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Abstract

In models of certification possible restrictions on the nature of the fee structures are commonly analyzed. We show that they are irrelevant for the certifier's ability to maximize profits and trade efficiency. Our results establish that certification schemes involve two substitutable dimensions—the fee structure and the disclosure rule. In the context of a canonical unit good certification setup, these dimensions act as perfect substitutes for achieving trade efficiency and (monotone) distributions of rents; adjustments in the disclosure dimension can fully mitigate restrictions in the fee dimension, but these changes do affect market transparency.

Keywords: certification, fee structures, disclosure rules, transparency

JEL classification: D82

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1 Introduction

Certifiers play a crucial role in many markets by making private information public, thereby mitigating adverse selection and potentially enhancing economic efficiency. However, their incentives may not always align with promoting efficiency. For example, commercial certifiers often prioritize profit maximization, which can conflict with the role of providing comprehensive information to market participants.

A notable case is credit rating agencies, whose services are vital to financial markets. Their performance during the 2007-2009 financial crisis raised concerns among regulators, who identified the agencies' fee structures as a contributing factor. Regulators argue that fee structures tied to certification outcomes encourage certification inflation, or the practice of awarding better certificates than warranted.

In response, regulatory proposals such as the Cuomo reform and the Franken amendment to the Dodd-Frank Act have recommended implementing flat fees, paid upfront and independent of certification outcomes, to better align incentives and promote transparency.²

Given this interest in the fee structure of certifiers, this paper provides a systematic study of its economic relevance in adverse selection markets. Our main insight is that restrictions on the fee structure are economically irrelevant for the certifier's profits and trade efficiency, and for the implementability of (monotone) distributions of rents.

The intuition for this irrelevance result is that certification schemes involve two dimensions — the fee structure and the disclosure rule. Our analysis shows that the two are perfect substitutes in that restrictions on fee structures can be fully compensated by adapting the certifier's disclosure rule.³ This explanation also reveals two limits of our irrelevance result: First, it breaks down if certifiers are unable to tailor their disclosure rules to the fee structure. Second and somewhat more subtle, certifiers' fee structures crucially affect the optimal disclosure rule and therefore the resulting transparency of markets. The subtlety is however that these differences in transparency have no impact on economic efficiency and profits.⁴

We derive these results by studying certification in a canonical model of adverse selection in the spirit of Akerlof (1970). A seller has private information on the value of the object to be traded. Expressing the seller's private information as his type, the seller's type can affect

¹In addition to fee structures, regulators have also expressed concerns about the initiators of certification. By focusing on fee structures for seller-initiated certification, we fully abstract from this regulatory dimension and refer to other literature (e.g. Stahl and Strausz, 2017).

²E.g., WSJ (2008) explains the Cuomo-reform stipulates fixed, up-front fees so that "the firms would get paid for their review, even if they aren't hired to rate the deal." (https://www.wsj.com/articles/SB121268203224348921 [last accessed Oct 26, 2022]). Such up-front payments were also part of the Franken amendment to the Dodd–Frank Act, which was eventually removed to allow for an extended review by the SEC (see Ozerturk, 2014).

³In the context of a moral hazard rather than a pure adverse selection market, Albano and Lizzeri (2001) note the substitutability between fees and disclosure rules, but apply this observation differently.

⁴Lizerri (1999)'s observation that the "intermediary reveals some information but only the minimal amount necessary to induce efficient trading behavior in the market" (p.224) is an expression of this subtlety.

both the seller's own consumption value and that of the buyer. The market interaction is such that any trade takes place at a price that equals the buyer's expected willingness to pay for the offered object. To this canonical setup, we introduce a profit-maximizing certifier, who can offer a certification scheme to the seller. The scheme prescribes both the fee structure and the disclosure rule by which the certification reveals the seller's private information. Given this setup, we study the extent to which different types of fee structures affect economic outcomes. The most flexible fee structure is a "type-contingent fee", which allows the fee to condition directly on the seller's (initially private) type. An intermediate form is a "certificate-contingent fee", which allows the fee to condition on the specific certificate that results from the certification process but not on the seller's type directly. The least flexible fee structure is a "flat fee" that is fixed and unresponsive to the certification outcome or to the seller's type.

Our first irrelevance result shows that the fee structure has no impact on market efficiency and the certifier's maximum profit. Not only type- and certificate-contingent fees but also flat fees enable the certifier to extract all gains from trade in excess of the seller's outside option, and these profit-maximizing schemes induce efficient trade. The disclosure rules that support this efficient and profit-maximizing outcome are however markedly different. While with type- and certificate-contingent fees the certifier can maximize profits with a fully revealing disclosure rule, this is not so with flat fees. The profit-maximizing disclosure rule under flat fees is necessarily coarser as it involves a pooling of low and high seller types to level their different willingness to pay for certification. Hence, even though with respect to profits and trade efficiency, the fee structure does not matter, it does affect market transparency. In particular, restricting profit-maximizing certifiers to use only flat fees leads to less transparent market outcomes. Yet, this difference in market transparency does neither impact trade efficiency nor the seller's profits.⁶

Our second result goes beyond considering a profit-maximizing certifier and concerns the potential distribution of rents between the certifier and the seller given an efficient market outcome.^{7,8} With a certificate contingent fee, any distribution of rents can be implemented, by charging the respective seller type an appropriate fee for the certificate that this type will be awarded. With flat fees, a distribution of rents is implementable for any prior if and only if the rents for *both* the seller and certifier are monotone increasing in the seller's type. These monotonicity requirements are necessary and sufficient for guaranteeing that

 $^{^5}$ We abstract from any moral hazard problems of certification and refer for such considerations to Ozerturk (2014) and Bizzotto and Vigier (2021).

⁶For papers that focus on the market transparency effect of certification see Pollrich and Wagner (2016), Stahl and Strausz (2017), Harbaugh and Rasmusen (2018), and Kattwinkel and Knoepfle (2022).

⁷Because in the canonical adverse selection setup, trade takes place at a price that equals the buyer's expected willingness to pay, buyer-rents are always zero.

⁸This relates our study to the literature on information design and achievable distributions of rents (e.g., Bergemann et al., 2015, Roessler and Szentes, 2017, or Kartik and Zhong, 2023). This literature, however, abstracts from the generation of informative certificates by a strategic third party, which is the focus of this paper.

the required pooling of types associated with the optimal flat-fee disclosure rule is feasible. Hence, fee schedules are also irrelevant for their ability to implement monotone distributions of rents.

The rest of the paper is organized as follows. In the next section, we present a canonical model of adverse selection, and discuss its relation to the existing literature. In Section 3, we derive equivalence results on profit-maximizing certification. Section 4 focuses on the distribution of rents. We conclude in Section 5.

2 Model

A canonical adverse selection market. A single buyer faces a single seller, who owns one unit of an indivisible good of a certain type. The good's type has $n \geq 1$ possible realizations.⁹ Hence, we denote the good's type by a number i of the index set $I_n \equiv \{1,\ldots,n\}$, the set of possible types. Initially, type $i \in I_n$ is drawn from the commonly known prior distribution $\boldsymbol{\pi} = (\pi_1,\ldots,\pi_n)$, where π_i denotes the probability that the good's type is i. Before deciding whether to sell her good, the seller observes the realization of this draw privately.

The good's type determines the consumption value of the good to both the buyer and seller. In particular, the buyer's (consumption) value of a good of type i is q_i , whereas its (consumption) value to the seller is s_i . We assume that trade is always efficient, i.e. $q_i \geq s_i$ for all i. Without loss of generality, we make the ordering assumption

$$q_1 \le q_2 \le \dots \le q_n.$$
 (Q-MON)

After learning the good's type i, the seller decides whether to offer her good for sale. Hence, when deciding to sell the good, she already knows that consuming the good herself yields her the value s_i . This is the first defining feature of an adverse selection market.

If the seller actually decides to sell the good, we assume that the market interaction is such that she sells it at a price equal to the buyer's expected valuation for the good. Importantly, the buyer's expectation is fully rational and, for instance, takes into account information contained in the fact that the good is offered for sale. That the selling price equals the buyer's rational expectation is the second defining feature of an adverse selection market.¹¹ As a consequence, a sale results in a price that always (weakly) exceeds q_1 . Hence, the seller's effective reservation value r_i for selling the good is given by $r_i = \max\{s_i, q_1\}$,

⁹We consider an adverse selection market with finite but arbitrarily many types, because, as explained in Remarks below, the proof of our result is based on an induction argument on the number of types. As the studies in the literature that use continuous type models are limits of an appropriate sequence of our canonical adverse selection model with finite types, our results also apply for these continuous type models.

¹⁰This assumption is inconsequential for our equivalence results, but simplifies the exposition and is standard in the literature.

¹¹One common micro-foundation for this assumption is that there are, in fact, two identical buyers who bid for the good in a second-price auction.

which is the least utility a seller with a good of type i can ever get. Throughout the paper, our equilibrium concept is Perfect Bayesian Equilibrium, and we make the following assumptions.

$$r_1 \le r_2 \le \ldots \le r_n$$
 (R-MON)

$$q_1 - r_1 \le q_2 - r_2 \le \dots \le q_n - r_n \tag{S-MON}$$

Assumption (R-MON) states that the reservation values increase with type. This assumption is equivalent to assuming $s_i \leq s_{i+1}$ for all i such that $s_i > q_1$. Assumption (S-MON) asserts that the surplus from trade $q_i - r_i$ increases with the seller's type, and is non-negative for all types. (S-MON) implies that it is always efficient to trade the good. Note that, together, (R-MON) and (S-MON) imply (Q-MON).

Canonical Certification. A disclosure rule $D = (\mathcal{C}, \mathbf{p})$ consists of a set of certificates $\mathcal{C} = \{C_1, \dots, C_m\}$ and a family of distributions $\mathbf{p} = (p_1, \dots, p_n)$. Each $p_i \in \Delta \mathcal{C}$ is a distribution over certificates, with the interpretation that when a good of type i is certified, it receives the certificate C_j with probability p_{ij} . Special cases of certification technologies are (i) full disclosure, where $\mathcal{C}^{FD} = \{C_1, \dots, C_n\}$ and $p_i = e_i$ for all i, ¹² and (ii) no disclosure, where $\mathcal{C}^{ND} = \{C\}$ and $p_i \equiv 1$ for all i.

In addition to the disclosure rule, the certifier commands a certification fee. In general, a fee schedule $f: I_n \times \mathcal{C} \to \mathbb{R}_+$ determines the fee to be paid by the seller if her good is of type i and receives the certificate C_j . Fee schedules encompass the following special cases:

- Flat fee: $f(i, C_i) \equiv F \in \mathbb{R}_+$ for all $i \in I_n$ and $j \in I_m$.
- Type-contingent fee: for every $i \in I_n$ there is a number F_i^t such that $f(i, C_j) \equiv F_i^t$ for all $j \in I_m$.
- Certificate-contingent fee: for every $j \in I_m$ there is a number F_j^c such that $f(i, C_j) \equiv F_j^c$ for all $i \in I_n$.

The certification game. A disclosure rule D together with a fee schedule f induce the following certification game.

- 1. Nature draws $i \in I_n$ according to π and reveals it to the seller;
- 2. Upon observing i, the seller decides whether to demand certification;
- 3. If the seller demands certification, the certifier draws a certificate C according to p, the seller makes the payment f;

Throughout we denote $e_i \in \mathbb{R}^n$ the *i*-th unit vector, i.e., $e_{ii} = 1$ and $e_{ij} = 0$ for all $j \neq i$.

Fee structure	Disclosure	Papers
	_	Doherty et al. (2012), Lizzeri (1999), Loerke & Niedermayer (2018),
flat	endogenous	Opp et al. (2013), Pollrich & Wagner (2016), Viscusi (1978)
	exogenous	Bolton et al. (2012), Bouvard & Levy (2018), Durbin (1999), Farhi et al. (2013), Mathis et al. (2009), Skreta & Veldkamp (2009), Stahl & Strausz (2017), Strausz (2005)
	endogenous	Faure-Grimaud et al. (2009), Kovbasyuk (2018)
certificate		Fulghieri et al. (2014), Bar-Isaac & Shapiro (2013),
contingent	exogenous	Peyrache & Quesada (2011)
type	endogenous	
contingent	exogenous	Frenkel (2015)

Table 1: Classification of the literature on certification in markets with adverse selection. Not listed are Ozerturk (2014) and Bizzotto & Vigier (2021), who both explicitly compare flat to certificate-contingent fees.

- 4. The certificate is publicly disclosed, and the seller decides whether to offer the good for sale;
- 5. Buyers update their belief about the good, based on the published certificate and the seller's decision to offer the good for sale, and pay the price equal to the expected quality.

Remarks. Assumptions (R-MON) and (S-MON) are satisfied in all models on certification in adverse selection markets that have been studied in the literature. In his seminal work, Akerlof (1970) assumes that $s_i = \alpha q_i$ for $\alpha \in (0,1)$, which yields $r_i = \max\{\alpha q_i, q_1\}$ and $q_i - r_i = \min\{(1 - \alpha)q_i, q_i - q_1\}$. (R-MON) and (S-MON) are then implied by (Q-MON), i.e., that quality is increasing in type. Numerous authors assume $s_i \leq q_1$, for which our conditions are naturally satisfied. Lizzeri (1999) brings forward another specification with $s_i = q_i - \alpha$. In our terminology we thus get $r_i = \max\{q_i - \alpha, q_1\}$, and $q_i - r_i = \min\{\alpha, q_i - q_1\}$. Again, (R-MON) and (S-MON) are implied by (Q-MON).

Our timing implicitly assumes that the seller's decision whether to certify is observable. For our results this assumption is without loss. Unobservability of the certification decision only matters if the disclosure rule allows for non-certification as an outcome, i.e., the entries of the vectors p_i do not have to add up to one. Also, the seller cannot hide the certificate, in case she is not satisfied with the outcome. In our results, the seller never wishes to do so. Our model however does allow the seller not to sell the good after an (unlucky) certification outcome.

The main driver of our irrelevance results is the assumption that certification schemes do not only specify a fee structure but also a disclosure rule, because the disclosure rule then can act as a substitute for the fee structure. For this reason, Table 1 classifies the work on

¹³Akerlof assumes $q_1 = 0$, hence $r_i = s_i$ in our terminology.

certification in adverse selection markets according to their underlying assumptions about the fee structure and whether the disclosure rule can be (at least in parts) endogenously chosen. It reveals that, except for Frenkel (2015), the literature either assumes a fee structure that is flat or certificate-contingent. About half the studies assume that the certification rule is endogenous, whereas the other half of the literature studies fixed certification rules and, thereby, mostly those that lead to full revelation.

3 Profit-Maximizing Certification

In this section, we focus on profit-maximizing certification. We first derive the maximal certifier profit under the most flexible fee structure. We next show that the certifier attains this profit also with less flexible fee structures and, in particular, with a flat fee.

To derive an upper bound on the certifier's profit note that trading a good of type i generates at most a surplus of q_i and does so if the buyer obtains the good i. Hence, an obvious upper bound on the certifier's profit is the ex ante expected consumption value $\sum_i \pi_i q_i$. However, each seller-type also has the option to sell the good without certification, which yields a price weakly above q_1 , or to consume it by herself, which yields s_i . Taking into account the resulting outside option for the seller, the surplus the certifier can extract from a seller with a good of type i is at most $q_i - r_i$, which is non-negative as $q_i \geq s_i$. Hence, an upper bound on the certifier profit is given by

$$S^* := \sum_{i=1}^n \pi_i (q_i - r_i). \tag{1}$$

Proposition 1. The certifier obtains the profit S^* with a fully revealing disclosure rule D and a type-contingent fee schedule f with $F_i^t = q_i - r_i$ for all $i \in I_n$.

Proof. Let the disclosure rule be fully revealing, i.e., $C = \{C_1, \ldots, C_n\}$ and $p_i = e_i$. Set $f^*(i, C_j) = q_i - r_i$ for all i, j.¹⁴ We verify that there exists an equilibrium in which the seller always demands certification. To see this, choose the following off-path beliefs: buyers believe uncertified goods are of the lowest quality q_1 with probability one, hence an uncertified good sells at price q_1 . If every seller-type certifies, then a good that is offered and carries certificate C_j sells at price q_j . Seller-type i's payoff from certification is $q_i - f^*(i, C_i) = q_i - q_i + r_i = r_i$. Hence, type i prefers selling the good certified to either selling it uncertified (at a price q_1) or keeping the good for herself (and realizing value s_i). We have thus shown that it is an equilibrium that all seller types demand certification. The certifier's profit in this equilibrium equals S^* .

Using a type-contingent fee schedule, Proposition 1 resembles classical results on first-

¹⁴Given that under full disclosure, a good i can only get certificate C_i , only the fees $f(i, C_i)$ play a role in verifying the equilibrium of the certification game.

degree price discrimination. The certifier charges each seller-type an amount equal to this type's willingness to pay (WTP) for certification. This WTP depends on the seller's outside option, which is either consuming the good herself or selling it uncertified. The maximum profit S^* is attained by making the latter option as unattractive as possible via inducing the off-path belief that an uncertified good has the lowest quality.

Our first equivalence result is that the certifier can also obtain the profit S^* with a certificate-contingent fee:

Proposition 2. The certifier obtains the profit S^* with a fully revealing disclosure rule D (i.e. m = n) and a certificate-contingent fee schedule f with $F_j^c = q_j - r_j$ for all $j \in I_n$.

The result is a direct corollary of Proposition 1 because the certifier uses a disclosure rule that fully reveals the seller's type. Hence, the issued certificate equals the seller's type and charging the fee based on the certificate is equivalent to charging the fee based on the discovered type.

We finally show the main result of this section: the certifier can attain the profit S^* with a flat fee. Deriving this result is more subtle as the certifier cannot obtain S^* with a flat fee using a fully revealing disclosure rule. Indeed, if she could do so, then necessarily the flat fee has to equal $F \equiv S^*$, but, to low seller types, paying the fee S^* for a fully disclosing certificate is not worthwhile. Hence, if a flat fee is able to attain the profit S^* , it has to do so with a disclosure rule D that is not fully revealing. In particular, the disclosure rule must ensure that all seller types are willing to pay the flat certification fee S^* and also induce them to sell their good independent of the specific certification outcome.

The main insight of the next proposition is that this is possible for any prior π . Hence, our next equivalence result holds regardless of the prior π , but the disclosure rule that sustains it depends on the prior π in a carefully calibrated way and does not yield a fully transparent market outcome, where all private information is fully disclosed to all market participants.

Proposition 3. For every prior π there exists a certification technolo D with a flat fee schedule $f = S^*$ such that the certification game induced by (D, f) exhibits an equilibrium in which the certifier's profit is S^* .

Before proving Proposition 3, we first state the following more technical sounding lemma.

Lemma 1. Suppose $\mathbf{u} \in \mathbb{R}^n$ satisfies

$$u_1 \le u_2 \le \ldots \le u_n,$$
 (U-MON)

$$q_1 - u_1 \le q_2 - u_2 \le \dots \le q_n - u_n,$$
 (S-MON')

$$\sum_{i} \pi_{i} q_{i} = \sum_{i} \pi_{i} u_{i}, \tag{F-SUM}$$

$$r_i \le u_i, \quad \forall i = 1, \dots, n.$$
 (F-IN)

Let $\mathcal{I}_{-} := \{i | q_i - u_i < 0\}, \mathcal{I}_{0} := \{i | q_i - u_i = 0\} \text{ and } \mathcal{I}_{+} := \{i | q_i - u_i > 0\}.$ There exists a disclosure rule $D = (\mathcal{C}, \mathbf{p})$ with $\mathcal{C} = \{C_1, \dots, C_n\}$ and

$$p_i = e_i \text{ for all } i \in \mathcal{I}_0 \cup \mathcal{I}_+,$$
 (ID)

$$p_{ij} = 0 \text{ for all } i \in \mathcal{I}_- \text{ and } j \in (\mathcal{I}_- \cup \mathcal{I}_0) \setminus \{i\},$$
 (UP)

such that in the certification game induced by D (with zero fee) every type i demands certification, sells the certified good, and obtains expected utility u_i from certification.

For a given vector $\mathbf{u} \in \mathbb{R}^n$ that describes the targeted utility for each of the n seller types, the lemma partitions types into three subsets. A set \mathcal{I}_{-} that contains all types, whose target utility u_i strictly exceeds their true quality q_i . A set \mathcal{I}_0 that contains types whose utility matches their quality. The set \mathcal{I}_+ that contains the remaining types; those where the quality level exceeds their utility target. (S-MON') implies that \mathcal{I}_{-} contains only low types, while \mathcal{I}_+ contains only high types. Hence, a pooling of types from $\mathcal{I}_$ with types from \mathcal{I}_+ naturally increases the expected utility from certification for low types, while reducing it for high types. The insight of the lemma is that, under the conditions (U-MON), (S-MON') and (F-SUM), there is a disclosure rule that guarantees each type i his targeted expected utility of u_i , while only using such "upward-pooling". In the proof presented below, we derive this disclosure rule constructively using an induction argument on the number of types. In particular, we construct the certificate for some type $k^* \in \mathcal{I}_+$, such that the sub-market—resulting from the remaining mass of types, after pooling some mass of \mathcal{I}_{-} together with type k^{\star} —satisfies the conditions of the lemma. The disclosure rule for the original market results from combining the disclosure rule from the sub-market with the constructed certificate for k^* . Property (F-IN) ensures that every seller-type is then willing to sell the certified good.¹⁵

While more technical, the lemma is informative about the structural properties of the associated disclosure rule. Moreover, it not only allows us to prove Proposition 3, but also extend our study of fee structures beyond profit-maximizing certifiers. In the next section, we use it to study the ability of different fee structures in supporting different non-profit-maximizing distributions of rents between the certifier and the seller. Before proving Lemma 1, we first show that it yields Proposition 3 and also provide two examples that highlight the role of properties (R-MON) and (S-MON) for the result.

Proof of Proposition 3. We apply Lemma 1 as follows. For all i = 1, ..., n define $u_i = r_i + S^*$. Equation (R-MON) implies (U-MON), and (S-MON) implies (S-MON'). By definition $S^* > 1$

¹⁵Indeed, this (ex post) possibility for the seller to retain the good after it is certified prevents us from proving Proposition 3 using the popular majorization techniques from information design. This is so, because we follow the literature in (naturally) requiring that the seller must be willing to sell his certified good for the *realized* rather than the *expected* certificate. As such an ex post requirement is stronger than an interim one, our results would not change if we had only imposed that the seller must be willing to sell his certified good before learning the obtained certificate.

0, which yields (F-IN). Finally,

$$\sum_{i=1}^{n} \pi_i u_i = \sum_{i=1}^{n} \pi_i (r_i + S^*) = \sum_{i=1}^{n} \pi_i r_i + \sum_{i=1}^{n} \pi_i (q_i - r_i) = \sum_{i=1}^{n} \pi_i q_i,$$

i.e., (F-SUM) holds. Lemma 1 implies there is a disclosure rule D with the described properties. Now add to D the flat certification fee $F^* = S^*$. We verify there is an equilibrium in which every seller-type demands certification, and offers the certified good for sale. As before, choose the out-of-equilibrium beliefs that an uncertified good is of the lowest quality q_1 .¹⁶ By construction of the disclosure rule from Lemma 1, every type sells the certified good, and this decision is independent of the (previously sunk) certification fee. Type i's expected utility from certifying at the certification fee F^* is $u_i - S^* = r_i$. Hence, every type prefers certification over keeping the good or selling it uncertified. Because all seller-types demand certification, the certifier's profit equals S^* .

Example 1 (Necessity of (R-MON)). Consider a market with three seller types, $q_1 < q_2 < q_3$ and assume $r_2 > r_3 > r_1 = q_1$, violating (R-MON). Define

$$\bar{q}_{23} \coloneqq \frac{\pi_2}{\pi_2 + \pi_3} q_2 + \frac{\pi_3}{\pi_2 + \pi_3} q_3$$

We have that $S^* = \pi_2(q_2 - r_2) + \pi_3(q_3 - r_3) = \bar{q}_{23} - r_2 + \pi_3(r_2 - r_3) - \pi_1(\bar{q}_{23} - r_2)$. In particular, $S^* > \bar{q}_{23} - r_2$ whenever $\pi_3/\pi_1 > \bar{q}_{23} - r_2/r_2 - r_3 > 0$. For any disclosure rule, type 2's expected payoff from certification is at most $\bar{q}_{23} - f$, where that bound results from pooling all q_3 -types together with type q_2 . That is, a necessary condition for type 2's participation is $\bar{q}_{23} - f \ge r_2$. But then, $f \le \bar{q}_{23} - r_2 < S^*$, whenever $\pi_3/\pi_1 > \bar{q}_{23} - r_2/r_2 - r_3$.

Example 2 (Necessity of (S-MON)). Consider a market with three seller types, $q_1 < q_2 < q_3$ and assume $q_2 - r_2 > q_3 - r_3 > q_1 - r_1 = 0$. Again, we have $S^* = \pi_2(q_2 - r_2) + \pi_3(q_3 - r_3)$. Note that $S^* > q_3 - r_3$ whenever $\pi_2/1 - \pi_3 > q_3 - r_3/q_2 - r_2$. Type 3's payoff from certification is at most $q_3 - f$. To guarantee that type's participation requires $q_3 - f \ge r_3$. But then, $f \le q_3 - r_3 < S^*$, whenever $\pi_2/1 - \pi_3 > q_3 - r_3/q_2 - r_2$.

Finally, we close this section with a proof of Lemma 1.

Proof of Lemma 1. We proceed by induction over n. In all cases of the proof, we will construct equilibria in which all seller types demand certification. Regarding the off-path event that an uncertified good is offered for sale, we assume the buyer believes it is of the lowest quality, hence it sells at a price q_1 . Throughout, we denote v_j the price at which a C_j -certified good sells in the equilibrium under consideration.

¹⁶These out-of-equilibrium beliefs are not only natural, but also robust in the sense that they are the limit of equilibria with only on-path beliefs, where the lowest type does not get certified with a probability that vanishes to zero.

¹⁷This condition holds for instance if $\pi_1 = \pi_3 = \varepsilon/2$ and $\varepsilon \to 0$. We have that $\pi_2/1 - \pi_3 = 2 - 2\varepsilon/2 - \varepsilon \to 1$, and by assumption $q_3 - r_3/q_2 - r_2 \in (0, 1)$.

We start by proving the claim for n = 2. By (F-SUM) we have that $1 \in \mathcal{I}_0$ if and only if $2 \in \mathcal{I}_0$. Hence, if $\mathcal{I}_0 \neq \emptyset$ a fully revealing disclosure rule with $p_i = e_i$ yields the desired result.

If $\mathcal{I}_0 = \emptyset$ conditions (U-MON), (F-SUM) and (S-MON') imply that $q_1 < u_1 \le u_2 < q_2$. Hence, $1 \in \mathcal{I}_-$ and $2 \in \mathcal{I}_+$. Consider a disclosure rule with $\mathcal{C} = \{C_1, C_2\}$, and $p_1 = (u_2 - u_1/u_2 - q_1, u_1 - q_1/u_2 - q_1)$ as well as $p_2 = (0, 1)$. Clearly, this rule satisfies (ID) and (UP). Suppose both seller types demand certification. We have $v_1 = q_1$, and

$$\begin{array}{lll} v_2 & = & \frac{\pi_1 p_{12}}{\pi_1 p_{12} + \pi_2} q_1 + \frac{\pi_2}{\pi_1 p_{12} + \pi_2} q_2 \\ & = & \frac{\pi_1 (u_1 - q_1)}{\pi_1 (u_1 - q_1) + \pi_2 (u_2 - q_1)} q_1 + \frac{\pi_2 (u_2 - q_1)}{\pi_1 (u_1 - q_1) + \pi_2 (u_2 - q_1)} q_2 \\ & \stackrel{(\text{F-SUM})}{=} & \frac{\pi_1 (u_1 - q_1)}{\pi_2 (q_2 - q_1)} q_1 + \frac{\pi_2 (u_2 - q_1)}{\pi_2 (q_2 - q_1)} q_2 \\ & \stackrel{(\text{F-SUM})}{=} & \frac{\pi_2 (q_2 - u_2) q_1 + \pi_2 (u_2 - q_1) q_2}{\pi_2 (q_2 - q_1)} \\ & = & u_2 \end{array}$$

Because $u_2 \ge r_2$, the type-2 seller indeed demands certification and sells the certified good. For the type-1 seller we have that $u_2 = v_2 > q_1 \ge r_1$. Hence, this type sells the certified good for either of the two certificates. That type's expected value from certification is $p_{11}u_1 + p_{12}u_2 = q_1 + p_{12}(u_2 - q_1) = q_1 + u_1 - q_1 = u_1$. Hence, both types demand certification. This completes the proof for n = 2.

Now suppose the claim is proven for every $\tilde{n} \leq n-1$. We prove it also holds for n.

<u>Case 1:</u> $|\mathcal{I}_0| = k \ge 1$. By (S-MON') there are $1 \le \underline{k} < \overline{k} \le n$ such that $\mathcal{I}_- = \{1, \dots, \underline{k} - 1\}$ and $\mathcal{I}_+ = \{\overline{k} + 1, \dots, n\}$. We construct a sub-market of size n - k with 18

$$(\widetilde{q}_i, \widetilde{r}_i, \widetilde{u}_i) = \begin{cases} (q_i, r_i, u_i), & i = 1, \dots, \underline{k} - 1, \\ (q_{i+k}, r_{i+k}, u_{i+k}), & i = \underline{k} + 2, \dots, n - k, \end{cases}$$

and prior belief $\widetilde{\pi}$

$$\widetilde{\pi}_i = \frac{\pi_i}{\sum_{j \in \mathcal{I}_- \cup \mathcal{I}_+} \pi_j}.$$

Using the respective conditions for the original market, the sub-market satisfies conditions (U-MON), (S-MON') and (F-IN). Because $q_i = u_i$ for all $i \in \mathcal{I}_0$ it also satisfies (F-SUM). For the submarket we have that $\widetilde{\mathcal{I}}_- = \mathcal{I}_-$, $\widetilde{\mathcal{I}}_+ = \{\underline{k}, \dots, n-k\}$, and $\widetilde{\mathcal{I}}_0 = \emptyset$. By induction hypothesis there exists a disclosure rule \widetilde{D} with $\widetilde{\mathcal{C}} = \{\widetilde{C}_1, \dots, \widetilde{C}_{n-k}\}$, $\widetilde{p}_i = e_i$ for all $i \in \widetilde{\mathcal{I}}_+$, and $\widetilde{p}_{ij} = 0$ whenever $i \in \widetilde{\mathcal{I}}_-$ and $j \in \widetilde{\mathcal{I}}_- \setminus \{i\}$.

Now consider the following disclosure rule for the original market: $C = \{C_1, \ldots, C_n\}$,

Note that, if $\mathcal{I}_0 = \{1, \dots, n\}$ this sub-market is empty. Trivially, full disclosure yields the desired result.

 $p_i = e_i \text{ for } i \in \mathcal{I}_0, \text{ and for } i \in \mathcal{I}_- \cup \mathcal{I}_+$

$$p_{ij} = \begin{cases} \widetilde{p}_{ij}, & \text{if } j \in \mathcal{I}_{-}, \\ 0, & \text{if } j \in \mathcal{I}_{0}, \\ \widetilde{p}_{ij-k}, & \text{if } j \in \mathcal{I}_{+}. \end{cases}$$

By construction and from the induction hypothesis this disclosure rule satisfies (ID) and (UP). Now suppose every seller-type demands certification in equilibrium. For any $i \in \mathcal{I}_- \cup \mathcal{I}_0$ the certificate C_i is solely awarded to type i, hence $v_i = q_i$. Furthermore, for any $j \in \mathcal{I}_+$ the respective certificate C_j has the same composition as in the sub-market described above, hence $v_j = u_j$. This implies that every seller-type indeed offers the certified good for sale. Also, for every type $j \in \mathcal{I}_0 \cup \mathcal{I}_+$ we have that $p_j = e_j$ and $v_j = u_j \geq r_j$, hence any such type demands certification. Any type $i \in \mathcal{I}_-$ has the same expected payoff from certification as in the sub-market, namely \tilde{u}_i . By construction $\tilde{u}_i = u_i \geq r_i$, hence also these types demand certification.

<u>Case 2:</u> $\mathcal{I}_0 = \emptyset$. In this case (S-MON') together with (F-SUM) implies existence of a unique $k \in \{1, \ldots, n-1\}$ such that $\mathcal{I}_- = \{1, \ldots, k\}$ and $\mathcal{I}_+ = \{k+1, \ldots, n\}$. Define $\widehat{\boldsymbol{\alpha}} = (\widehat{\alpha}_1, \ldots, \widehat{\alpha}_k)$ via

$$\widehat{\alpha}_i = \frac{u_i - q_i}{u_{k+1} - q_i}, \qquad i = 1, \dots, k.$$

Because $u_{k+1} - q_i \ge u_i - q_i > 0$ we have that $\widehat{\alpha}_i \in (0,1]$ for all $i = 1, \dots, k$. Define the set $\mathcal{A} \subset [0,1]^k$ as follows. $\boldsymbol{\alpha} = (\alpha_1, \dots, \alpha_k) \in \mathcal{A}$ if and only if for all $i = 1, \dots, k-1$

$$u_{i+1} - \frac{\alpha_{i+1}}{1 - \alpha_{i+1}} (u_{k+1} - u_{i+1}) \ge u_i - \frac{\alpha_i}{1 - \alpha_i} (u_{k+1} - u_i)$$
(2)

$$q_{i+1} - u_{i+1} + \frac{\alpha_{i+1}}{1 - \alpha_{i+1}} (u_{k+1} - u_{i+1}) \ge q_i - u_i + \frac{\alpha_i}{1 - \alpha_i} (u_{k+1} - u_i)$$
(3)

and $\alpha_i \leq \widehat{\alpha}_i$ for all i = 1, ..., k. The set \mathcal{A} is a connected subset of $[0, 1]^k$, endowed with the Euclidean metric.

Consider the mapping $f: \mathcal{A} \to \mathbb{R}$ given by

$$f(\alpha_1, \dots, \alpha_k) = \sum_{i=1}^k \alpha_i \pi_i (q_i - u_{k+1}) + \pi_{k+1} (q_{k+1} - u_{k+1}).$$
 (4)

By assumptions (U-MON) and (S-MON) we have $(0, ..., 0) \in \mathcal{A}$, and $f(0, ..., 0) = \pi_{k+1}(q_{k+1} - u_{k+1}) > 0$. Further, note that

$$\frac{\widehat{\alpha}_i}{1 - \widehat{\alpha}_i} (u_{k+1} - u_i) = u_i - q_i,$$

and thus $\widehat{\boldsymbol{\alpha}} = (\widehat{\alpha}_1, \dots, \widehat{\alpha}_k) \in \mathcal{A}$. We have

$$f(\widehat{\alpha}) = \sum_{i=1}^{k} \frac{u_i - q_i}{u_{k+1} - q_i} \pi_i (q_i - u_{k+1}) + \pi_{k+1} (q_{k+1} - u_{k+1})$$

$$= \sum_{i=1}^{k+1} \pi_i (q_i - u_i) \stackrel{\text{(F-SUM)}}{=} - \sum_{i=k+2}^{n} \pi_i (q_i - u_i) < 0,$$

where the strict inequality follows from $\{k+2,\ldots,n\}\subset\mathcal{I}_+$. Since f is continuous and \mathcal{A} connected, the image $f(\mathcal{A})\subset\mathbb{R}$ is an interval, due to the intermediate value theorem. Hence, there exists $\boldsymbol{\alpha}^{\star}=(\alpha_1^{\star},\ldots,\alpha_k^{\star})\in\mathcal{A}$ such that $f(\boldsymbol{\alpha}^{\star})=0$. Hence,

$$\sum_{i=1}^{k} \alpha_i^{\star} \pi_i q_i + \pi_{k+1} q_{k+1} = \left(\sum_{i=1}^{k} \alpha_i^{\star} \pi_i + \pi_{k+1} \right) u_{k+1}.$$
 (5)

We use α^* to construct a sub-market of size n-1, by dropping type k+1 and adjusting the target utilities u for types $1, \ldots, k$. Formally, let

$$(\widetilde{q}_i, \widetilde{r}_i) = \begin{cases} (q_i, r_i), & i = 1 \dots, k \\ (q_{i+1}, r_{i+1}), & i = k+1, \dots, n-1 \end{cases}$$

and

$$\widetilde{u}_{i} = \begin{cases} u_{i} - \frac{\alpha_{i}^{\star}}{1 - \alpha_{i}^{\star}} (u_{k+1} - u_{i}), & i = 1 \dots, k \\ u_{i+1}, & i = k+1, \dots, n-1 \end{cases}$$

and

$$\widetilde{\pi}_{i} = \begin{cases} \frac{(1-\alpha_{i}^{\star})\pi_{i}}{\sum_{j=1}^{k} (1-\alpha_{j}^{\star})\pi_{j} + \sum_{l=k+2}^{n} \pi_{l}}, & i = 1 \dots, k \\ \frac{\pi_{i+1}}{\sum_{j=1}^{k} (1-\alpha_{j}^{\star})\pi_{j} + \sum_{l=k+2}^{n} \pi_{l}}, & i = k+1, \dots, n-1. \end{cases}$$

We verify that $(\widetilde{q}, \widetilde{r}, \widetilde{u})$ satisfies the conditions of the lemma. We have $\widetilde{u}_i \leq u_i$ for all i = 1, ..., k, hence (2) together with (U-MON) for the original market imply that the sub-market satisfies (U-MON). By construction $\alpha_i^* \leq \widehat{\alpha}_i$, and thus $q_i - \widetilde{u}_i \leq 0$ for all i = 1, ..., k. Hence, (3) together with (S-MON') for the original market imply (S-MON') for the sub-market. (F-IN) for the sub-market holds, because it holds for the original market

and $\widetilde{u}_i \geq q_i \geq r_i$ for all $i = 1, \ldots, k$. To see that (F-SUM) holds, observe that

$$\sum_{j=1}^{n-1} \widetilde{\pi}_{j} (\widetilde{q}_{j} - \widetilde{u}_{j}) = \frac{\sum_{i=1}^{k} (1 - \alpha_{i}^{\star}) \pi_{i} \left(q_{i} - u_{i} + \frac{\alpha_{i}^{\star}}{1 - \alpha_{i}^{\star}} (u_{k+1} - u_{i}) \right) + \sum_{l=k+2}^{n} \pi_{l} (q_{l} - u_{l})}{\sum_{j=1}^{k} (1 - \alpha_{j}^{\star}) \pi_{j} + \sum_{l=k+2}^{n} \pi_{l}}$$

$$= \frac{\sum_{i=1}^{k} \pi_{i} \left((1 - \alpha_{i}^{\star}) (q_{i} - u_{i}) + \alpha_{i}^{\star} (u_{k+1} - u_{i}) \right) + \sum_{l=k+2}^{n} \pi_{l} (q_{l} - u_{l})}{\sum_{j=1}^{k} (1 - \alpha_{j}^{\star}) \pi_{j} + \sum_{l=k+2}^{n} \pi_{l}}$$

$$= \frac{\sum_{i=1}^{k} \pi_{i} \alpha_{i}^{\star} (u_{k+1} - q_{i}) + \sum_{l \neq k+1} \pi_{l} (q_{l} - u_{l})}{\sum_{j=1}^{k} (1 - \alpha_{j}^{\star}) \pi_{j} + \sum_{l=k+2}^{n} \pi_{l}}$$

$$= \frac{\pi_{k+1} (q_{k+1} - u_{k+1}) + \sum_{l \neq k+1} \pi_{l} (q_{l} - u_{l})}{\sum_{j=1}^{k} (1 - \alpha_{j}^{\star}) \pi_{j} + \sum_{l=k+2}^{n} \pi_{l}}$$

$$= 0,$$

where the penultimate equality uses $f(\boldsymbol{\alpha}^*) = 0$, and the last equality follows from (F-SUM) for the original market. Hence, the sub-market satisfies all conditions from the lemma. Note that in the sub-market we have $\widetilde{\mathcal{I}}_+ = \{k+1,\ldots,n-1\}$. By induction hypothesis there exists $(\widetilde{p}_1,\ldots,\widetilde{p}_{n-1})$, such that the associated disclosure game has the desired properties. In particular $\widetilde{p}_j = e_j$ for all j > k, and $\widetilde{p}_{ij} = 0$ if $i,j \leq k$ and $i \neq j$. Note that in the sub-market the value of certificate C_j is $\widetilde{v}_j = q_j$ if $j = 1,\ldots,k$ and $\widetilde{v}_j = \widetilde{u}_j = u_{j+1}$ if $j = k+1,\ldots,n-1$

To complete the proof, consider the following disclosure rule for the grand market: $C = \{C_1, \ldots, C_n\}$, $p_j = e_j$ for j > k, and for $i \le k$ set

$$p_{ij} = \begin{cases} \widetilde{p}_{ij}(1 - \alpha_i^*), & j < k + 1, \\ \alpha_i^*, & j = k + 1, \\ \widetilde{p}_{ij-1}(1 - \alpha_i^*), & j > k + 1. \end{cases}$$

The properties of $\widetilde{\mathbf{p}}$ imply that the disclosure rule satisfies (ID) and (UP).

Finally assume that all types demand certification in equilibrium. Then, by construction $v_i = q_i$ for all i = 1, ..., k. We have $v_{k+1} = u_{k+1}$ by construction of $\boldsymbol{\alpha}^*$. The properties of the sub-market yield $v_i = u_i$ for all i = k+2, ..., n. Then, (ID) and (UP) imply that each seller-type offers the certified good for sale for any certificate she obtains with positive probability. For type $i \in \mathcal{I}_+$ the expected value from certification is $v_i = u_i$, while for type

 $i \in \mathcal{I}_{-}$ it is

$$\sum_{j=1}^{n} p_{ij}v_{j} = \sum_{j=1}^{k} \widetilde{p}_{ij}(1 - \alpha_{i}^{\star})v_{j} + \alpha_{i}^{\star}v_{k+1} + \sum_{j=k+2}^{n} \widetilde{p}_{ij-1}(1 - \alpha_{i}^{\star})v_{j}$$

$$= (1 - \alpha_{i}^{\star}) \sum_{j=1}^{n-1} \widetilde{p}_{ij}\widetilde{v}_{j} + \alpha_{i}^{\star}u_{k+1}$$

$$= (1 - \alpha_{i}^{\star})\widetilde{u}_{i} + \alpha_{i}^{\star}u_{k+1}$$

$$= (1 - \alpha_{i}^{\star}) \left(u_{i} - \frac{\alpha_{i}^{\star}}{1 - \alpha_{i}^{\star}} (u_{k+1} - u_{i}) \right) + \alpha_{i}^{\star}u_{k+1}$$

$$= u_{i}.$$

where the third inequality uses the induction hypothesis. Hence, all types demand certification. We have thus verified existence of the desired equilibrium in the original market. \Box

4 Implementable Rent Distributions

In the previous section, we focused on a profit-maximizing certifier. In this section, we take a more general view and study the extent to which fee structures affect the ability to implement different distributions of rents among the certifier and different seller types. Such implementation concerns become relevant when regulators want, next to the fee structures, to influence also the certifier's objectives; or the certifier represents a self-regulated organization set up by the sellers themselves; or the certifier is a non-profit organization.¹⁹ Characterizing the implementable distributions of rents under the fee structures of type-contingent, certificate-contingent, and flat fees, we focus on efficient allocations, i.e., where certification leads to efficient trade in equilibrium.

A rent vector (S, u_1, \ldots, u_n) specifies the certifier's (expected) profit S and each seller type's utility u_1, \ldots, u_n . A rent vector is *feasible* if

$$S \ge 0,$$
 (C-IR)

and

$$u_i \ge r_i, \quad \forall i.$$
 (S-IR)

An efficient allocation gives rise to the aggregate surplus $\sum_i \pi_i q_i$. This aggregate surplus is distributed between the certifier and the seller types. A rent vector is exhaustive if

$$S + \sum_{i} \pi_i u_i = \sum_{i} \pi_i q_i. \tag{EX}$$

¹⁹See Zapechelnyuk (2020) or Vellodi (2021) for models where, rather than profits, the certifier maximizes welfare or consumer surplus.

Our next result establishes that certification with type- or certificate-contingent fees allows for implementing any rent vector that is feasible and exhaustive.

Proposition 4. Any rent vector (S, u_1, \ldots, u_n) that is feasible and exhaustive can be implemented by certification with a type- or certificate-contingent fee.

Proof. Let the disclosure rule be fully revealing and take the fee structure $f(i, C_j) = q_i - u_i$ for all i, j (resp. $f(i, C_j) = q_j - u_j$ for a certificate-contingent fee). We verify there exists an equilibrium in which the seller always demands certification, and that implements the desired rents. If all seller types demand certification, a good with certificate C_i sells at a price q_i and in equilibrium sellers do sell their certified goods. Choose the out-of-equilibrium belief that an uncertified good is of the lowest quality with probability one. Hence, an uncertified good sells at a price q_1 . Seller type i obtains $q_i - f(i, C_i) = q_i - (q_i - u_i) = u_i$ from certification. Not certifying yields r_i . Feasibility then implies that every seller-type demands certification. Using (EX) and (C-IR) the certifier's profit is $\sum_i \pi_i f(i, C_i) = \sum_i \pi_i (q_i - u_i) = S \ge 0$. \square

Proposition 4 resembles once more classical results on first-degree price discrimination. In conjunction to revealing the seller's type publicly, the certifier charges each seller-type the difference between her contribution to surplus q_i and her designated utility level u_i . Via subsidies (i.e., negative fees) the certifier can shift rents across types. Re-distribution is limited by each individual's outside option, given by the above feasibility constraints, and by the fact that the certifier is the residual claimant of the surplus after re-distribution across seller types. As before, there is essentially no difference between type- and certificate-contingent fees, because the fully revealing disclosure rule allows for inferring the true type from the issued certificate.

When restricted to the use of flat fees, surplus can, by contrast, not be re-distributed via monetary payments, leaving the disclosure rule as the sole channel for redistribution. This introduces additional constraints on implementable rent distributions.

Proposition 5. Any rent vector $(S, u_1, ..., u_n)$ that is feasible, exhaustive and satisfies (U-MON) and (S-MON') can be implemented by certification with a flat fee.

Proof. We apply Lemma 1 to the vector of utilities $\mathbf{u}' = (u'_1, \dots, u'_n)$ where $u'_i = u_i + S$. Conditions (U-MON) and (S-MON') are invariant upon adding constants, hence \mathbf{u}' satisfies them, as by assumption (u_1, \dots, u_n) satisfies them. Similarly, \mathbf{u}' satisfies (F-IN), because we have $u'_i = u_i + S \ge r_i$ due to (C-IR) and (S-IR). Finally, \mathbf{u}' satisfies (F-SUM), because

$$\sum_{i} \pi_i u_i' = \sum_{i} \pi_i u_i + S \stackrel{\text{(EX)}}{=} \sum_{i} \pi_i q_i.$$

Hence, the vector \mathbf{u}' satisfies all the conditions from Lemma 1. It is straightforward to verify that the resulting disclosure rule together with a (possibly non-zero) fee S implements rent vector (S, u_1, \ldots, u_n) .

The additional constraints (U-MON) and (S-MON') arise because redistribution via the disclosure rule is limited by Bayes' consistency. Hence, it is not possible to reduce the utility of some seller type below the average resulting from that type with the lowest type. Unlike monetary payments, probabilities cannot become negative. Though it is possible to find specific rent distributions that can be implemented with a flat certification fee while violating (U-MON) or (S-MON'), the next two examples show that this is not possible in general.

Example 3 (Necessity of (U-MON)). Suppose n = 2 and assume (S, u_1, u_2) satisfies (C-IR), (S-IR) and (EX). In addition assume $u_1 > u_2$. Let $(u'_1, u'_2) = (u_1 + S, u_2 + S)$. A disclosure rule with flat fee S implements utilities (u_1, u_2) if and only if a disclosure rule with flat fee 0 implements utilities (u'_1, u'_2) . Note that $u_1 > u_2$ implies $u'_1 > u'_2$. Then (EX) implies that $u'_1 > \bar{q} > u'_2$. But the utility of type 1 cannot be increased above \bar{q} by certification alone.

Example 4 (Necessity of (S-MON')). Suppose n = 2 and assume (S, u_1, u_2) satisfies (C-IR), (S-IR) and (EX). In addition assume $q_1 - u_1 > q_2 - u_2$. Again, add $S \ge 0$ to the utilities to get (u'_1, u'_2) which then satisfies $\pi_1 u'_1 + \pi_2 u'_2 = \pi_1 q_1 + \pi_2 q_2$ and $q_1 - u'_1 > q_2 - u'_2$. Together, these imply $q_1 - u'_1 > 0 > q_2 - u'_2$, and thus $u'_2 > q_2$. It is clearly impossible to implement such a utility vector with certification, because any certified good is worth less than q_2 .

5 Conclusion

We have proven our results abstracting from costs of certification. In practice, there are however (at least) two natural sources for certification costs. First, certification may require cost intensive investigations. Second, it is costly to generate and publicly reveal the respective certificate. For the former case it is natural to assume that costs are type-specific. Our results readily extend if we assume that it costs c_i to certify a type i seller. With a type-contingent fee certification of type i is optimal whenever $q_i - r_i \ge c_i$ and the certifier's maximal profit becomes

$$S_c^{\star} = \sum_{i} \pi_i \max \{q_i - r_i - c_i, 0\}.^{20}$$

To see that Proposition 3 continues to hold, observe that Lemma 1 is independent of certification costs. After dropping all seller-types that are not certified in the above procedure (i.e., all i such that $q_i - r_i < c_i$) we can apply the lemma to the resulting smaller market.

Matters are more delicate when the certification costs directly depend on the amount of information that the certifier discovers. For instance, it seems natural to assume this cost is increasing in the precision of certification.²¹ A corollary of our results is then that

²⁰As before, the certifier uses full disclosure and charges the fee $f(i, C_j) = q_i - r_i$ for all i, j s.t. $q_i - r_i \ge c_i$.
²¹See Pomatto et al. (2022) for an axiomatic foundation of such costs, or Ozerturk (2014) and Bizzotto and

the imprecise disclosure associated with a flat fee leads to less costs than the full disclosure associated with a type- or certificate-contingent fee structure and is socially superior.

While focusing on a single, monopolistic certifier and not explicitly modelling competition, our analysis on the distribution of rents is indicative of competitive pressures that lower monopolistic rents to the certifier. It is an exciting avenue for future research to study whether competition between certifiers yields additional insights about the economic effect of limitations on the fee structures in certification.

Because our irrelevance results are based on the ability of pooling different seller types and thereby requiring them to sell identical quantities, our results do not readily extend to settings beyond the unit-good case. This is so because when the efficient quantity of two seller types differ, then a pooling of these types reduces their flexibility in offering different quantities to buyers. On the other hand, our assumption that trade is always efficient does not impact our irrelevance results; any seller type i for whom trade is inefficient, i.e., for whom it holds that $q_i < s_i$, can be excluded with a disclosure rule that fully reveals its identity.

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Vigier (2021) for specific examples of such costs with binary certification outcomes, or Ball and Kattwinkel (2022) for a mechanism design foundation of such costs based on probabilistic verification.

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