The maximum number of iterations without a pumping cycle of at least p = 10% improvement were set to $maxStalls_{ST1} = 70$ and $maxStalls_{ST2} = 600$. The shifting in Step 2 is applied on a random number of $T \in [10, 30]$ variables, but only variables x_j with current fractionality $f(x_j^*) > 0.02$ are regarded as shifting candidates. For the unmodified Feasibility Pump we set $\alpha_0 = 0$, so as to deactivate all modifications. For the Objective Feasibility Pump we set $\alpha_0 = 1$, $\varphi = 0.9$, and $\delta_{\alpha} = 0.005$.

Because we wanted to investigate the performance of the Feasibility Pump used as a root node heuristic inside a MIP solver, we applied the MIP preprocessing

of CPLEX prior to running the Feasibility Pump algorithm itself. This usually avoids difficulties with the scaling of degenerated objective functions in the modified distance function Δ_{α}^{S} , see Equation (5). For example, some instances in our test set have objective functions consisting of only a single artificial variable which is defined as a linear combination of several other variables by an equality constraint. Such equations lead to unbalanced situations in the calculation of Δ_{α}^{S} , since in this case the norm $\|c\|$ of the objective function is misleading. We observed that MIP preprocessing usually resolves this issue.

We also applied CPLEX 9.03 to the problem instances in order to compare the Feasibility Pump to the primal heuristics of a state-of-the-art MIP solver. We deactivated all cutting planes as they are also not used in the Feasibility Pump, and stopped CPLEX after the root node was solved and the heuristics were applied.

3.2 Results

Table 1 and Table 2 compare the performance of the two Feasibility Pump versions. The left hand sides show the results of the original version proposed by Bertacco, Fischetti, and Lodi [6]. The central columns show the results of the Objective Feasibility Pump described in this paper. As an additional comparison the results of CPlex' root node heuristics are displayed in the right hand side columns. The column 'Objective' contains the objective values of the feasible solutions that were found with either algorithm. A bar '–' means that no solution was found within the time limit of one hour, or, in the case of CPlex, before branching took place. Values marked with a star ' \star ' indicate instances where the heuristic found an optimal solution. 'Gap' denotes the percentage gap γ to the optimal or best known solution of the corresponding instance. It is printed in bold face if the corresponding version of the Feasibility Pump produced a solution with a better or equal value than the other version. The gap is calculated as

$$\gamma := 100 \cdot \frac{(\tilde{c} - c^{\star})}{|c^{\star}|}$$

with \tilde{c} being the value of the heuristic solution and c^{\star} being the optimal or best known solution value of the instance. If $\tilde{c}=c^{\star}=0$ we define $\gamma:=0$. If $\tilde{c}>c^{\star}$ and $c^{\star}=0$ we define $\gamma:=\infty$. The instances displayed in italics in the tables are those for which we do not know the optimal solution. In this case we compare to the best solution we know, which was either generated by CPLEX 9.1 running for an hour with default settings, retrieved from the MIPLIB 2003 web site [1], or produced by one of the Feasibility Pump versions.

Column 'Time' shows the time in seconds to find a solution. The first geometric means at the bottom of Table 2 are calculated over the 116 instances for which a solution was found by both versions of the Feasibility Pump. The second geometric means are calculated over the 77 instances for which all three algorithms, including CPLEX, found a solution. In the calculations of the geometric means individual values smaller than 1 are replaced by 1.

As one can see in the tables the Objective Feasibility Pump produced a strictly better solution than the original version in 89 out of 121 cases, whereas the unmodified Feasibility Pump ranked first in 17 cases. For 11 instances both versions computed the same objective value, and for 4 instances both versions were not able to find any feasible solution within one hour. Only for one instance, namely acc-6, the original version could find a solution while the Objective Feasibility Pump did not succeed.

The running times usually differ only slightly in terms of absolute numbers. Only on some instances the Objective Feasibility Pump was significantly slower, namely on air04, dano3mip, momentum3, mzzv42z, rd-rplusc-21, the three dano instances, on qap10, acc-6, and neos16. However, for all those instances except acc-6 a better solution was found. The Objective Feasibility Pump was substantially faster on momentum1, protfold, t1717, icir97_potential, and neos10. Nevertheless, the solutions on these instances are at least as good as the ones of the unmodified Feasibility Pump. The quality improvement can also be seen in the geometric means: the mean gap to the optimal or best known solution was reduced from 43.9% to 23.3%, while the running time increased only slightly.

The comparison to CPLEX yields that the Feasibility Pump in both versions performs very well in finding an initial solution: the original version only fails on 4, the modified version on 5 instances, while CPLEX cannot find a solution in the root node for 43 instances. The Objective Feasibility Pump, however, produced solutions that are much closer to the ones of CPLEX w.r.t. quality. It could even find the optimal or best known solution in 12 cases, whereas this was achieved only 9 times by the original Feasibility Pump and only 8 times by CPLEX. These two properties—the ability to find solutions and their quite good quality—show that the Objective Feasibility Pump is indeed a reasonable root node heuristic.

The different behavior of the two Feasibility Pump versions is displayed in Figure 1 for selected problem instances. The figures show the evolution of the objective values of the LP solutions x^* and their fractionalities $f^I(x^*)$ during the course of the algorithm. The graphs on the left hand side arise from the unmodified version, while the ones on the right hand side arise from the Objective Feasibility Pump.

In the upper plots (aflow40b) one can see that the original version of the Feasibility Pump rapidly left the region of small objective values while the fractionality measure decreased quite fast. However, the algorithm was not able to drive the solution to integrality before restarting at iteration 10. At this point, the objective value was already far away from the optimal solution value of 1168. In contrast, the Objective Feasibility Pump stayed much closer to the optimal solution but did not decrease the fractionality measure as fast. Nevertheless, after 15 iterations a feasible solution was found with an objective value that was already exceeded after four iterations of the unmodified Feasibility Pump.

The two plots of rococoB11-010000 show an example where both versions produced a similar solution in the same number of iterations, although the two algorithms behaved differently. Again, the unmodified Feasibility Pump increased the objective value and decreased the fractionality faster than the Objective Feasibility Pump.

The bottom plots (rout) show a situation where the Objective Feasibility Pump is inferior. The original version performed 35 restarts, most of which can be seen as spikes in the fractionality graph. The last random perturbation at iteration 96 "coincidentally" produced a feasible solution. The Objective Feasibility Pump did not succeed to drive the fractionality to a value less than 0.5 until the last two iterations. Only six restarts were performed. Interestingly, the cycle between two points from iteration 12 to 30 was left without a restart just by decreasing α .

As already shown by Fischetti, Glover, and Lodi [8] and Bertacco, Fischetti, and Lodi [6] the Feasibility Pump is a useful heuristic for mixed integer programming, because it usually finds feasible solutions in a reasonable amount of time. Our results show that the modification presented in this paper further improves the Feasibility Pump: the quality of the resulting solutions is substantially enhanced with only a slight increase in the running time.

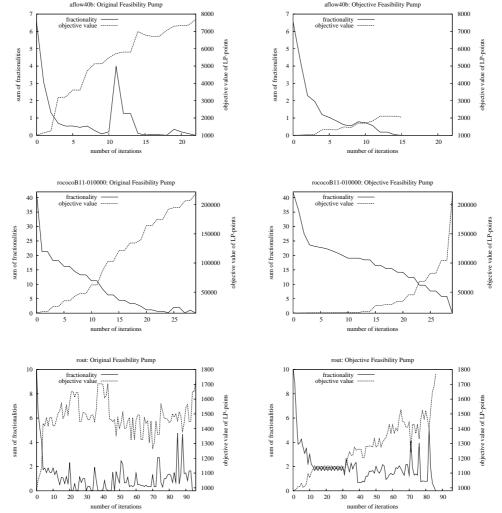


Figure 1. Evolution of the objective value and fractionality for aflow40b, rococoB11-010000, and rout.

Acknowledgements

We thank Livio Bertacco, Matteo Fischetti, and Andrea Lodi for providing the source code of their original Feasibility Pump.

References

- [1] T. Achterberg, T. Koch, and A. Martin. The mixed integer programming library: MIPLIB 2003. http://miplib.zib.de.
- [2] T. Achterberg, T. Koch, and A. Martin. MIPLIB 2003. Operations Research Letters, 2005. to appear.
- [3] E. Balas, S. Ceria, M. Dawande, F. Margot, and G. Pataki. OCTANE: A new heuristic for pure 0-1 programs. *Operations Research*, 49(2):207–225, 2001.
- [4] E. Balas and C. H. Martin. Pivot-and-complement: A heuristic for 0-1 programming. *Management Science*, 26(1):86–96, 1980.

- [5] E. Balas, S. Schmieta, and C. Wallace. Pivot and shift a mixed integer programming heuristic. *Discrete Optimization*, 1(1):3–12, June 2004.
- [6] L. Bertacco, M. Fischetti, and A. Lodi. A feasibility pump heuristic for general mixedinteger problems. Technical Report OR-05-5, University of Padova, Italy, May 2005.
- [7] E. Danna, E. Rothberg, and C. Le Pape. Exploring relaxation induced neighborhoods to improve MIP solutions. *Mathematical Programming*, 102(1):71–90, 2005.
- [8] M. Fischetti, F. Glover, and A. Lodi. The feasibility pump. Mathematical Programming, 104(1):91–104, 2005.
- [9] M. Fischetti and A. Lodi. Local branching. Mathematical Programming, 98(1-3):23-47, 2003.
- [10] F. Glover and M. Laguna. General purpose heuristics for integer programming part I. Journal of Heuristics, 3, 1997.
- [11] F. Glover and M. Laguna. General purpose heuristics for integer programming part II. *Journal of Heuristics*, 3, 1997.
- [12] F. Glover and M. Laguna. Tabu Search. Kluwer Academic Publisher, Boston, Dordrecht, London, 1997.
- [13] F. Glover, A. Løkketangen, and D. L. Woodruff. Scatter search to generate diverse MIP solutions. In M. Laguna and J. González-Velarde, editors, OR Computing Tools for Modeling, Optimization and Simulation: Interfaces in Computer Science and Operations Research, pages 299–317. Kluwer Academic Publishers, 2000.
- [14] F. S. Hillier. Efficient heuristic procedures for integer linear programming with an interior. Operations Research, 17:600–637, 1969.
- [15] ILOG CPLEX. Reference Manual, 2004. http://www.ilog.com/products/cplex.
- [16] A. Løkketangen and F. Glover. Solving zero/one mixed integer programming problems using tabu search. European Journal of Operations Research, 106:624–658, 1998.
- [17] H. Mittelmann. Decision tree for optimization software: Benchmarks for optimization software, 2003. http://plato.asu.edu/bench.html.
- [18] M. Nediak and J. Eckstein. Pivot, cut, and dive: A heuristic for 0-1 mixed integer programming. Technical Report RRR 53-2001, Rutgers University, 2001.
- [19] R. M. Saltzman and F. S. Hillier. A heuristic ceiling point algorithm for general integer linear programming. *Management Science*, 38(2):263–283, February 1992.

·	Original Feasibility Pump			Objective Feasibility Pump			CPLEX 9.03		
Name	Objective Gap % Time		Time	Objective Gap % Time			Objective Gap %		Time
10teams	958	4	1	952	3	5	_	_	0
a1c1s1	17762	53	1	16076.6	39	1	21029.4	81	0
aflow30a	2549	120	0	4105	254	0	1304	13	0
aflow40b	7682	558	0	2049	75	0	_	_	0
air04	58608	4	15	57298	2	164	56843	1	5
air05	30883	17	3	26942	2	8	27578	5	2
arki001	7.75064e+06	2	12	7.70474e+06	2	10	_	_	0
at lant a-ip	166.014	75	45	138.012	45	56	_	-	95
cap6000	-2.37503e+06	3	0	-2.42701e+06	1	0	-2.44946e+06	0	0
dano3mip	1000	43	30	769.25	10	383	761.9	9	145
danoint	93	42	1	87	32	3	66.5	1	0
disctom	-5000*	0	9	-5000*	0	11	-	-	16
ds	-	-	3600	_	-	3600	615.992	117	107
fast0507	245	41	20	179	3	21	177	2	39
fiber	4.01694e + 06	890	0	1.20751e+06	197	0	471805	16	0
fixnet6	9283	133	0	4807	21	0	4435	11	0
gesa2-o	4.91411e+07	91	0	2.6504e+07	3	0	_	-	0
gesa2	2.82478e+07	10	1	2.67652e+07	4	1	2.58091e+07	0	0
glass4	5.20005e + 09	333	0	3.10003e+09	158	0	-	-	0
harp2	-6.06939e+07	18	0	-5.58762e+07	24	0	-7.31719e+07	1	0
liu	6378	444	0	4100	250	1	5268	349	0
manna81	-12891	2	0	-12894	2	0	-13164*	0	3
markshare1	362	36100	0	194	19300	1	1095	109400	0
markshare2	1523	152200	0	365	36400	0	346	34500	0
mas74	18692.3	58	0	19033.1	61	0	14372.9	22	0
mas76	72860.6	82	0	50124	25	0	40005.1*	0	0
misc07	4100	46	1	3425	22	0	-	-	0
mkc	-288.01	49	0	-289.95	49	0	-499.464	11	0
mod011	-2.38751e+07	56	0	-4.56201e+07	16	1	-5.14737e+07	6	0
modglob	3.08143e+07	49	0	2.10876e+07	2	0	2.07868e+07	0	0
momentum1	359238	229	818	346535	218	223	-	-	26
momentum2	-	-	3600	_	_	3600	_	_	40
momentum3	509585	38	272	420724	14	599	_	_	2229
msc98- ip	3.02737e+07	30	34	3.02655e+07	30	38	_	_	57
mzzv11	-11286	48	118	-17688	19	112	_	-	59
mzzv42z	-12472	39	22	-15470	25	78	_	-	33
net12	337	57	8	337	57	14	_	_	37
noswot	-26	37	0	-40	2	0	-40	2	0
nsrand-ipx	78240	53	0	89120	74	1	56000	9	0
nw04	19124	13	3	17856	6	9	17056	1	1
opt1217	-16*	0	0	-16*		0	-16*		0
p2756	91972	2844	2	89266	2757	3	3555	14	0
pk1	78	609	0	83	655	0	31	182	0
pp08a	12180	66	1	10940	49	0	8070	10	0
pp08aCUTS	10750	46	0	8530	16	0	8050	10	0
protfold	-10	67 1564	683	-12	60	268	- 04.6065	171	11
qiu	1945.5	1564	0	625.709	571	700	94.6865	171	0
rd-rplusc-21	173065	1	375	171182*		790	_	_	15
roll3000	18812	46	0	24417.6	89	6	1760.01	-	0
rout	1720.82	60	0	1773.95	65	0	1768.21	64	0
set1ch	72987.8	34	1	84167.5	54	0	67334.5	23	0
seymour	527	25	1	445	5	3	435	3	10
sp97ar	9.57074e+08	44	3	9.40566e+08	42	3600	6.75288e+08	2	13
stp3d	1620.0	100	3600	1000.05	100	3600	1405 50	150	2036
swath	1630.8	192	3	1280.95	130	13	1405.58	152	0
t1717	237564	23	556	195779	1	171	_	-	27
timtab1	1.51227e+06	98	1	1.33858e+06	75	1	_	_	0
timtab2	1.91798e+06	58	1	1.73262e+06	42	4	_	_	0
tr12-30	269910	107	0	163794	25	0	16.05	- 10	0
vpm2	19.5	42	0	15.25	11	0	16.25	18	0

Table 1. Comparison of original feasibility pump and objective sensitive version

Name Objective Gap % Time Objective Gap % Time Objective bell3a 9.85707e+07 11121 0 7.21256e+07 8111 0 1.67409e+0 bell5 4.81498e+07 437 0 4.08948e+07 356 0 9.50297e+0 gesa3 3.5368e+07 26 0 2.89813e+07 4 1 2.80236e+0 gesa3.o 6.76543e+07 142 1 2.87697e+07 3 0 2.79914e+0 1152lav 4781 1 0 4757 1 0 3.627914e 1152lav	7 960 7 0 7 0 5 1 1 3 3 6 5 11 0 11 7 8 2 2 7 35 4 0 1 3 7 16 3 3 5 21 5 20 6 0 6 0 6 0 7 0 8 0 8 0 9 0 9 0 9 0 9 0 9 0 9 0 9 0 9	0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0
bell5 4.81498e+07 437 0 4.08948e+07 356 0 9.50297e+0 gesa3 3.5368e+07 26 0 2.89813e+07 4 1 2.80236e+0 gesa3_o 6.76543e+07 142 1 2.87697e+07 3 0 2.79914e+0 It52lav 4781 1 0 4757 1 0 475 stein45 45 50 0 35 17 0 475 ran8x32 6033 15 0 5817 11 0 555 ran10x26 5050 18 0 4231 15 0 408 ran12x21 4330 18 0 7156.21<	7 960 7 0 7 0 5 1 1 3 3 6 5 11 0 11 17 3 4 0 1 3 7 16 3 3 3 3 5 20 5 20 6 0 5 0 8 0 2 2	0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0
gesa3 3.5368e+07 26 0 2.89813e+07 4 1 2.80236e+07 24 1 2.87697e+07 3 0 2.79914e+015 1 0 4757 1 0 2.79914e+015 3 0 2.79914e+015 2.87697e+07 1 0 475 355 355 2.72814 2.87697e+07 1 0 355 2.72814 2.87697e+07 3 355 2.72814 0 355 2.72814 0 362 2.72814 0 355 1472 2.72814 0 362 2.72814 0 355 2.72814 0 352 33437 0 355 15 0 352 121624 0 1 121262 0 121624 0	7 0 0 7 7 0 7 7 0 7 5 1 1 3 3 3 6 6 5 11 1 0 11 1 7 3 5 2 2 2 7 3 5 5 21 1 5 5 20 6 6 0 0 5 * 0 8 0 2 2 2 2	0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0
gesa3_0 6.76543e+07 142 1 2.87697e+07 3 0 2.79914e+0 I152lav 4781 1 0 4757 1 0 475 stein45 45 50 0 35 17 0 475 ran8x32 6033 15 0 5817 11 0 555 ran10x26 5050 18 0 4833 13 0 477 ran12x21 4330 18 0 4231 15 0 406 ran13x13 3705 14 0 3820 17 0 351 binkar10_1 7170.23 6 0 7156.21 6 1 6874 eiID76 1616.97 83 10 2300.06 160 10 1196.67 irp 12715.3 5 2 12162.4 0 1 12162 mas284 105336 15 0 9552.7 9<	7 0 0 5 1 1 3 3 6 6 5 11 1 7 8 2 2 2 2 7 3 5 4 4 0 1 1 3 3 7 16 6 5 5 20 6 6 0 5 4 0 2 2 2 2 2	0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0
I152lav 4781 1 0 4757 1 0 475 stein45 45 50 0 35 17 0 35 ran8x32 6033 15 0 5817 11 0 553 ran10x26 5050 18 0 4833 13 0 477 ran12x21 4330 18 0 4231 15 0 406 ran13x13 3705 14 0 3820 17 0 351 binkar10_1 7170.23 6 0 7156.21 6 1 6874 eilD76 1616.97 83 10 2300.06 160 10 1196.9 irp 12715.3 5 2 12162.4 0 1 12162 mas284 105336 15 0 99522.7 9 0 93708 bc1 3.52343 6 2 5.4391 63 2 </td <td>5 1 1 3 3 6 6 5 11 1 17 8 7 2 2 2 7 35 4 0 11 3 3 7 16 5 2 20 6 6 0 5 * 0 8 0 2 2 2 2</td> <td>0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0</td>	5 1 1 3 3 6 6 5 11 1 17 8 7 2 2 2 7 35 4 0 11 3 3 7 16 5 2 20 6 6 0 5 * 0 8 0 2 2 2 2	0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0
stein45 45 50 0 35 17 0 35 ran8x32 6033 15 0 5817 11 0 555 ran10x26 5050 18 0 4833 13 0 408 ran12x21 4330 18 0 4231 15 0 408 ran13x13 3705 14 0 3820 17 0 355 binkar10_1 7170.23 6 0 7156.21 6 1 6874 eiID76 1616.97 83 10 2300.06 160 10 1196.2 mas284 105336 15 0 99522.7 9 0 93708 prod1 -42 25 0 -53 5 0 93708 prod1 -42 25 0 -53 5 0 93708 prod1 -42 25 0 -55.5 19 0	1 3 3 6 5 11 0 11 7 8 2 2 2 7 35 5 4 0 1 1 3 7 16 3 3 3 5 21 5 5 20 6 6 0 0 5 * 0 0 2 2 2 2	3 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0
ran8x32	33 65 11 00 11 7 8 22 2 2 7 35 4 4 0 11 3 7 16 3 3 3 5 21 5 20 6 6 0 5 5 0 8 0 2 2	0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0
ran10x26	5 11 0 11 7 8 2 2 2 7 35 4 0 1 3 7 16 3 3 3 5 21 5 20 6 0 6 0 5* 0 8 0 2 2	0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0
ran12x21	0 11 7 8 2 2 2 7 35 4 0 1 3 7 16 3 3 5 21 5 20 6 0 5* 0 8 0 2 2	0 0 0 0 0 0 0 0 0 0 0 0 152
ran13x13	7 8 2 2 7 35 4 0 1 3 7 16 3 3 5 21 5 20 6 0 5* 0 8 0 2 2	3 0 2 0 6 0 0 0 8 0 6 0 3 2 0 0 0 0
binkar10_1 7170.23 6 0 7156.21 6 1 6874 eilD76 1616.97 83 10 2300.06 160 10 1196.9 irp 12715.3 5 2 12162.4 0 1 12162 mas284 105336 15 0 99522.7 9 0 93708 prod1 -42 25 0 -53 5 0 9252.7 9 0 93708 bec1 3.52343 6 2 5.4391 63 2 3.4370 bienst1 72.9757 56 0 55.5 19 0 56.76 bienst2 38.2326 62 0 73.6667 35 1 65.2 dano3_4 646.702 12 26 576.345* 0 47 576.3 dano3_5 667.574 16 26 576.994 0 106 578.64 dmcc1 -522.815	2 2 2 7 35 4 0 1 3 7 16 3 3 5 21 5 20 6 0 5* 0 8 0 2 2	2 0 6 0 0 0 8 0 6 0 8 2 0 0 0 152
eilD76 1616.97 83 10 2300.06 160 10 1196.95 irp 12715.3 5 2 12162.4 0 1 12162 mas284 105336 15 0 99522.7 9 0 93708 prod1 -42 25 0 -53 5 0 93708 bc1 3.52343 6 2 5.4391 63 2 3.4370 bienst1 72.9757 56 0 55.5 19 0 56.75 bienst2 88.2326 62 0 73.6667 35 1 65.2 dano3_3 629.604 9 25 576.345* 0 47 576.33 dano3_4 646.702 12 26 576.994 0 106 578.64 dano3_5 667.574 16 26 576.994 0 106 578.64 meos1 85 347 1 68	7 35 4 0 1 3 7 16 3 3 5 21 5 20 6 0 5* 0 8 0 2 2	0 0 0 0 0 0 0 0 0 0 0 0 152
irp 12715.3 5 2 12162.4 0 1 12162 mas284 105336 15 0 99522.7 9 0 93708 prod1 -42 25 0 -53 5 0 -4 bc1 3.52343 6 2 5.4391 63 2 3.4370 bienst1 72.9757 56 0 55.5 19 0 56.7 bienst2 88.2326 62 0 73.6667 35 1 65.2 dano3_3 629.604 9 25 576.435* 0 47 576.33 dano3_4 646.702 12 26 576.435* 0 76 576.43 dano3_5 667.574 16 26 576.994 0 106 578.64 mkc1 -522.815 14 0 -563.1 7 0 -595.8 neos2 898.216 97 8 958.977	4 0 1 3 7 16 3 3 5 21 5 20 6 0 5* 0 8 0 2 2	0 0 8 0 6 0 8 2 0 0 0 152
mas284 105336 15 0 99522.7 9 0 93708 prod1 -42 25 0 -53 5 0 -24 bc1 3.52343 6 2 5.4391 63 2 3.4377 bienst1 72.9757 56 0 55.5 19 0 56.7 bienst2 88.2326 62 0 73.6667 35 1 65.2 dano3.3 629.604 9 25 576.345* 0 47 576.33 dano3.4 646.702 12 26 576.945* 0 47 576.33 dano3.5 667.574 16 26 576.994 0 106 578.64 mkc1 -522.815 14 0 -563.1 7 0 -595.8 neos1 85 347 1 68 258 1 2 neos2 898.216 97 8 958.977	1 3 7 16 3 3 5 21 5 20 6 0 5* 0 8 0 2 2	3 0 5 0 8 2 0 0 0 152
prod1 -42 25 0 -53 5 0 -42 bc1 3.52343 6 2 5.4391 63 2 3.4370 bienst1 72.9757 56 0 55.5 19 0 56.76 bienst2 88.2326 62 0 73.6667 35 1 65.2 dano3_3 629.604 9 25 576.345* 0 47 576.35 dano3_4 646.702 12 26 576.435* 0 76 576.43 dano3_5 667.574 16 26 576.935* 0 76 576.43 dano3_5 667.574 16 26 576.935* 0 76 576.43 mcs1 85 347 1 68 258 1 7 0 -595.8 neos1 85 347 1 68 258 1 2 neos2 898.216 97 8<	7 16 3 3 5 21 5 20 6 0 5* 0 8 0 2 2	0 3 2 0 0 0 152
bc1 3.52343 6 2 5.4391 63 2 3.4370 bienst1 72.9757 56 0 55.5 19 0 56.7 bienst2 88.2326 62 0 73.6667 35 1 65.2 dano3_3 629.604 9 25 576.345* 0 47 576.3 dano3_4 646.702 12 26 576.345* 0 76 576.43 dano3_5 667.574 16 26 576.994 0 106 578.64 dano3_5 667.574 16 26 576.994 0 106 578.64 mkc1 -522.815 14 0 -563.1 7 0 -595.8 neos1 85 347 1 68 258 1 2 neos2 898.216 97 8 958.977 111 7 neos3 1278.4 2241 12 1630.21 2886 8 neos4 -4.81256e+10 1 3 -4.8132e+10 1 3 -4.83137e+1 neos5 -4.81256e+10 1 4 -4.8132e+10 1 3 -4.83137e+1 neos6 137 65 4 93 12 12 neos7 5.2039e+06 621 0 1.10593e+06 53 1 neos7 5.2039e+06 621 0 1.10593e+06 53 1 seymour1 435.9 6 2 2214* 0 3 21 qap10 442 30 27 386 14 62 36 seymour1 435.9 6 2 427.063 4 3 412.63 swath1 499.711 32 1 439.106 16 2 swath2 1337.12 247 0 641.544 67 2 acc-0 0* 0 0 0 0* 0 0 acc-1 0 0* 0 2 0 0* 0 1 acc-2 0 0* 0 2 0* 0 3 acc-3 0 0* 0 10 0 0* 0 12 acc-4 - 3600 - 3600 acc-5 0 0* 0 1847 0 * 0 2054	3 3 5 21 5 20 6 0 5* 0 8 0 2 2	3 2 0 0 0 152
bienst1 72.9757 56 0 55.5 19 0 56.75 bienst2 88.2326 62 0 73.6667 35 1 65.2 dano3_3 629.604 9 25 576.345* 0 47 576.33 dano3_4 646.702 12 26 576.435* 0 76 576.43 dano3_5 667.574 16 26 576.994 0 106 578.64 mkc1 -522.815 14 0 -563.1 7 0 -595.8 neos1 85 347 1 68 258 1 2 neos2 898.216 97 8 958.977 111 7 1 68 28 8 1 2 2 286 8 8 1 2 2 4 83137e+1 1 7 1 1 3 -4.83137e+1 1 3 -4.83137e+1 1 1	5 21 5 20 6 0 5* 0 8 0 2 2	0 0 0 0 152
bienst2 88.2326 62 0 73.6667 35 1 65.2 dano3_3 629.604 9 25 576.345* 0 47 576.33 dano3_4 646.702 12 26 576.435* 0 76 576.43 dano3_5 667.574 16 26 576.994 0 106 578.64 mkc1 -522.815 14 0 -563.1 7 0 -595.8 neos1 85 347 1 68 258 1 2 neos2 898.216 97 8 958.977 111 7 11 7 11 7 11 7 11 7 11 7 11 7 11 7 11 7 11 7 11 7 11 7 11 7 11 7 11 7 11 7 11 7 11 11 12 14.8132e+10 <t< td=""><td>5 20 6 0 5* 0 8 0 2 2</td><td>0 152</td></t<>	5 20 6 0 5* 0 8 0 2 2	0 152
dano3_3 629.604 9 25 576.345* 0 47 576.33 dano3_4 646.702 12 26 576.435* 0 76 576.43 dano3_5 667.574 16 26 576.994 0 106 578.64 mkc1 -522.815 14 0 -563.1 7 0 -595.8 neos1 85 347 1 68 258 1 2 neos2 898.216 97 8 958.977 111 7	6 0 5* 0 8 0 2 2	152
dano3_4 646.702 12 26 576.435* 0 76 576.436 dano3_5 667.574 16 26 576.994 0 106 578.64 mkc1 -522.815 14 0 -563.1 7 0 -595.8 neos1 85 347 1 68 258 1 2 neos2 898.216 97 8 958.977 111 7 7 neos3 1278.4 2241 12 1630.21 2886 8 neos4 -4.81256e+10 1 3 -4.8132e+10 1 3 -4.83137e+1 neos5 -4.81256e+10 1 4 -4.8132e+10 1 3 -4.83137e+1 neos6 137 65 4 93 12 12 neos7 5.2039e+06 621 0 1.10593e+06 53 1 nug08 214* 0 2 214* 0 3	5* 0 8 0 2 2	
dano3_5 667.574 16 26 576.994 0 106 578.64 mkc1 -522.815 14 0 -563.1 7 0 -595.6 neos1 85 347 1 68 258 1 2 neos2 898.216 97 8 958.977 111 7 2 neos3 1278.4 2241 12 1630.21 2886 8 neos4 -4.81256e+10 1 3 -4.8132e+10 1 3 -4.83137e+1 neos5 -4.81256e+10 1 4 -4.8132e+10 1 3 -4.83137e+1 neos6 137 65 4 93 12 12 neos7 5.2039e+06 621 0 1.10593e+06 53 1 nug08 214* 0 2 214* 0 3 21 qap10 442 30 27 386 14 62 36	8 0 2 2	156
dano3_5 667.574 16 26 576.994 0 106 578.64 mkc1 -522.815 14 0 -563.1 7 0 -595.6 neos1 85 347 1 68 258 1 2 neos2 898.216 97 8 958.977 111 7 2 neos3 1278.4 2241 12 1630.21 2886 8 neos4 -4.81256e+10 1 3 -4.8132e+10 1 3 -4.83137e+1 neos5 -4.81256e+10 1 4 -4.8132e+10 1 3 -4.83137e+1 neos6 137 65 4 93 12 12 neos7 5.2039e+06 621 0 1.10593e+06 53 1 qap10 442 30 27 386 14 62 36 seymour1 435.9 6 2 427.063 4 3 41	8 0 2 2	
mkc1 -522.815 14 0 -563.1 7 0 -595.8 neos1 85 347 1 68 258 1 2 neos2 898.216 97 8 958.977 111 7 7 neos3 1278.4 2241 12 1630.21 2886 8 neos4 -4.81256e+10 1 3 -4.8132e+10 1 3 -4.83137e+1 neos6 137 65 4 93 12 12 neos7 5.2039e+06 621 0 1.10593e+06 53 1 nug08 214* 0 2 214* 0 3 21 qap10 442 30 27 386 14 62 36 seymour1 435.9 6 2 427.063 4 3 412.63 swath1 499.711 32 1 439.106 16 2 swath2 <td>2 2</td> <td>93</td>	2 2	93
neos1 85 347 1 68 258 1 2 neos2 898.216 97 8 958.977 111 7 neos3 1278.4 2241 12 1630.21 2886 8 neos4 -4.81256e+10 1 3 -4.8132e+10 1 3 -4.83137e+1 neos5 -4.81256e+10 1 4 -4.8132e+10 1 3 -4.83137e+1 neos6 137 65 4 93 12 12 neos7 5.2039e+06 621 0 1.10593e+06 53 1 nug08 214* 0 2 214* 0 3 21 qap10 442 30 27 386 14 62 36 seymour1 435.9 6 2 427.063 4 3 412.63 swath1 499.711 32 1 439.106 16 2 swath2		2 0
neos3 1278.4 2241 12 1630.21 2886 8 neos4 -4.81256e+10 1 3 -4.8132e+10 1 3 -4.83137e+1 neos5 -4.81256e+10 1 4 -4.8132e+10 1 3 -4.83137e+1 neos6 137 65 4 93 12 12 neos7 5.2039e+06 621 0 1.10593e+06 53 1 nug08 214* 0 2 214* 0 3 21 app10 442 30 27 386 14 62 36 seymour1 435.9 6 2 427.063 4 3 412.63 swath1 499.711 32 1 439.106 16 2 swath2 1337.12 247 0 641.544 67 2 acc-0 0* 0 0 0 0 0 acc-1 0*		2 0
neos3 1278.4 2241 12 1630.21 2886 8 neos4 -4.81256e+10 1 3 -4.8132e+10 1 3 -4.83137e+1 neos5 -4.81256e+10 1 4 -4.8132e+10 1 3 -4.83137e+1 neos6 137 65 4 93 12 12 neos7 5.2039e+06 621 0 1.10593e+06 53 1 nug08 214* 0 2 214* 0 3 20 qap10 442 30 27 386 14 62 36 seymour1 435.9 6 2 427.063 4 3 412.63 swath1 499.711 32 1 439.106 16 2 swath2 1337.12 247 0 641.544 67 2 acc-0 0* 0 0* 0 0 0 acc-1 0*		- 0
neos4 -4.81256e+10 1 3 -4.8132e+10 1 3 -4.8132e+10 1 3 -4.83137e+1 neos5 -4.81256e+10 1 4 -4.8132e+10 1 3 -4.83137e+1 1 3 -1.82137e+1 3 -2.82137e+1 2 2 2 2 2 2 3 2 2 3 3 2 2 3 3 2 3 3 4 12.62 3 3 4 12.63 3 3 4 12.63 <td></td> <td></td>		
neos5 -4.81256e+10 1 4 -4.8132e+10 1 3 -4.83137e+10 neos6 137 65 4 93 12 12 neos7 5.2039e+06 621 0 1.10593e+06 53 1 nug08 214* 0 2 214* 0 3 21 qap10 442 30 27 386 14 62 36 seymour1 435.9 6 2 427.063 4 3 412.63 swath1 499.711 32 1 439.106 16 2 swath2 1337.12 247 0 641.544 67 2 acc-0 0* 0 0 0 0 0 acc-1 0* 0 2 0* 0 1 acc-2 0* 0 0 0 12 acc-3 0* 0 10 0 0	0 1	
neos6 137 65 4 93 12 12 neos7 5.2039e+06 621 0 1.10593e+06 53 1 nug08 214* 0 2 214* 0 3 23 qap10 442 30 27 386 14 62 36 seymour1 435.9 6 2 427.063 4 3 412.63 swath1 499.711 32 1 439.106 16 2 swath2 1337.12 247 0 641.544 67 2 acc-0 0* 0 0 0 0 0 acc-1 0* 0 2 0* 0 1 acc-2 0* 0 2 0* 0 12 acc-3 0* 0 10 0* 0 12 acc-4 - - 3600 - - 3600 <t< td=""><td></td><td></td></t<>		
neos7 5.2039e+06 621 0 1.10593e+06 53 1 nug08 214* 0 2 214* 0 3 21 qap10 442 30 27 386 14 62 36 seymourl 435.9 6 2 427.063 4 3 412.63 swath1 499.711 32 1 439.106 16 2 swath2 1337.12 247 0 641.544 67 2 acc-0 0* 0 0 0 0 0 acc-1 0* 0 2 0* 0 1 acc-2 0* 0 2 0* 0 12 acc-3 0* 0 10 0 12 acc-4 - - 3600 - - 3600 acc-5 0* 0 1847 0* 0 2054		
nug08 214* 0 2 214* 0 3 21 qap10 442 30 27 386 14 62 36 seymour1 435.9 6 2 427.063 4 3 412.63 swath1 499.711 32 1 439.106 16 2 swath2 1337.12 247 0 641.544 67 2 acc-0 0* 0 0 0 0 0 acc-1 0* 0 2 0* 0 1 acc-2 0* 0 2 0* 0 3 acc-3 0* 0 10 0* 0 12 acc-4 - - 3600 - - 3600 acc-5 0* 0 1847 0* 0 2054		- 0
qap10 442 30 27 386 14 62 36 seymour1 435.9 6 2 427.063 4 3 412.63 swath1 499.711 32 1 439.106 16 2 swath2 1337.12 247 0 641.544 67 2 acc-0 0* 0 0* 0 0 0 acc-1 0* 0 2 0* 0 1 acc-2 0* 0 2 0* 0 3 acc-3 0* 0 10 0* 0 12 acc-4 - - 3600 - - 3600 acc-5 0* 0 1847 0* 0 2054	4* 0	
seymour1 435.9 6 2 427.063 4 3 412.63 swath1 499.711 32 1 439.106 16 2 swath2 1337.12 247 0 641.544 67 2 acc-0 0* 0 0 0* 0 0 acc-1 0* 0 2 0* 0 1 acc-2 0* 0 2 0* 0 3 acc-3 0* 0 10 0* 0 12 acc-4 - - 3600 - - 3600 acc-5 0* 0 1847 0* 0 2054	6 8	3 71
swath1 499.711 32 1 439.106 16 2 swath2 1337.12 247 0 641.544 67 2 acc-0 0* 0 0 0 0 0 acc-1 0* 0 2 0* 0 1 acc-2 0* 0 2 0* 0 3 acc-3 0* 0 10 0* 0 12 acc-4 - - 3600 - - 3600 acc-5 0* 0 1847 0* 0 2054		
swath2 1337.12 247 0 641.544 67 2 acc-0 0* 0 0 0 0 0 acc-1 0* 0 2 0* 0 1 acc-2 0* 0 2 0* 0 3 acc-3 0* 0 10 0* 0 12 acc-4 - - 3600 - - 3600 acc-5 0* 0 1847 0* 0 2054		
acc-0 0* 0 0 0* 0 0 acc-1 0* 0 2 0* 0 1 acc-2 0* 0 2 0* 0 3 acc-3 0* 0 10 0* 0 12 acc-4 - - 3600 - - 3600 acc-5 0* 0 1847 0* 0 2054		
acc-1 0* 0 2 0* 0 1 acc-2 0* 0 2 0* 0 3 acc-3 0* 0 10 0* 0 12 acc-4 - - 3600 - - 3600 acc-5 0* 0 1847 0* 0 2054	0* 0	
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	0* 0	
acc-3 0^* 0 10 0^* 0 12 acc-4 $ 3600$ $ 3600$ acc-5 0^* 0 1847 0^* 0 2054		
acc-4 $ -$ 3600 $ -$ 3600 acc-5 0^{\star} 0 1847 0^{\star} 0 2054	0* 0	
acc-5 0^{\star} 0 1847 0^{\star} 0 2054		
acc-0 0 0 1017 = - 3000		
<i>ic97_potential</i> 4568 15 2 4433 11 2		
ic97_tension 4487 14 1 4539 15 1		
icir97_tension 7309 14 8 7288 13 9		
icir97_potential 7724 17 62 7526 14 24		
nh97_potential 1598 13 10 1554 10 17		
<i>nh97_tension</i> 1575 4 10 1511* 0 11		_
B10-011000 117462 499 1 108472 453 1 3126		
<i>B10-011001</i> 117109 444 0 108472 404 1 4765		
B11-010000 219275 547 2 215163 535 1 8920		
B11-110001 206342 342 3 208823 347 4 7814		
B12-1111111 80931 89 46 83096 94 35		
C10-001000 255030 2124 0 159137 1288 0 2340		
C10-100001 239789 1135 1 134440 593 1		- 2
C11-010100 146524 450 1 136976 415 2 9064	0 241	
C11-011100 13024 430 1 130970 413 2 9004 C11-011100 130241 488 1 128149 479 1 3242		
C12-100000 534256 1283 4 456140 1080 5 10923		
	4 6/	
neos16 458 2 88 451 0 383 neos20 -199 54 3 -199 54 7		
		- 0
Geom. Mean (116) 43.9 3.2 23.3 3.8		- 2.4
Geom. Mean (77) 49.5 1.8 25.9 2.1		

Table 2. Comparison of original feasibility pump and objective sensitive version (cont'd)